



INT Program INT-17-3

Spatial and Momentum Tomography of Hadrons and Nuclei

August 28 – September 29, 2017

Heavy Quarkonium Production at EIC Energies

- ✧ Why heavy quarkonium?
- ✧ Production mechanism?
- ✧ EIC: Inclusive DIS, SIDIS, Exclusive, ...
- ✧ Gluon distribution, imaging, threshold, ...
- ✧ Summary and outlook

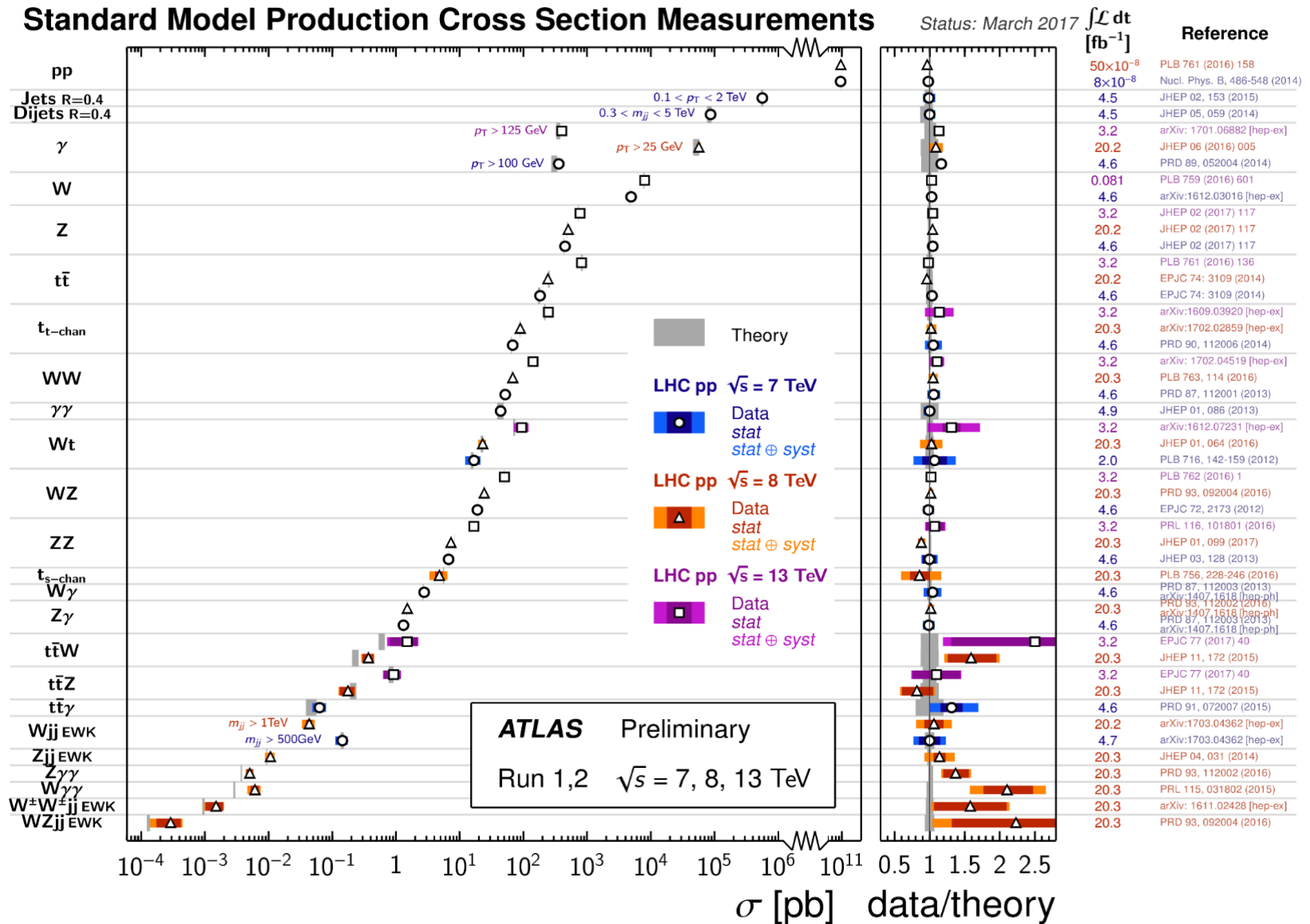


Theory Center

Jianwei Qiu



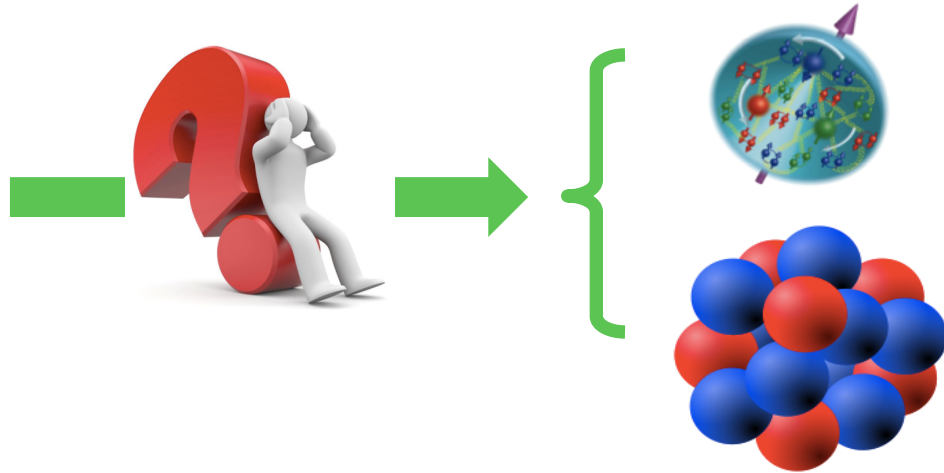
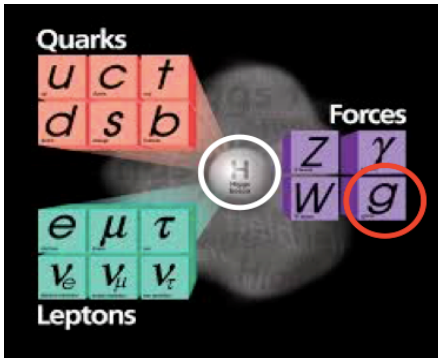
The great success of SM physics



SM: Electroweak processes + QCD perturbation theory works!

QCD – Final frontier of the SM physics

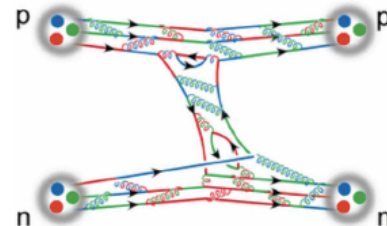
- How QCD works to get all of us? – the next QCD frontier!



- How hadrons are **emerged** from quarks and gluons?
- What is the quark/gluon **structure** of nucleon and nuclei?
- How does QCD make up the **properties** of hadrons?

Their mass, spin, magnetic moment, ...

- How does the **nuclear force** arise from QCD?
- ...



Why QCD is so hard to deal with?

- ❑ It is strongly coupled – nonlinear + nonperturbative!
- ❑ It is relativistic – nontrivial QCD vacuum!
- ❑ No localized heavy mass/charge center – nucleus in an atom!
- ❑ Gluons are “dark” and carry “color” – intellectual challenge!

How to probe the quark-gluon dynamics, quantify the hadron structure, study the emergence of hadrons, ..., if we cannot see quarks and gluons?

Heavy quarkonium:

- ✧ Heavy quark as relatively localized heavy mass/charge center
- ✧ Heavy quark in the pair's rest frame is almost non-relativistic
- ✧ Production of heavy quark pair could be perturbative
- ✧ Top decays too quickly, strange is too light, ...



Charmonium ($c\bar{c}$) + Bottomonium ($b\bar{b}$)

c	1.0 – 1.4 GeV
b	4.0 – 4.5 GeV

Heavy quarkonium

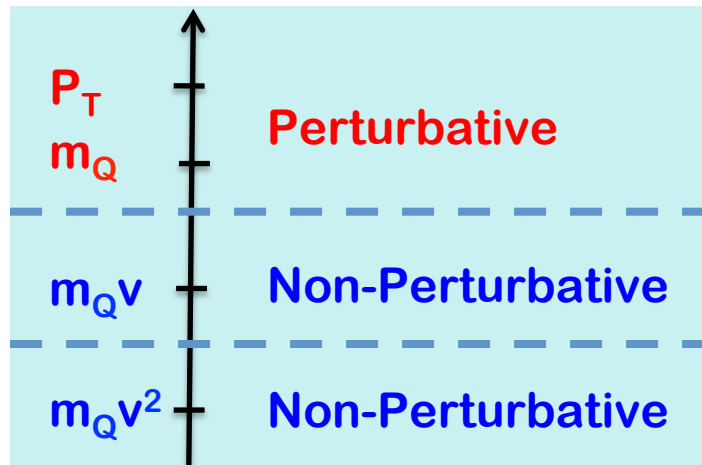
□ One of the simplest QCD bound states:

Localized color charges (heavy mass), non-relativistic relative motion

Charmonium: $v^2 \approx 0.3$

Bottomonium: $v^2 \approx 0.1$

□ Well-separated momentum scales – effective theory:



Hard — Production of $Q\bar{Q}$ [pQCD]

Soft — Relative Momentum [NRQCD]

← Λ_{QCD}

Ultrasoft — Binding Energy [pNRQCD]

□ Cross sections and observed mass scales:

$$\frac{d\sigma_{AB \rightarrow H(P)X}}{dy dP_T^2} \quad \sqrt{S}, \quad P_T, \quad M_H,$$

PQCD is “expected” to work for the production of heavy quarks

Difficulty: Emergence of a quarkonium from a heavy quark pair?

Double $c\bar{c}$ production in e^+e^- collisions

□ Inclusive production:

$$\sigma(e^+e^- \rightarrow J/\psi c\bar{c})$$

Belle: $(0.87_{-0.19}^{+0.21} \pm 0.17) \text{ pb}$

NRQCD: : 0.07 pb

Kiselev, et al 1994,
Cho, Leibovich, 1996
Yuan, Qiao, Chao, 1997

□ Ratio to light flavors:

$$\sigma(e^+e^- \rightarrow J/\psi c\bar{c}) / \sigma(e^+e^- \rightarrow J/\psi X)$$

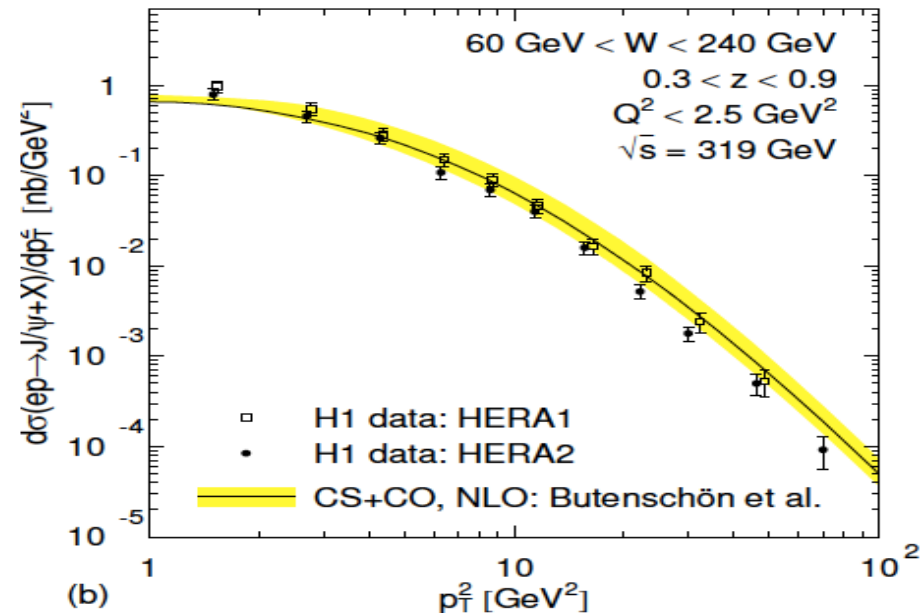
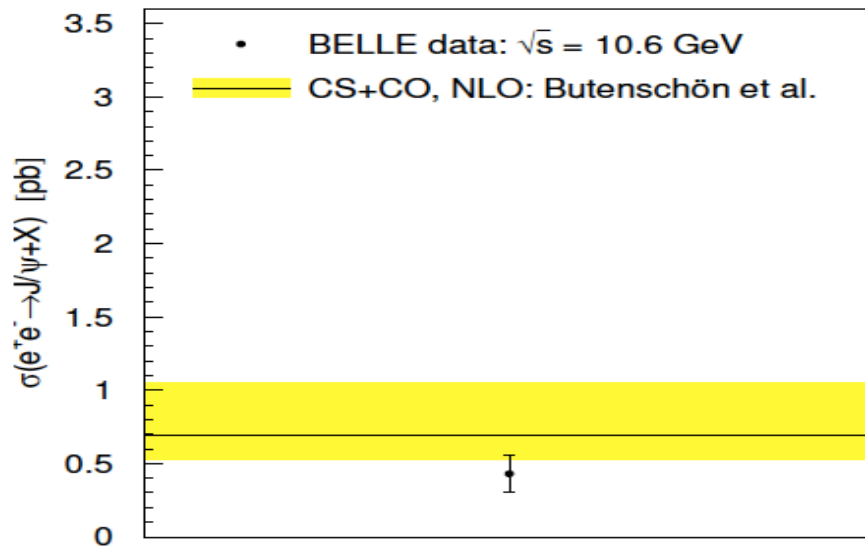
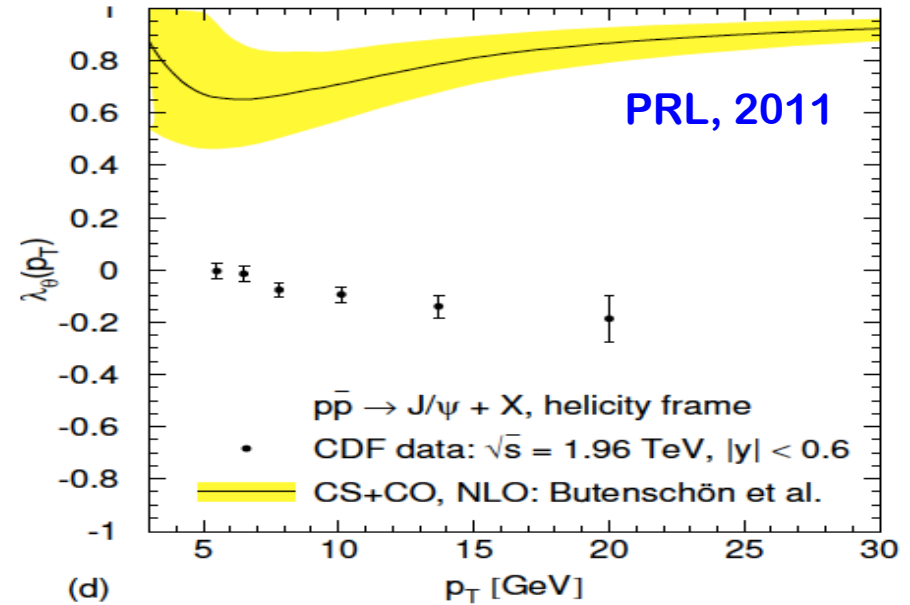
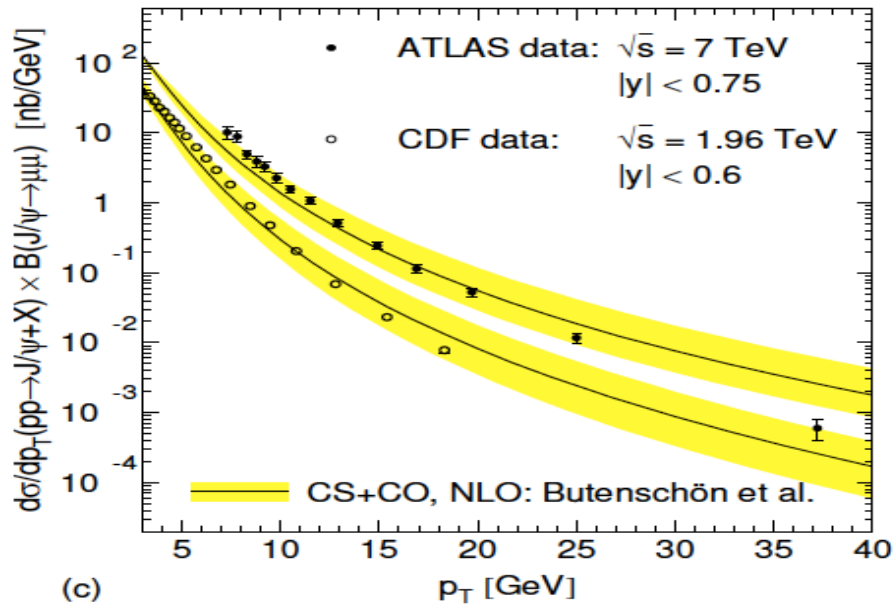
Belle: $0.59_{-0.13}^{+0.15} \pm 0.12$

Message:

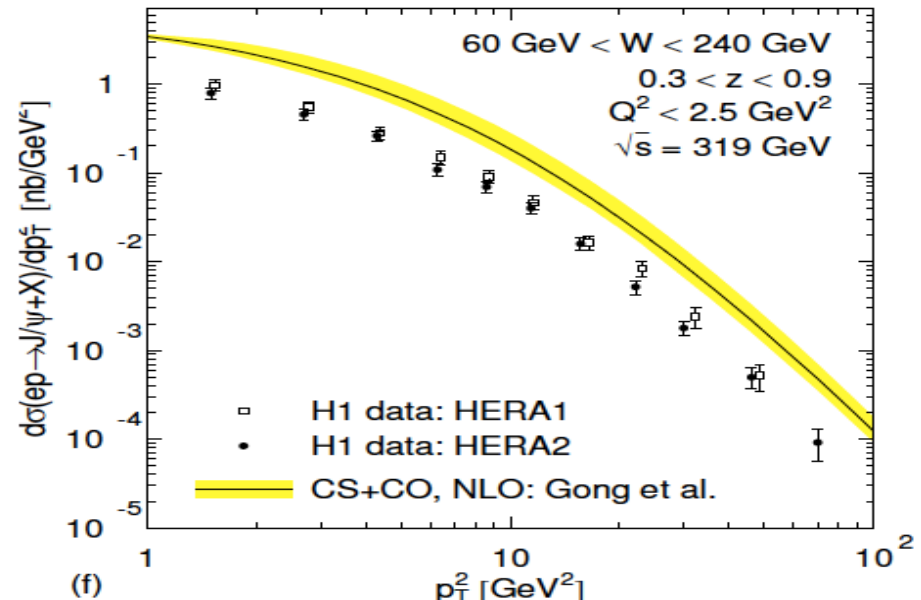
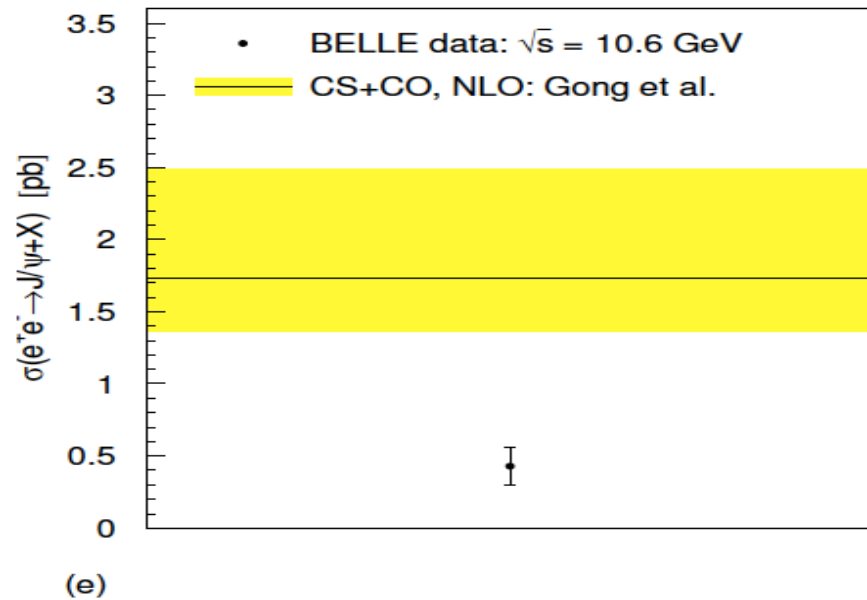
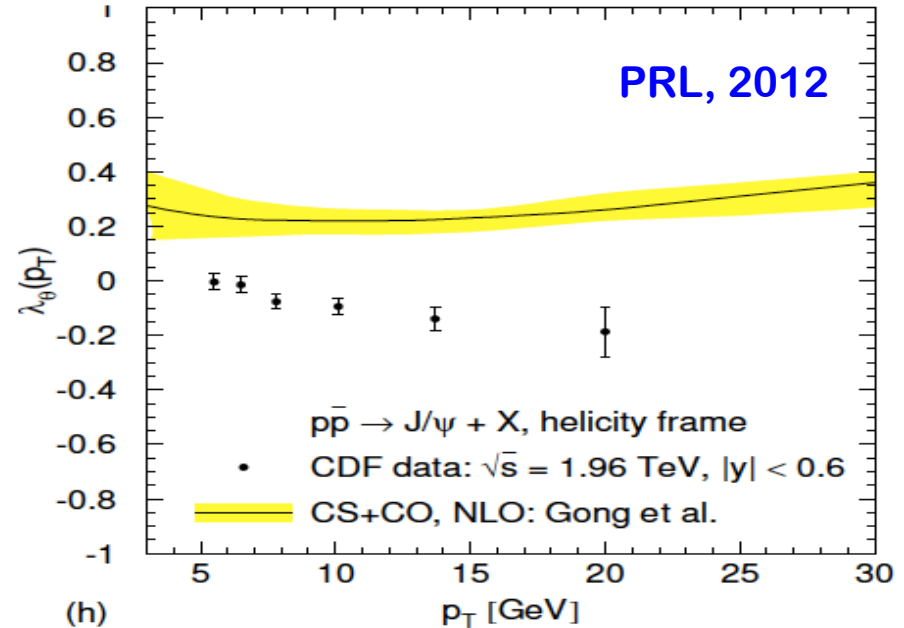
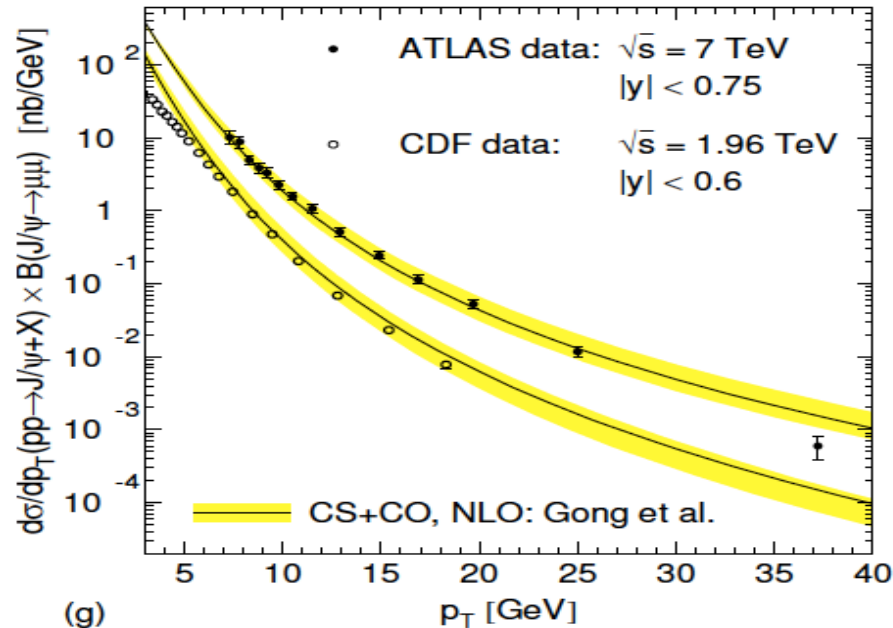
Production rate of $e^+e^- \rightarrow J/\psi c\bar{c}$ is larger than

all these channels: $e^+e^- \rightarrow J/\psi gg, e^+e^- \rightarrow J/\psi q\bar{q}, \dots$
combined ?

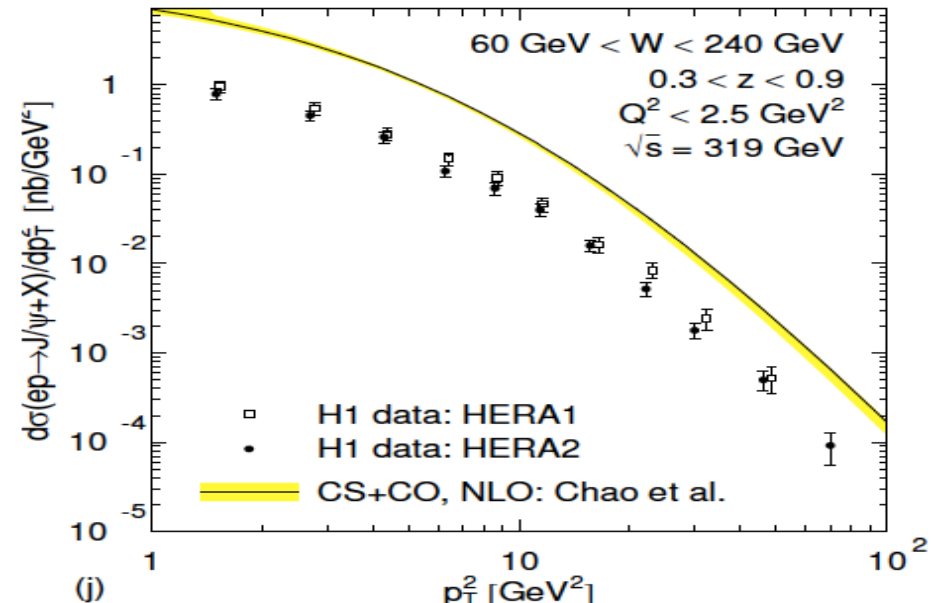
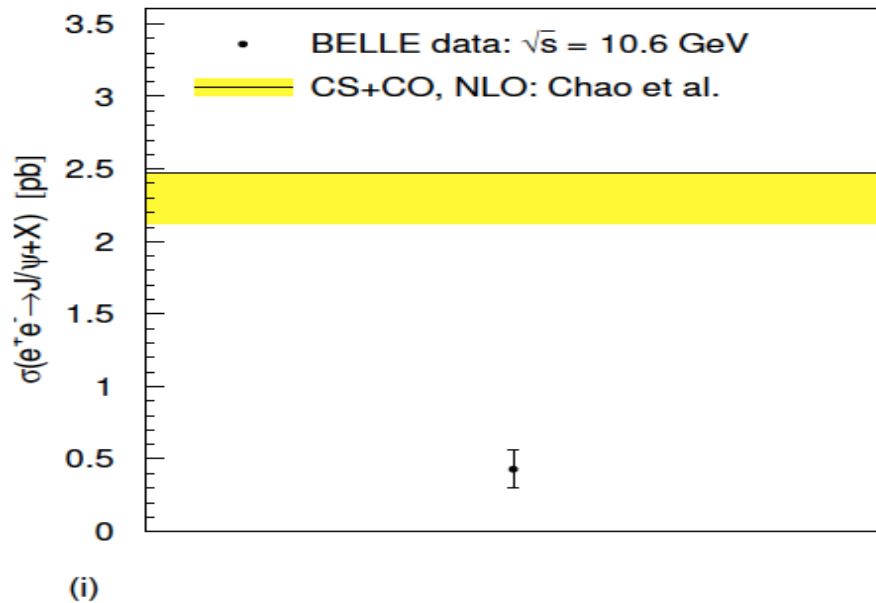
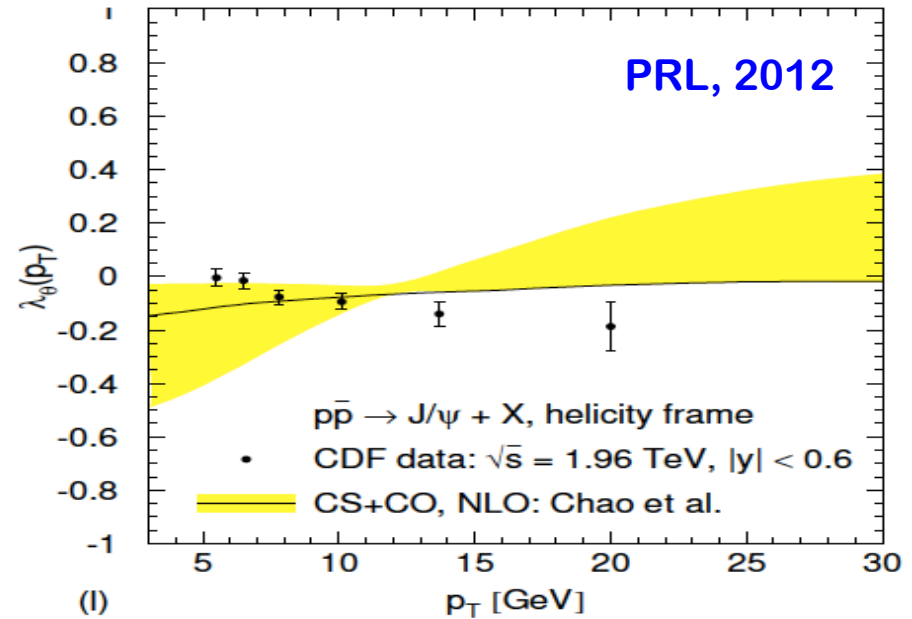
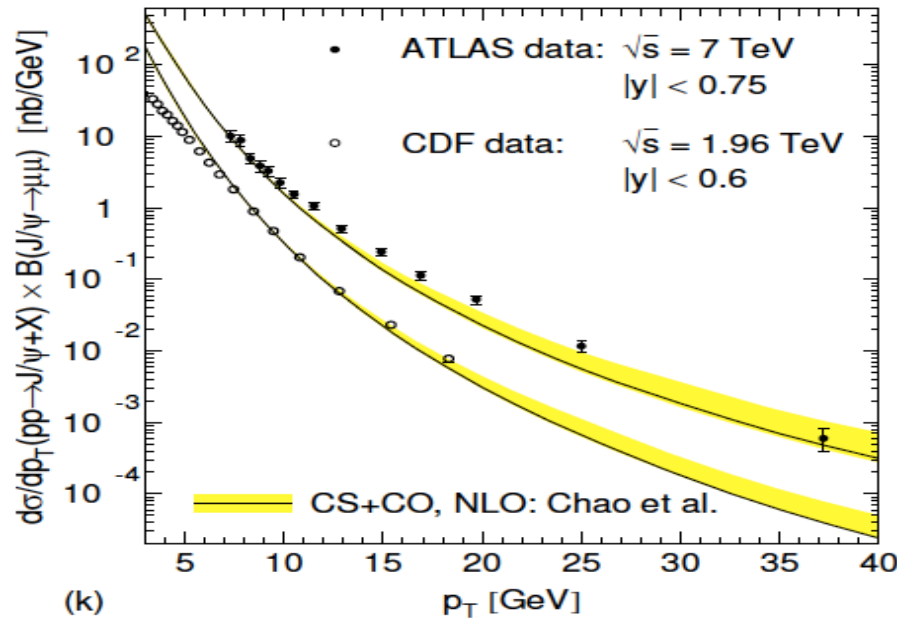
NLO theory fits – Butenschön et al.



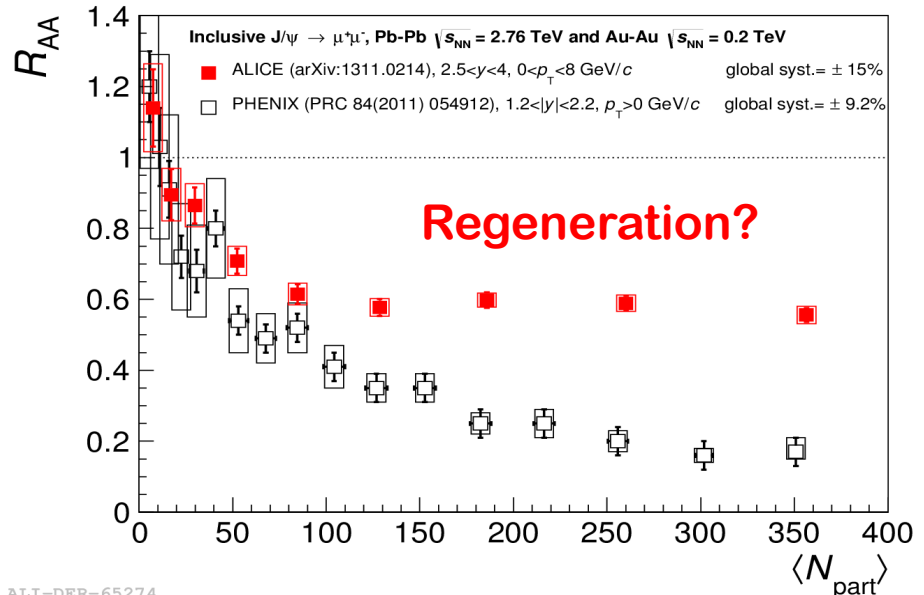
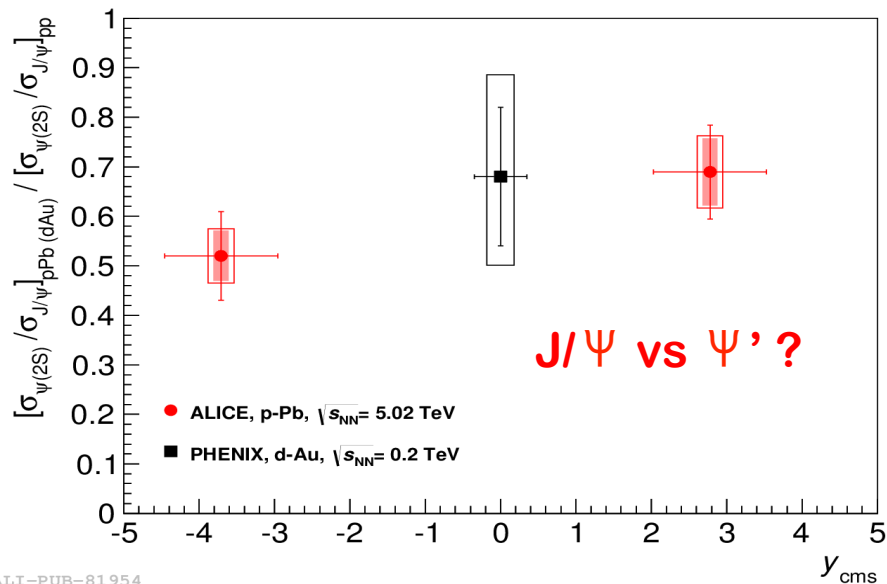
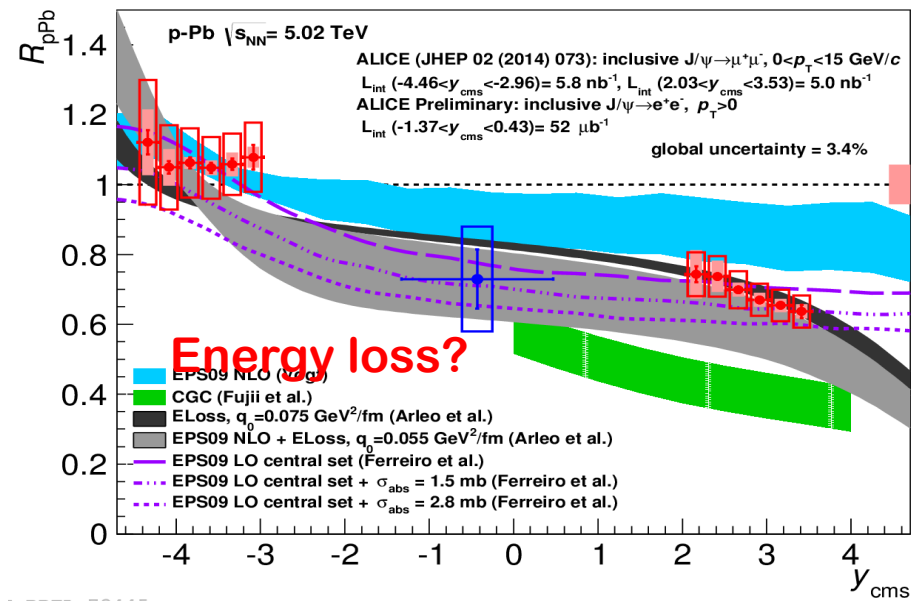
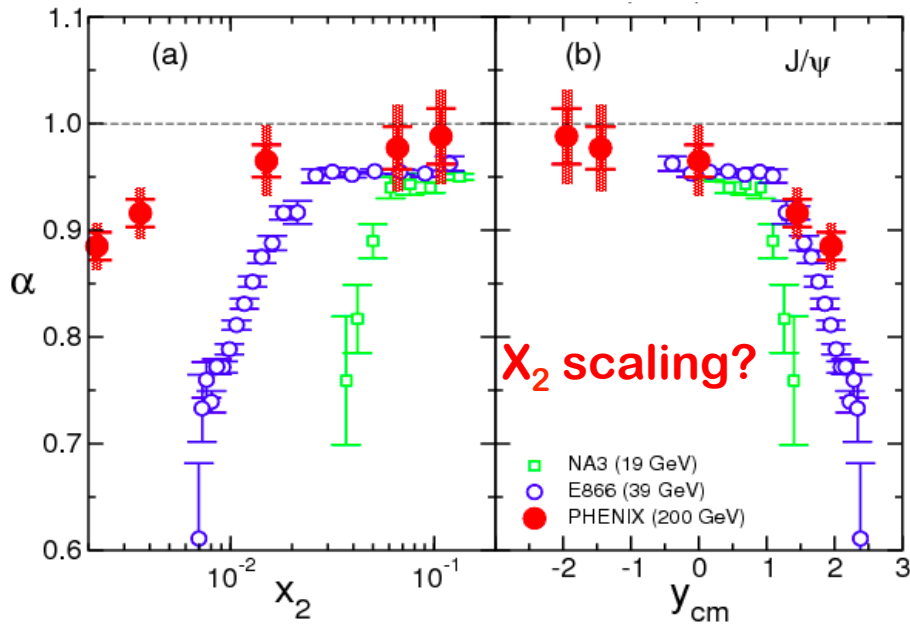
NLO theory fits – Gong et al.



NLO theory fits – Chao et al.



Production in medium, cold or hot?



Quarkonium 2017

The 12th International Workshop on Heavy Quarkonium



November 6-10, 2017, PKU, Beijing, China
Organized by the Quarkonium Working Group

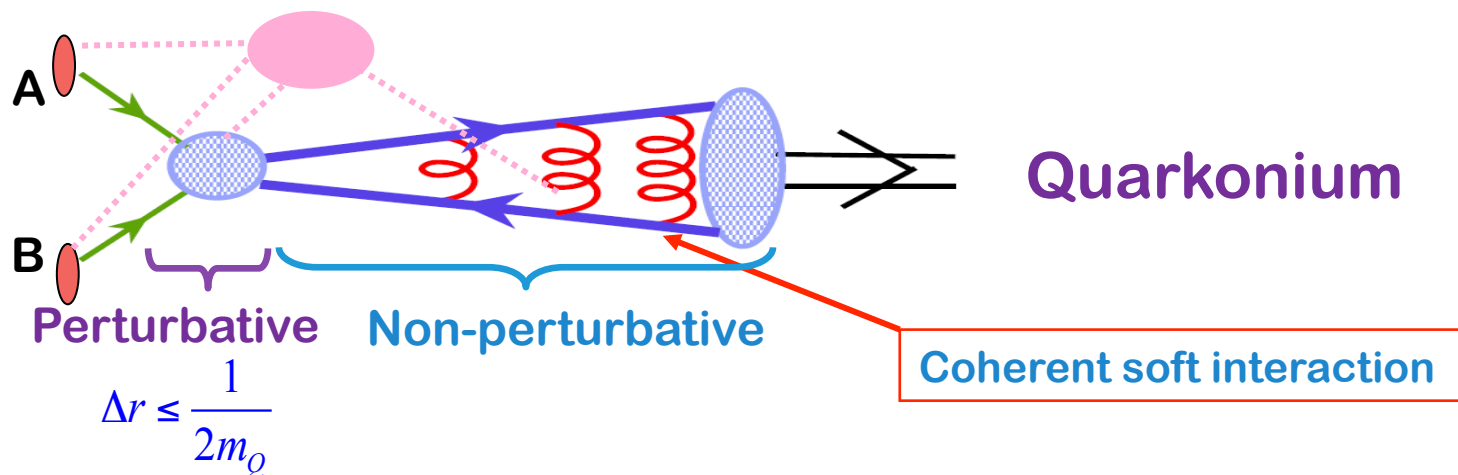
<http://itp.phy.pku.edu.cn/conference/qwg2017/>



Basic production mechanism

□ Factorization is likely to be valid for producing the pairs:

- ✧ Momentum exchange is much larger than $1/\text{fm}$
- ✧ Spectators from colliding beams are “frozen” during the hard collision



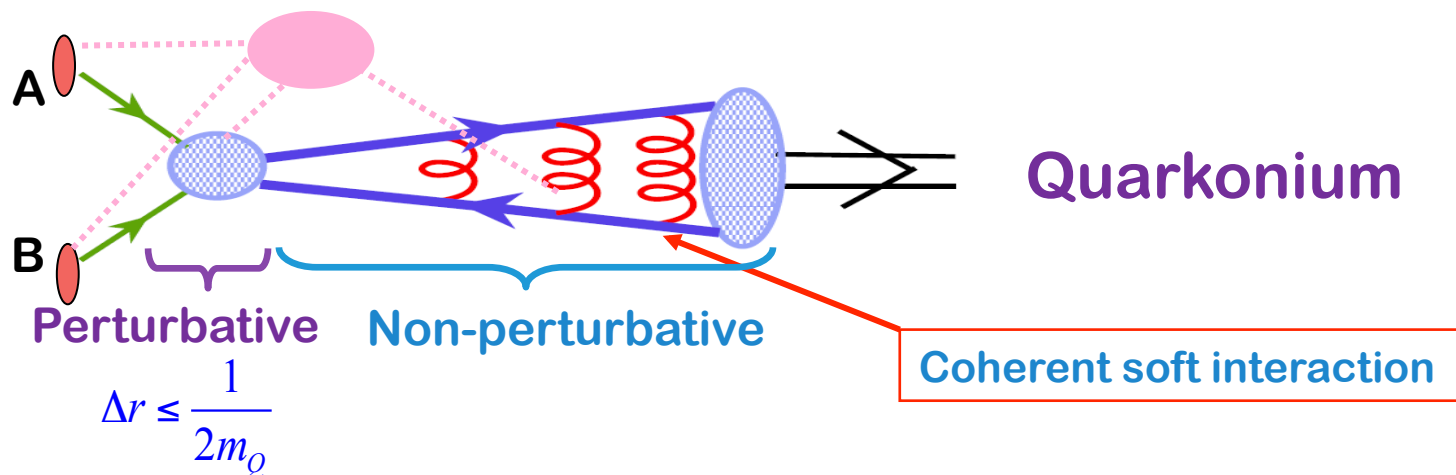
□ Approximation:

$$\begin{aligned}
 \sigma_{AB \rightarrow h} &\propto \left| \begin{array}{c} A \rightarrow \text{H} \rightarrow Q \rightarrow \text{h} \\ B \rightarrow \text{H} \rightarrow \bar{Q} \rightarrow \text{h} \end{array} \right|^2 \\
 &\propto \left| \begin{array}{c} A \rightarrow \text{H} \rightarrow Q \\ B \rightarrow \text{H} \rightarrow \bar{Q} \end{array} \right|^2 \otimes \left| \begin{array}{c} Q \rightarrow \text{h} \\ \bar{Q} \rightarrow \text{h} \end{array} \right|^2 + \frac{\langle M_{\text{H}}^2 - 4m_Q^2 \rangle}{M_{\text{H}}^2} \\
 \Rightarrow \sigma_{AB \rightarrow h} &= \int dq^2 \hat{\sigma}_{AB \rightarrow [Q\bar{Q}]}(m_Q^2, q^2) F_{[Q\bar{Q}] \rightarrow h}(q^2) + \dots
 \end{aligned}$$

Basic production mechanism

□ Factorization is likely to be valid for producing the pairs:

- ✧ Momentum exchange is much larger than 1/fm
- ✧ Spectators from colliding beams are “frozen” during the hard collision



□ Naïve factorization: on-shell pair + hadronization

$$\sigma_{AB \rightarrow J/\psi} = \sum_{[Q\bar{Q}(n)]} \int d\Gamma_{[Q\bar{Q}]} \hat{\sigma}_{AB \rightarrow [Q\bar{Q}(n)]}(p_Q, p_{\bar{Q}}) F_{[Q\bar{Q}(n)] \rightarrow J/\psi}(p_Q, p_{\bar{Q}}, P_{J/\psi})$$

Models & Debates

⇔ Different assumptions/treatments on $F_{[Q\bar{Q}(n)] \rightarrow J/\psi}(p_Q, p_{\bar{Q}}, P_{J/\psi})$
how the heavy quark pair becomes a quarkonium?

A long history for the production

□ Color singlet model: 1975 –

Einhorn, Ellis (1975),
Chang (1980),
Berger and Jones (1981), ...

Only the pair with right quantum numbers

Effectively No free parameter!

□ Color evaporation model: 1977 –

Fritsch (1977), Halzen (1977), ...

All pairs with mass less than open flavor heavy meson threshold

One parameter per quarkonium state

□ NRQCD model: 1986 –

Caswell, Lapage (1986)
Bodwin, Braaten, Lepage (1995)
QWG review: 2004, 2010

All pairs with various probabilities – NRQCD matrix elements

Infinite parameters – organized in powers of v and α_s

□ QCD factorization approach: 2005 –

Nayak, Qiu, Sterman (2005), ...
Kang, Qiu, Sterman (2010), ...

$P_T \gg M_H$: M_H/P_T power expansion + α_s – expansion

Unknown, but universal, fragmentation functions – evolution

□ Soft-Collinear Effective Theory + NRQCD: 2012 –

Fleming, Leibovich, Mehen, ...

NRQCD – most successful so far

Bodwin, Braaten, Lepage, PRD, 1995

NRQCD factorization:

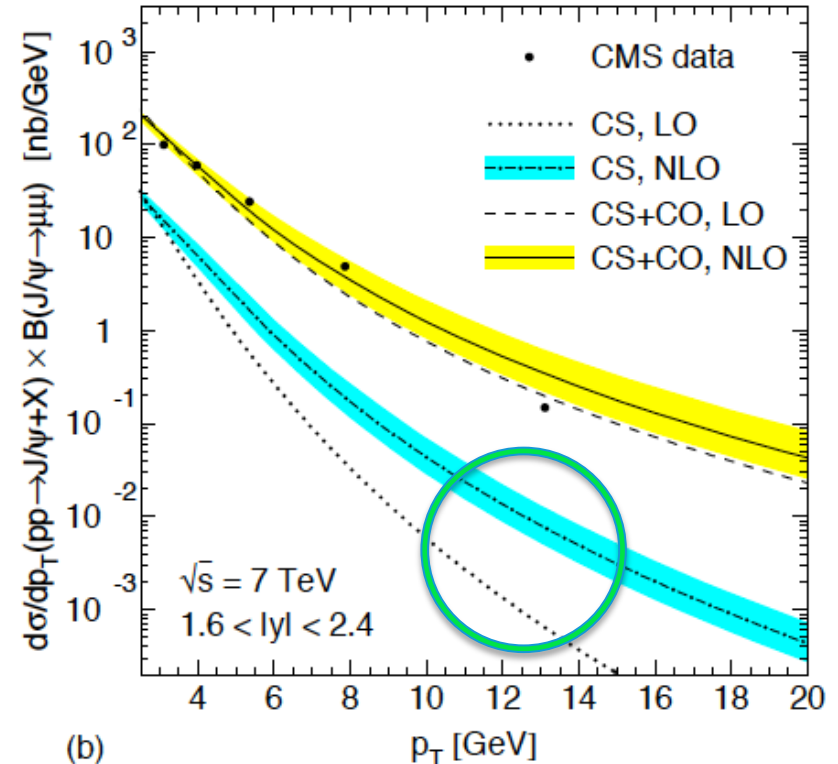
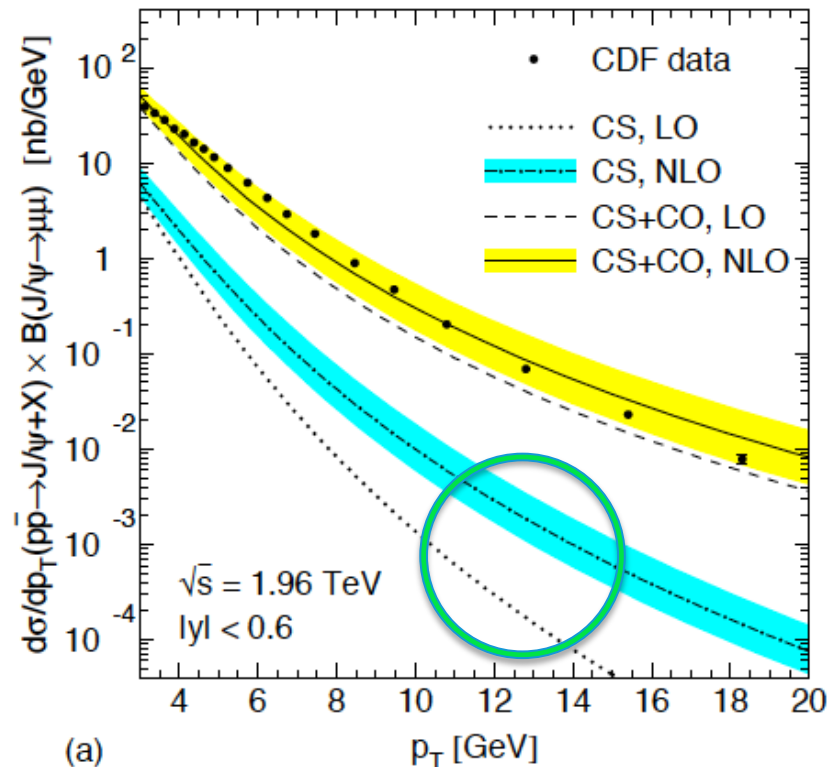
$$d\sigma_{A+B \rightarrow H+X} = \sum_n d\sigma_{A+B \rightarrow Q\bar{Q}(n)+X} \langle \mathcal{O}^H(n) \rangle$$

✧ 4 leading channels in v

$$^3S_1^{[1]}, \quad ^1S_0^{[8]}, \quad ^3S_1^{[8]}, \quad ^3P_J^{[8]}$$

Phenomenology:

✧ Full NLO in α_s



Fine details – shape – high at large p_T ?

NRQCD model

□ **NRQCD Lagrangian:** $\mathcal{L}_{\text{NRQCD}} = \mathcal{L}_{\text{light}} + \mathcal{L}_{\text{heavy}} + \delta\mathcal{L}$

$\mathcal{L}_{\text{light}} = -\frac{1}{2}\text{tr } G_{\mu\nu}G^{\mu\nu} + \sum_{n_F=1}^{3 \text{ or } 4} \bar{q} i\not{D}q$ Caswell, Lepage, Phys. Lett. B, 1986
Bodwin, Braaten, Lepage, PRD, 1995

$\mathcal{L}_{\text{heavy}} = \psi^\dagger \left(iD_t + \frac{\mathbf{D}^2}{2M} \right) \psi + \chi^\dagger \left(iD_t - \frac{\mathbf{D}^2}{2M} \right) \chi$ Pauli spinor for antiquark

$\delta\mathcal{L}_{\text{bilinear}} = \frac{c_1}{8M^3} \left(\psi^\dagger (\mathbf{D}^2)^2 \psi - \chi^\dagger (\mathbf{D}^2)^2 \chi \right)$ Pauli spinor for heavy quark

$+ \frac{c_2}{8M^2} \left(\psi^\dagger (\mathbf{D} \cdot g\mathbf{E} - g\mathbf{E} \cdot \mathbf{D}) \psi + \chi^\dagger (\mathbf{D} \cdot g\mathbf{E} - g\mathbf{E} \cdot \mathbf{D}) \chi \right)$

$+ \frac{c_3}{8M^2} \left(\psi^\dagger (i\mathbf{D} \times g\mathbf{E} - g\mathbf{E} \times i\mathbf{D}) \cdot \boldsymbol{\sigma} \psi + \chi^\dagger (i\mathbf{D} \times g\mathbf{E} - g\mathbf{E} \times i\mathbf{D}) \cdot \boldsymbol{\sigma} \chi \right)$

$+ \frac{c_4}{2M} \left(\psi^\dagger (g\mathbf{B} \cdot \boldsymbol{\sigma}) \psi - \chi^\dagger (g\mathbf{B} \cdot \boldsymbol{\sigma}) \chi \right),$

□ Limitation:

Powerful for a process with available kinetic energy: $Mv^2 \ll Mc^2$

✧ Formalism is ideal for heavy quarkonium decay

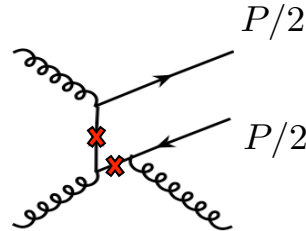
✧ Additional complications for production with $s \gg (2M)^2$

Why high orders in CSM are so large?

Kang, Qiu and Sterman, 2011

- LO in α_s but higher power in $1/p_T$:

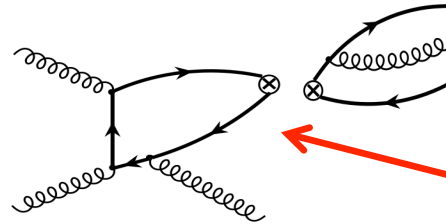
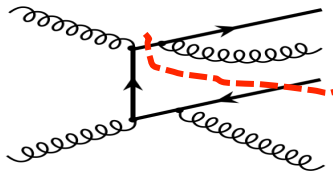
LO in α_s :



$$\hat{\sigma}^{\text{LO}} \propto \frac{\alpha_s^3(p_T)}{p_T^8}$$

CSM and NRQCD
spin-1 projection
NNLP in $1/p_T$!

- NLO in α_s but lower power in $1/p_T$:

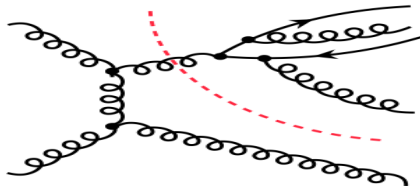


Relativistic
projection to
all
“spin states”

$$\hat{\sigma}^{\text{NLO}} \rightarrow \frac{\alpha_s^3(p_T)}{p_T^6} \otimes \alpha_s(\mu) \log(\mu^2/\mu_0^2)$$

$$\mu_0 \gtrsim 2m_Q$$

- NNLO in α_s but leading power in $1/p_T$:



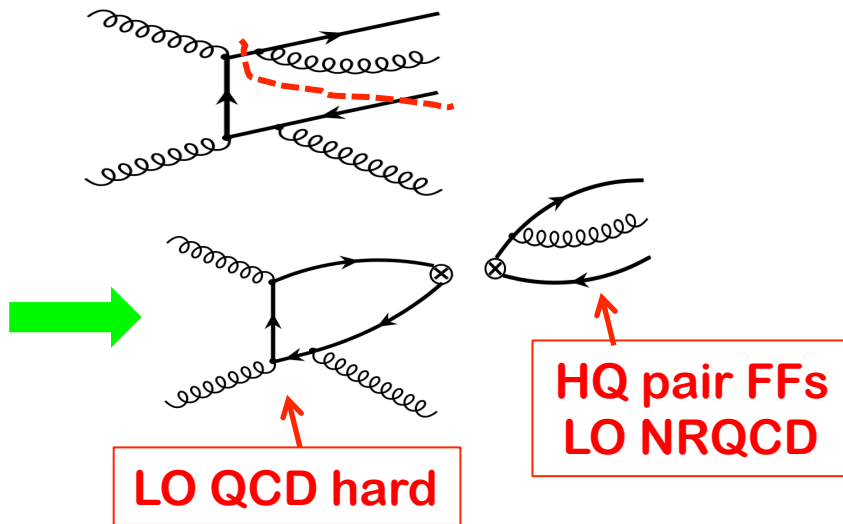
$$\hat{\sigma}^{\text{NNLP}} \rightarrow \frac{\alpha_s^2(p_T)}{p_T^4} \otimes \alpha_s^3(\mu) \log^m(\mu^2/\mu_0^2)$$

Leading order in α_s -expansion $\neq$ leading power in $1/p_T$ -expansion!

QCD factorization + NRQCD factorization

Kang, Qiu and Sterman, 2011

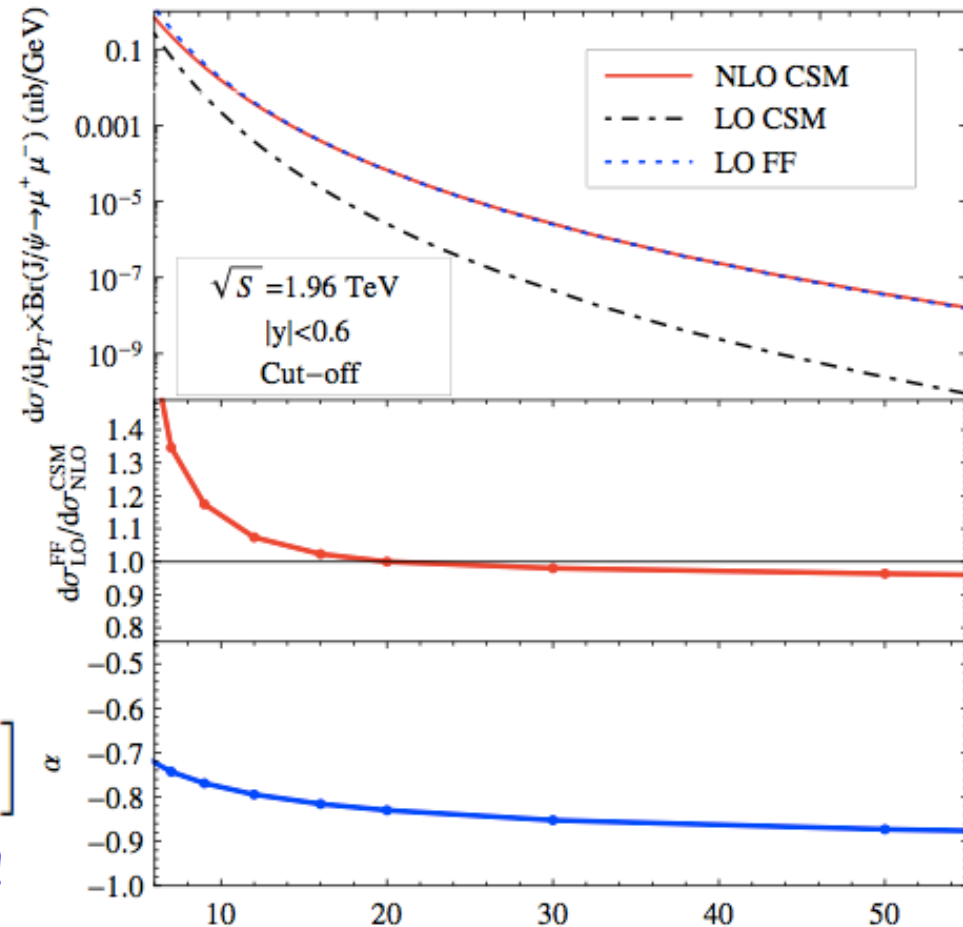
□ Color singlet as an example:



$$\sigma_{\text{NRQCD}}^{(\text{NLO})} \propto \left[d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(v8)]}^{A(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(v8)] \rightarrow J/\psi}^{(\text{LO})} + d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(a8)]}^{S(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(a8)] \rightarrow J/\psi}^{(\text{LO})} \right]$$

Reproduce NLO CSM for $p_T > 10$ GeV!

Cross section + polarization

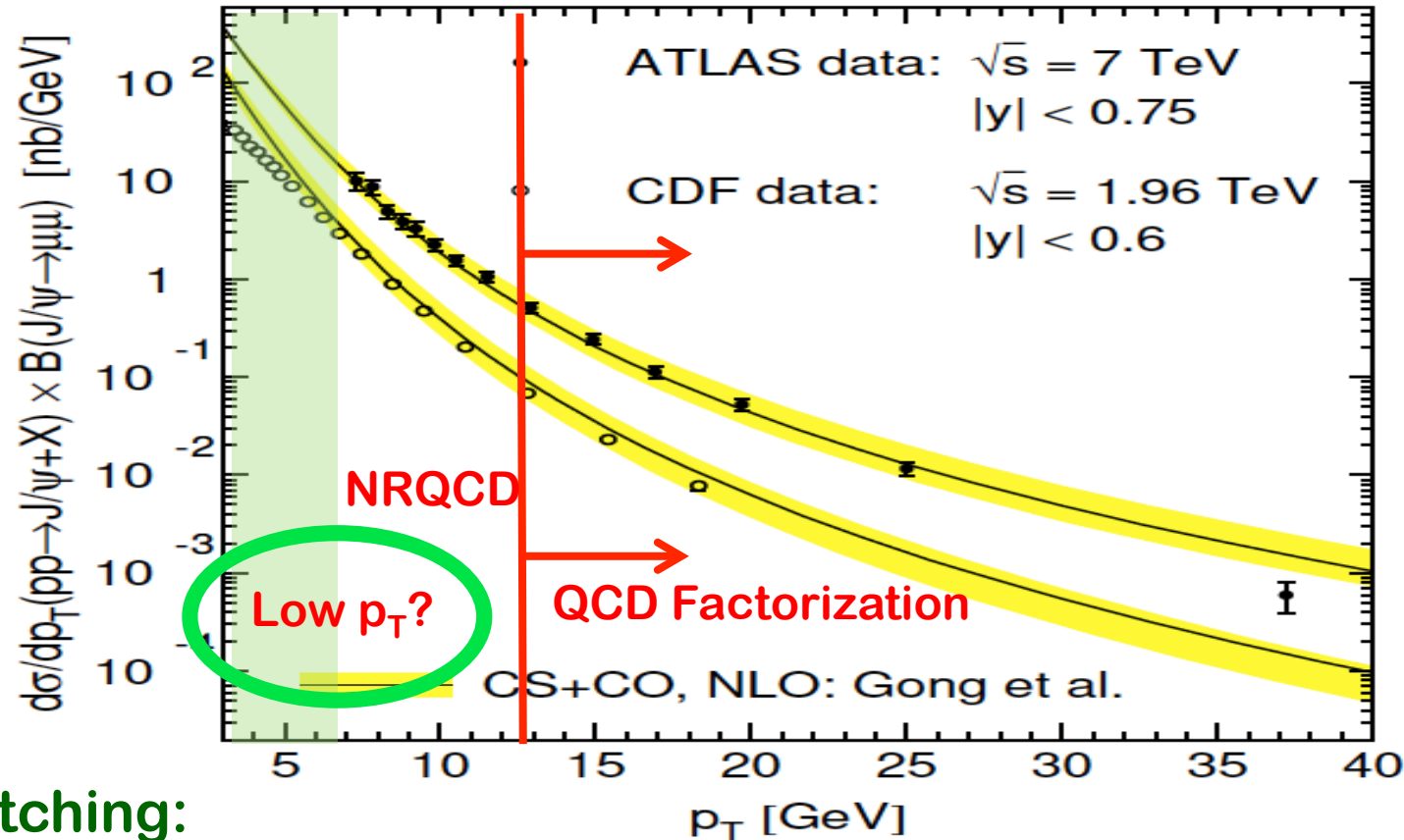


*Different kinematics, different approximation,
Dominance of different production channels!*

Matching between different approaches

□ Expectation:

Kang, Ma, Qiu and Sterman, 2014



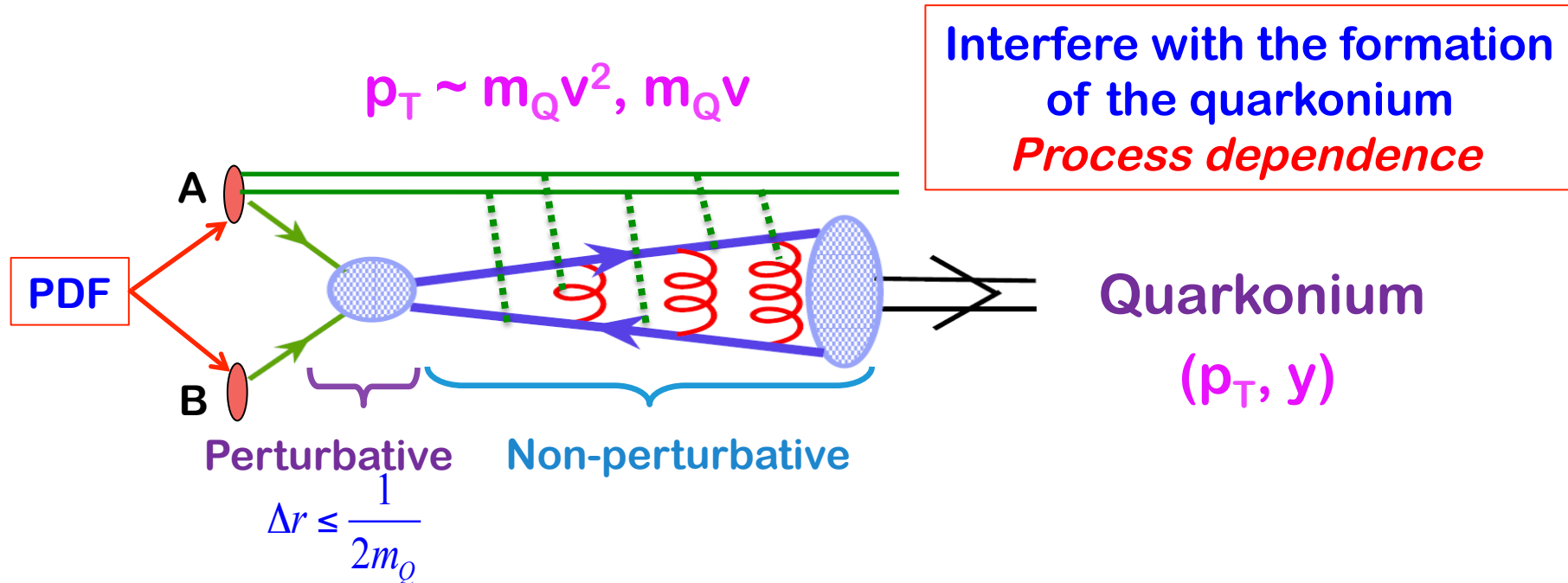
□ Matching:

$$E_P \frac{d\sigma_{A+B \rightarrow H+X}}{d^3P}(P, m_Q) \equiv E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{QCD}}}{d^3P}(P, m_Q = 0) \\
+ E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{NRQCD}}}{d^3P}(P, m_Q \neq 0) - E_P \frac{d\sigma_{A+B \rightarrow H+X}^{\text{QCD-Asym}}}{d^3P}(P, m_Q = 0)$$

Mass effect + expanded P_T region ($P_T \gtrsim m_Q$)

Production at low p_T ($< M_Q$)

- Spectator interaction – always there:



- The Challenge:

Break factorization – Process dependence – Alter p_T distribution, ...

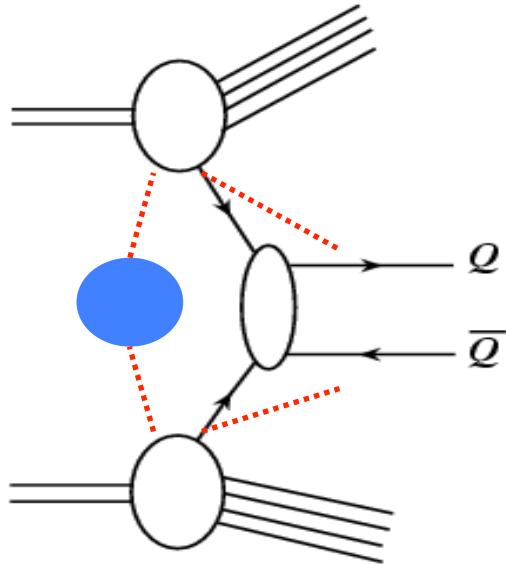
- Understand the factorization breaking:

If the breaking effect is controllable, we still have predictive power!

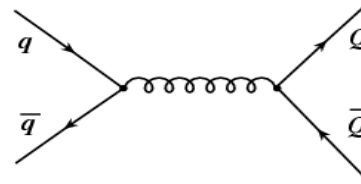
Even the Drell-Yan process is NOT fully factorizable!

Production at low p_T ($< M_Q$)

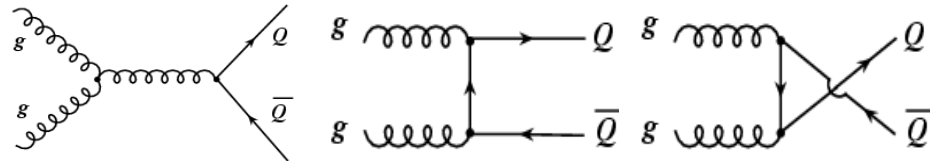
□ Gluon shower – Sudakov resummation dominated?



✧ Quark-antiquark channel:



✧ Gluon-gluon channel:



□ Assumption:

Leading double logarithms from the gluon shower are from initial-state active partons



Mimic the Drell-Yan type radiation pattern,
Resum the leading soft radiation into Sudakov form factor

Upsilon production at hadron colliders

□ CSS formalism (the b-space approach to low P_T region):

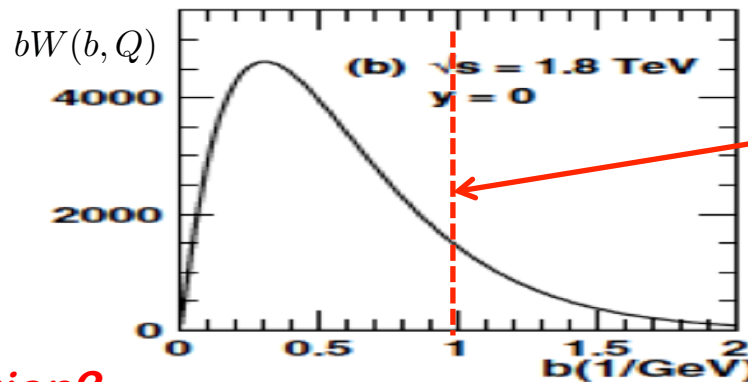
Use Drell-Yan as an example:

$$\begin{aligned} \frac{d\sigma_{AB}^{DY}}{dQ^2 dq_T^2}(Q, q_T, x_A, x_B) &= \hat{H}_{f\bar{f}}(Q) \otimes \Phi_{f/A}(x_A, k_{a\perp}) \otimes \Phi_{\bar{f}/B}(x_B, k_{b\perp}) \otimes \mathcal{S}(k_{s\perp}) + Y(Q, q_T) \\ &= \frac{1}{2\pi} \int_0^\infty db J_0(bq_T) b \widetilde{W}_{AB}(b, Q; x_A, x_B) + \left[\frac{d\sigma_{AB}^{(\text{Pert})}}{dQ^2 dq_T^2} - \frac{d\sigma_{AB}^{(\text{Asym})}}{dQ^2 dq_T^2} \right] \end{aligned}$$

The b-space distribution:

$$\widetilde{W}_{AB}^{\text{Pert}}(b, Q; x_A, x_B) = \hat{H}_{f\bar{f}}(Q) \left[\mathcal{C}_{f/a} \otimes \Phi_{a/A}(x_A, 1/b) \right] \otimes \left[\mathcal{C}_{\bar{f}/b} \otimes \Phi_{b/B}(x_B, 1/b) \right] e^{-\mathcal{S}(b, Q)}$$

Predictive power:
very sensitive to
the role of
non-perturbative
contribution!



**Ratio of areas
large b vs. small b**
Nonperturbative
Vs. perturbative

The role of large-b region?

Good predictive power (not sensitive to the large-b region):

if the area under the b-space distribution is dominated by small-b region!

Upsilon production at hadron colliders

□ Expect good predictive power:

Peak of p_T -distribution is around 4 GeV
 >> intrinsic p_T
 >> the Q_s at this energies

Shower is the dominant source to the observed large p_T

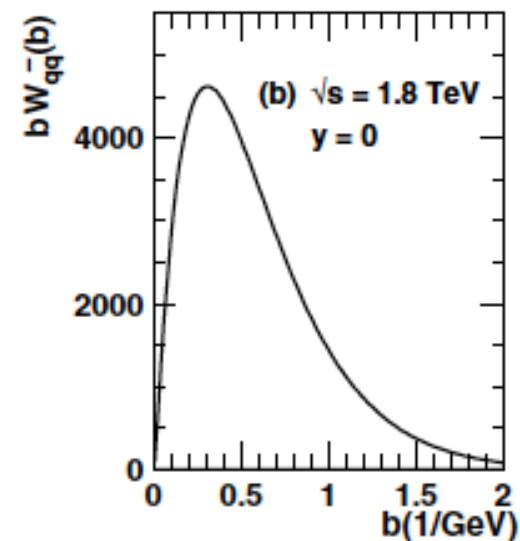
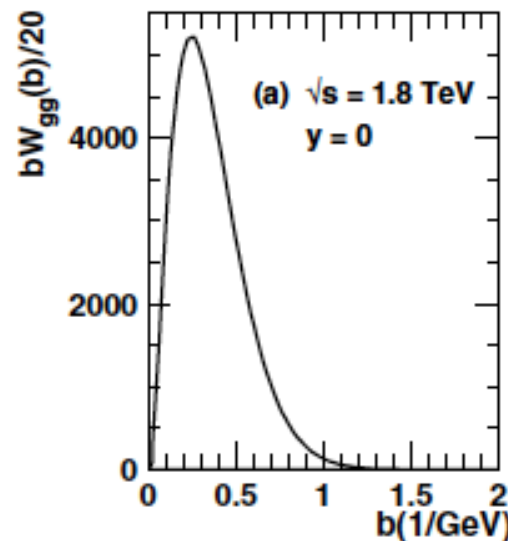
□ Matching procedure to large- b region:

$$W_{ij}(b, Q, x_A, x_B) = \begin{cases} W_{ij}^{\text{pert}}(b, Q, x_A, x_B) & b \leq b_{\text{max}} \\ W_{ij}^{\text{pert}}(b_{\text{max}}, Q, x_A, x_B) F_{ij}^{\text{NRP}}(b, Q; b_{\text{max}}) & b > b_{\text{max}} \end{cases}$$

$$F_{ij}^{\text{NRP}} = \exp \left\{ - \ln \left(\frac{Q^2 b_{\text{max}}^2}{c^2} \right) \{ g_1 [(b^2)^\alpha - (b_{\text{max}}^2)^\alpha] + g_2 (b^2 - b_{\text{max}}^2) \} - \bar{g}_2 (b^2 - b_{\text{max}}^2) \right\}$$

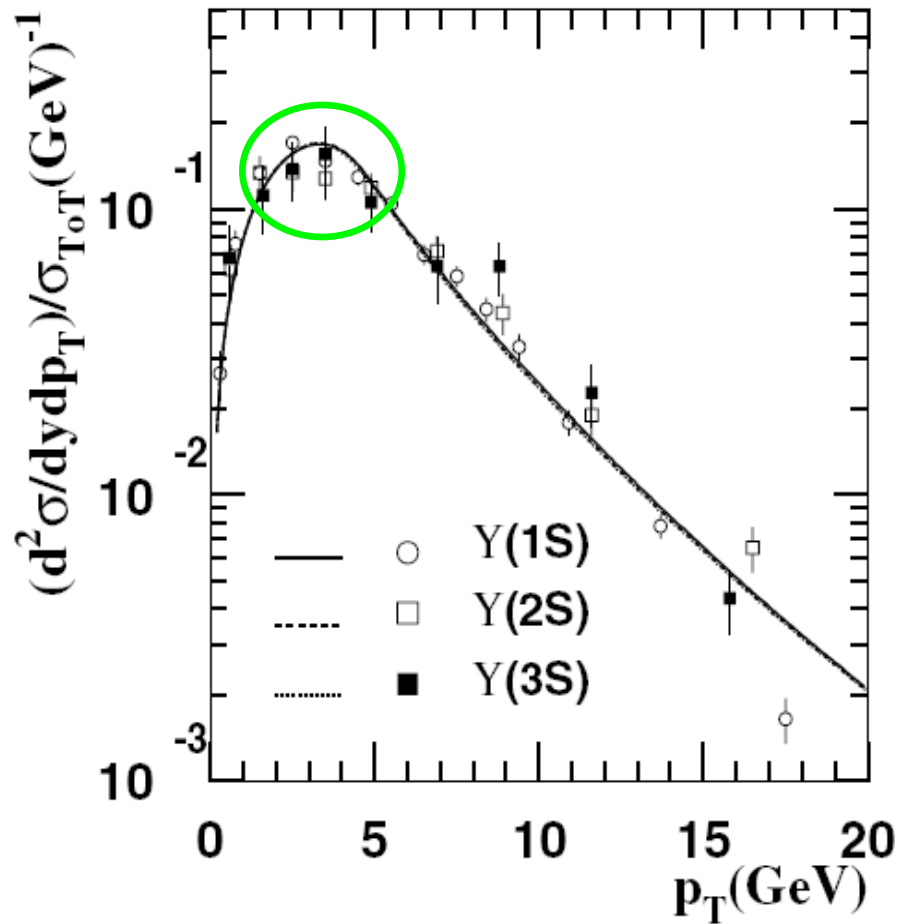
□ b -space distribution for Upsilon production at Tevatron energy:

All parameters fixed by the derivatives to be continuous at $b = b_{\text{max}}$.

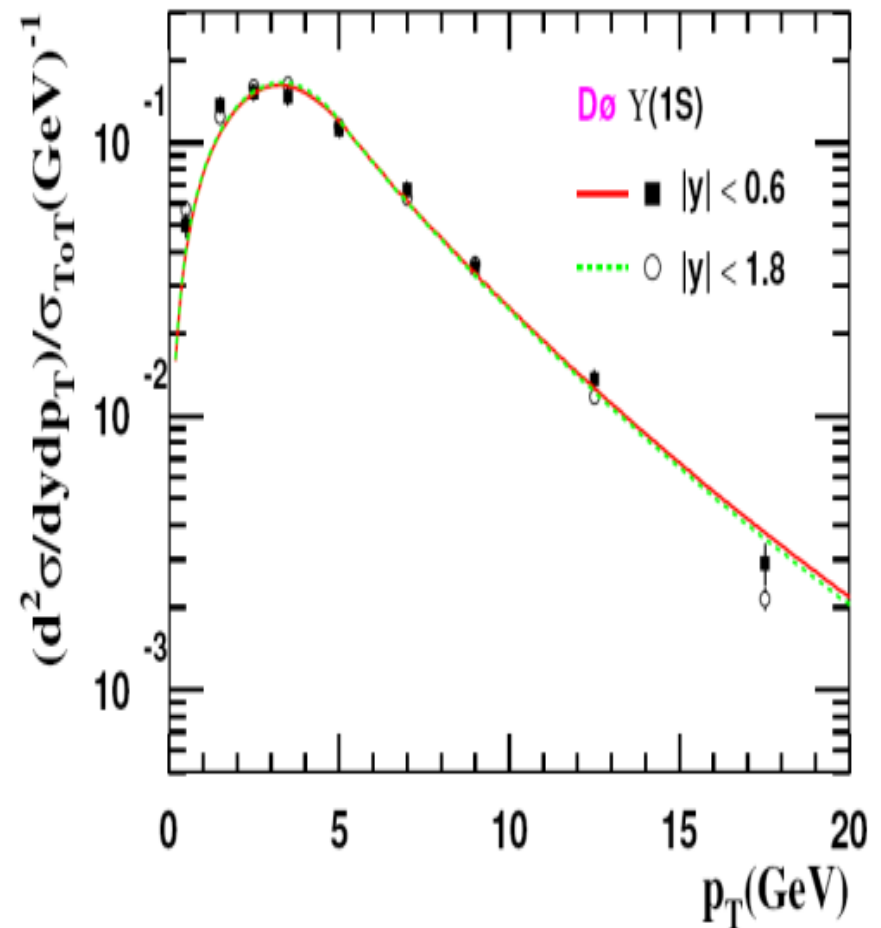


Upsilon production at hadron colliders

CDF Run-I



D0 Run-II



□ Strong gluon shower:

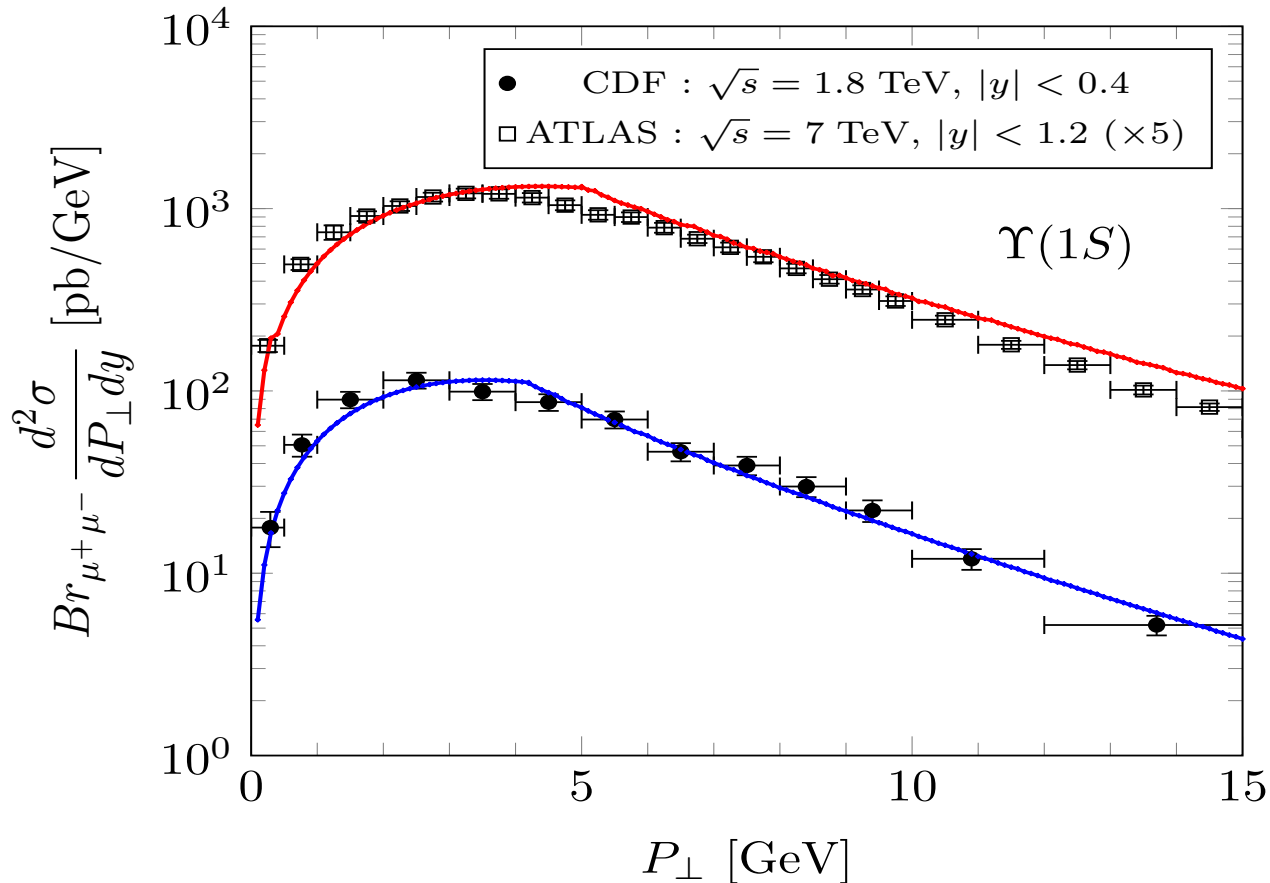
Berger, Qiu, Wang, 2005

Sufficiently large Q (Upsilon mass) + large shower phase space!

Predictive power – Upsilon

Qiu, Watanabe, 2017

□ Upsilon at the LHC:



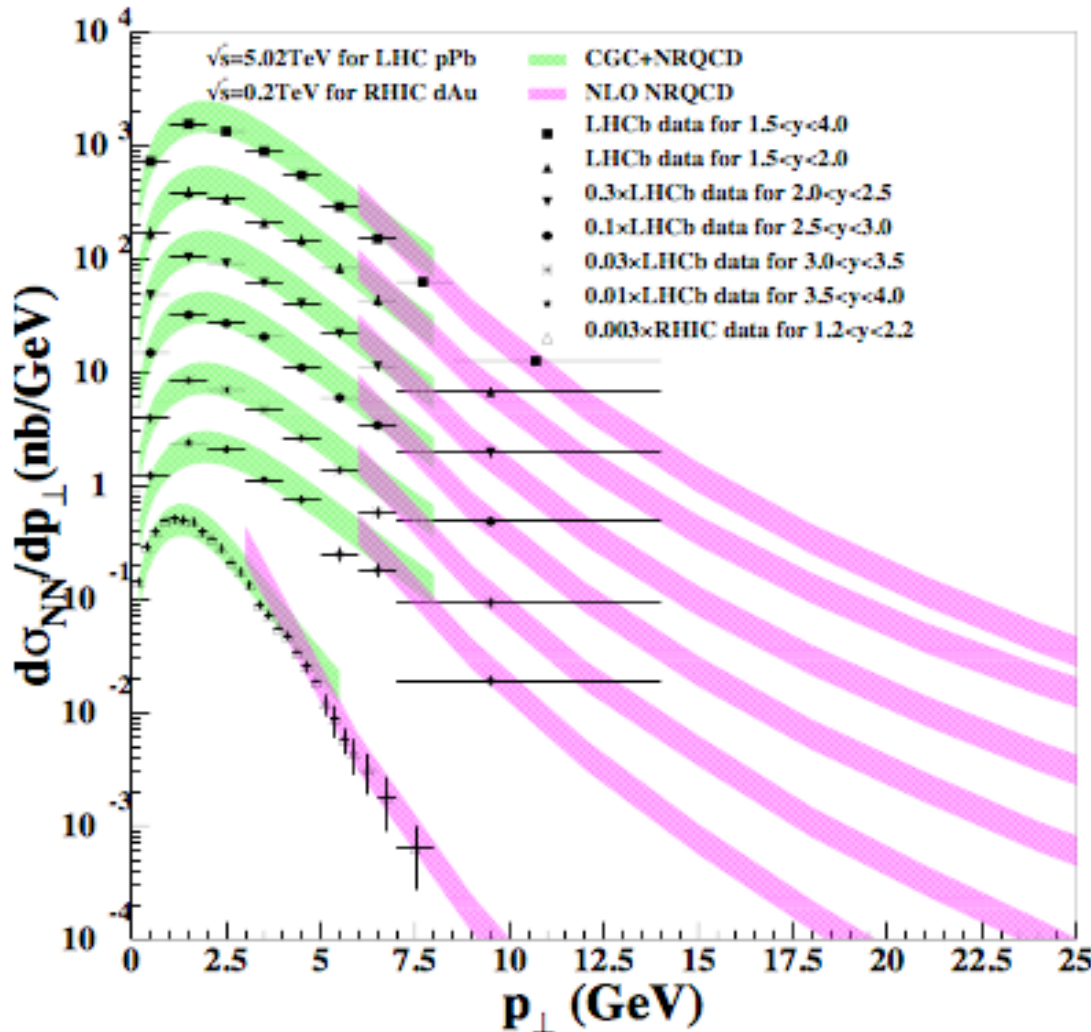
No adjustment on any parameter from Tevatron to the LHC!

BUT: this does not apply for J/ψ at low PT ,
logarithmic contribution from the shower is not strong enough!

Forward quarkonium production in p(d)+A

□ CGC for low p_T region:

Ma et al. Phys.Rev. D92 (2015) 071901



✧ Two free fitted parameters:
transverse overlap area,
saturation scale at initial
rapidities
seem reasonable

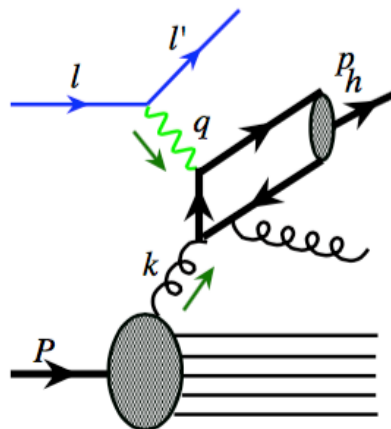
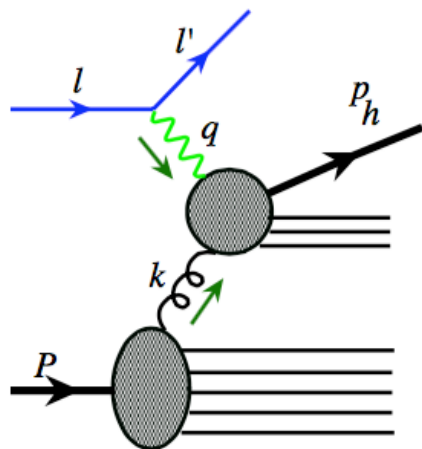
✧ Matching to NLO NRQCD
calculation,
modulo small
shadowing effect,
seem to be smooth

✧ Better agreement with
data than previous CGC
calculations

To understand what we could calculate, test, and learn at EIC energies!

Heavy quarkonium production at EIC

□ Semi-inclusive DIS:



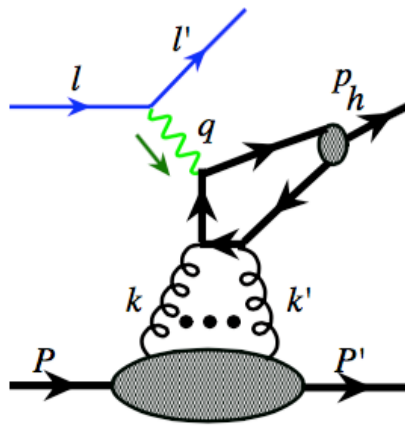
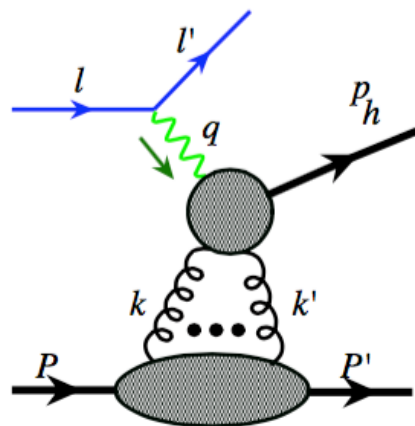
Low P_T : **Glue TMD ?**
CGC ?

Shower vs.
multiple scattering

$P_T \sim Q$: **Gluon PDF**

High P_T : **LP +NLP**
FFs

□ Exclusive / Gap:



$$\frac{d\sigma}{dt}(x_B, Q^2) \propto \text{GPDs}$$

Imaging gluon
density distribution

$$\frac{d\sigma}{dt}(x_B, Q^2)$$

Near threshold

$\propto$ Trace Anomaly?

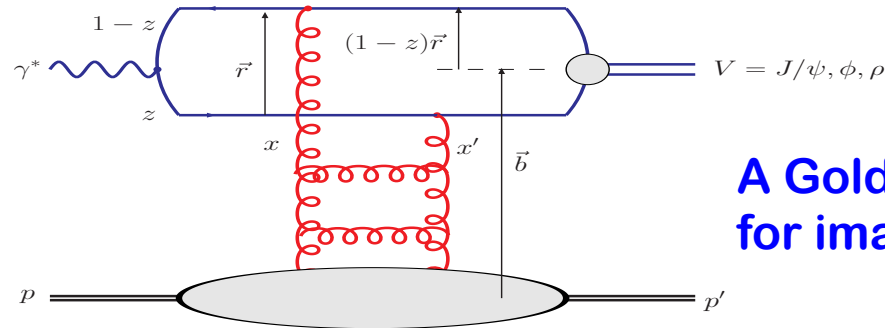
On-going effort, ...

One facility covers all issues of quarkonium production!

Critical role of J/ψ production at EIC

EIC WP, 1212.1701

❑ Exclusive:



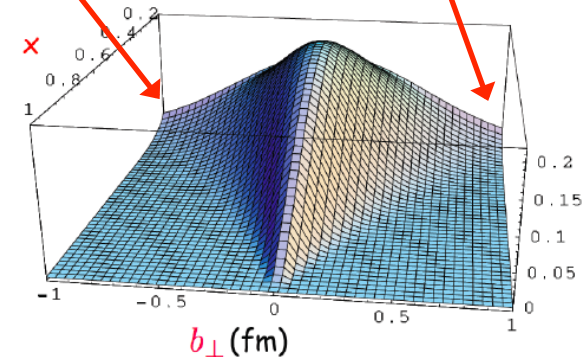
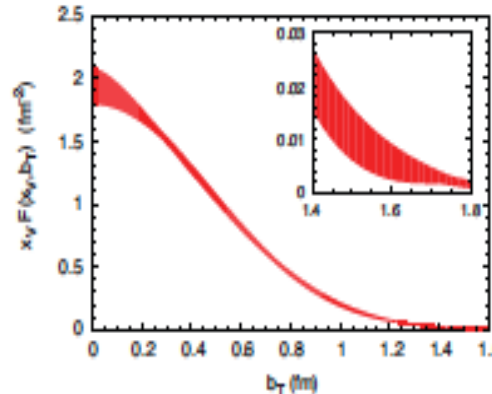
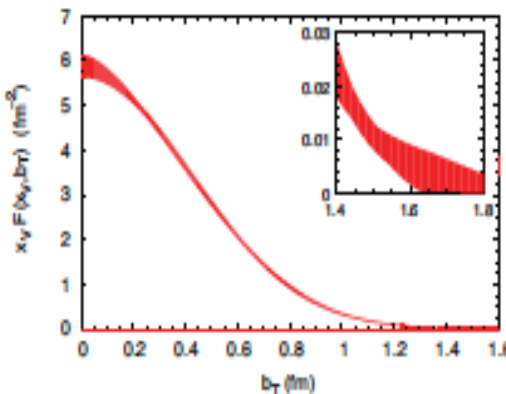
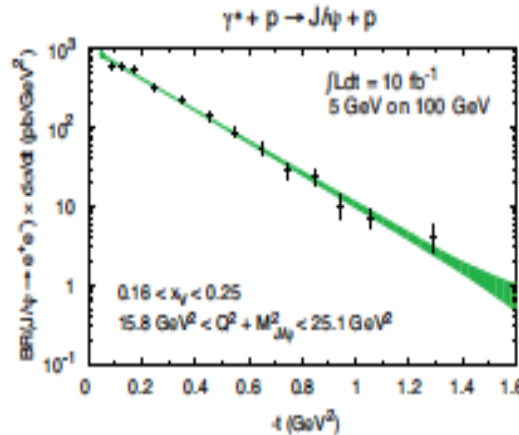
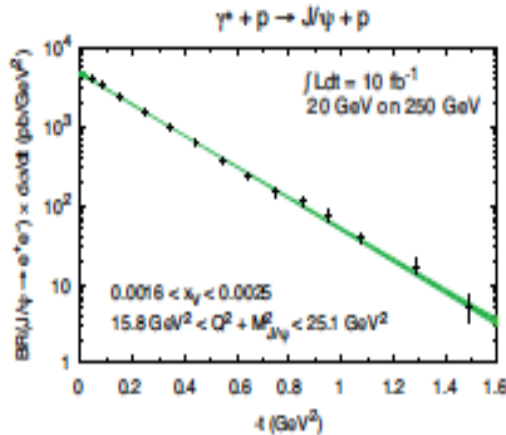
A Golden process
for imaging gluon

Allow us to ask “new”
fundamental questions:

Color confining radius?

How far does glue
density spread?

How fast does
glue density fall?

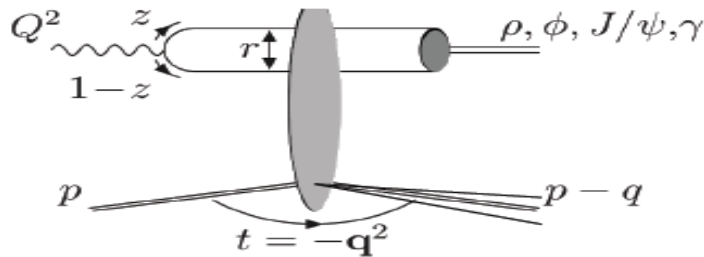


Can A be a bigger P at small-x?

Diffractive production in e+A at EIC

□ Diffractive vector meson (Φ , J/ψ , ..) production:

EIC WP, 1212.1701

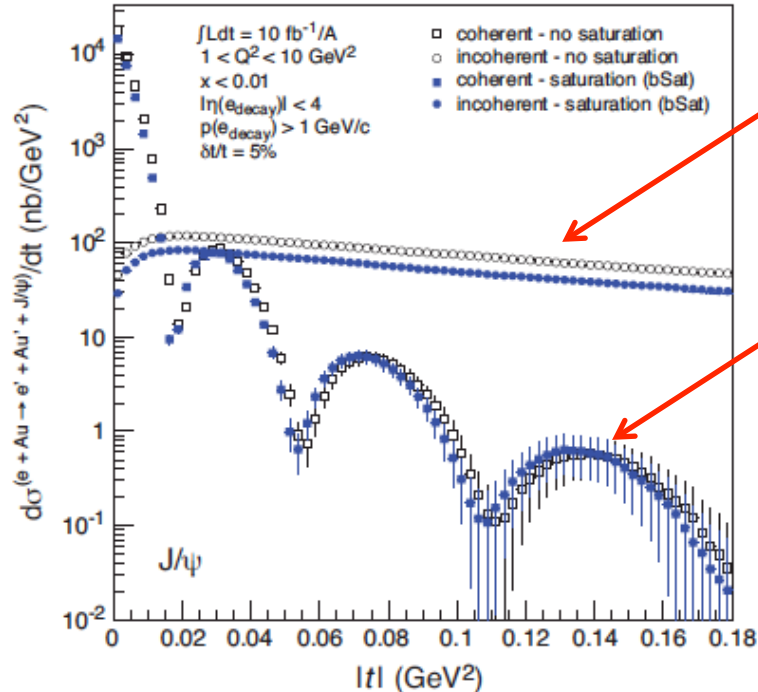
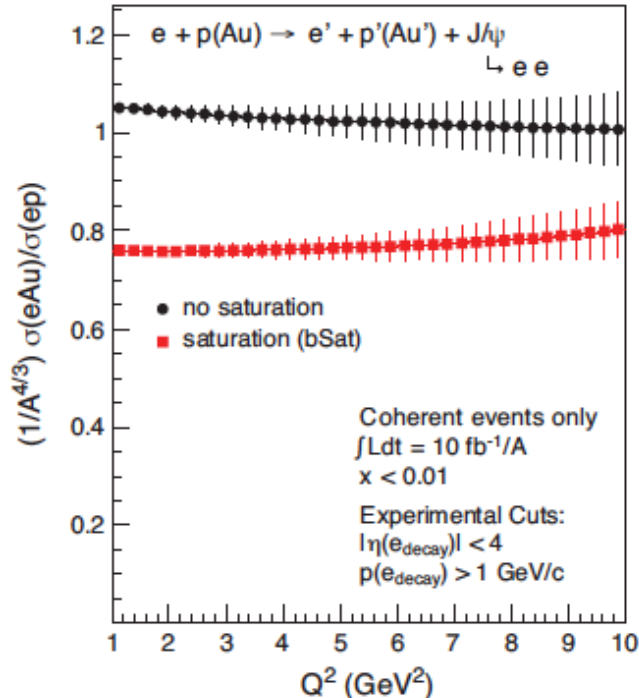


$$\frac{d\sigma}{dx_B dQ^2 dt}$$

Fourier transform
of the t -dependence

- as a function of t

□ J/ψ -production – probe for saturation and nuclear imaging:



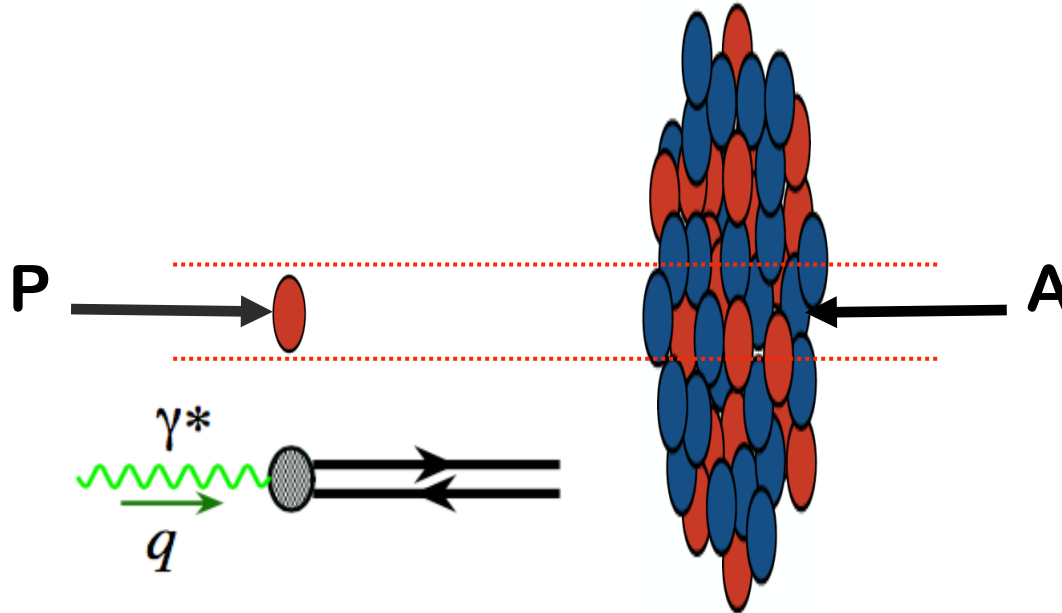
✧ Incoherent:
Nucleus
breaks up

✧ Coherent:
Nucleus
stays intact

Need EIC's
Energy &
Luminosity
to do this!

What have we learned from p+A collisions?

□ Proton (deuteron) – Nucleus Collisions:

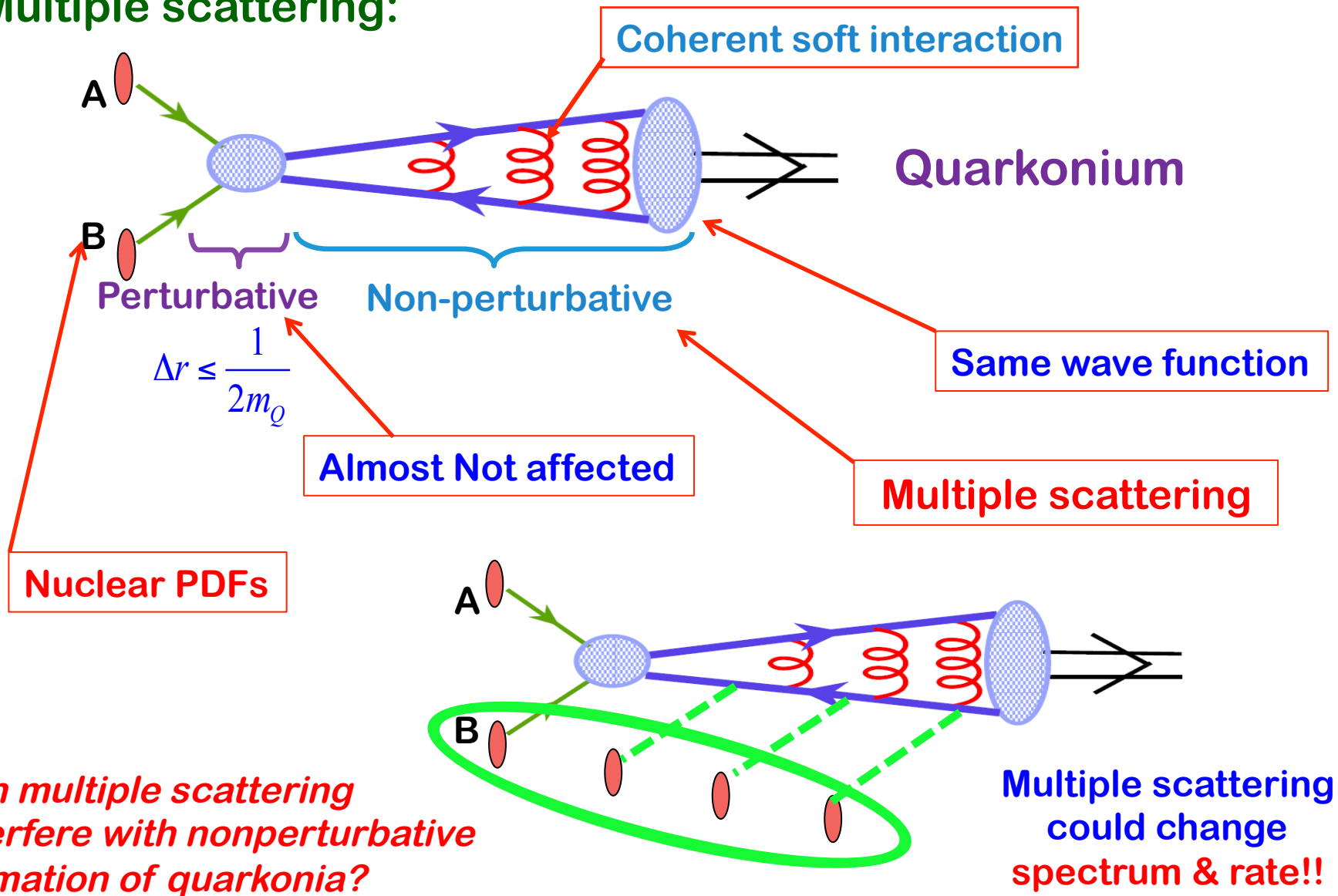


- ✧ NO QGP ($m_Q \gg T$)! → Cold nuclear effect for the “production”
- ✧ Nuclei as potential filters of production mechanisms
- ✧ Hard probe ($m_Q \gg 1/\text{fm}$) → quark-gluon structure of nucleus!

Nucleus is not a simple superposition of nucleons!

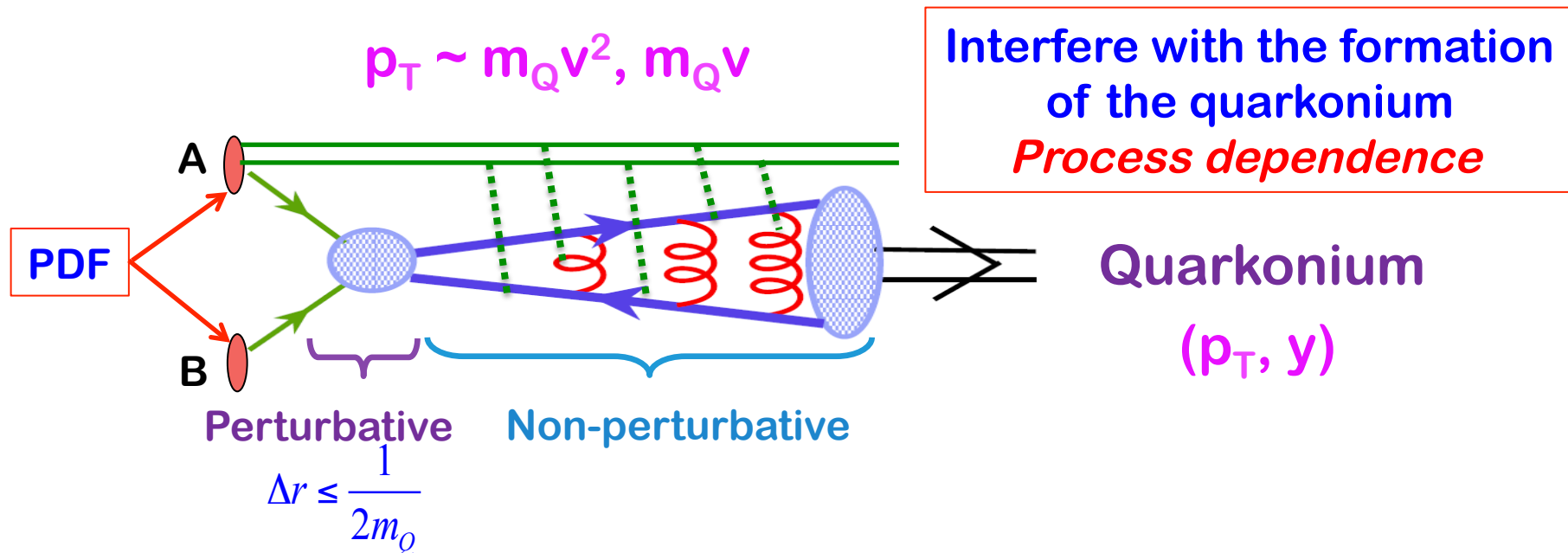
Production in p(d)+A collisions

□ Multiple scattering:



Production at low p_T ($< M_Q$)

- Spectator interaction – always there for $p+A$, but, not for $e+A$!



- The Challenge:

Process dependence – Break of factorization – No predictive power

- The need:

Controllable calculation of medium effect, extract medium properties, ...

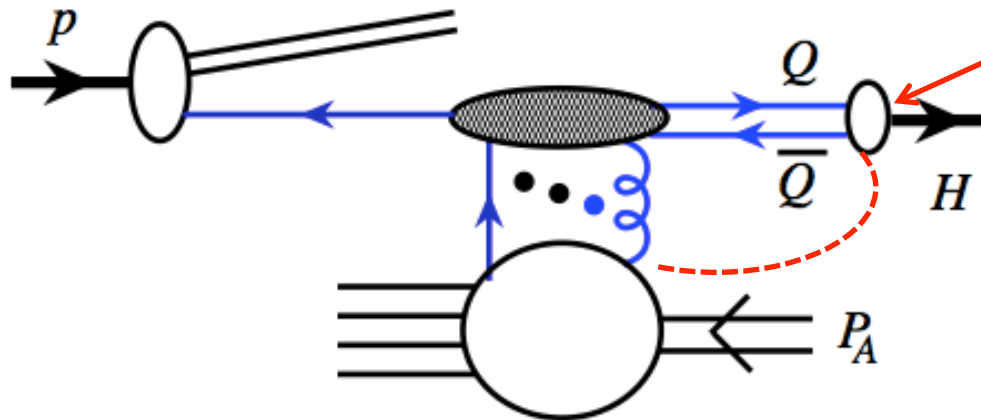
- The Opportunities:

Medium as a “detector” or “filter” to probe “color neutralization”, ...

Production with multiple scattering

Brodsky and Mueller, PLB 1988

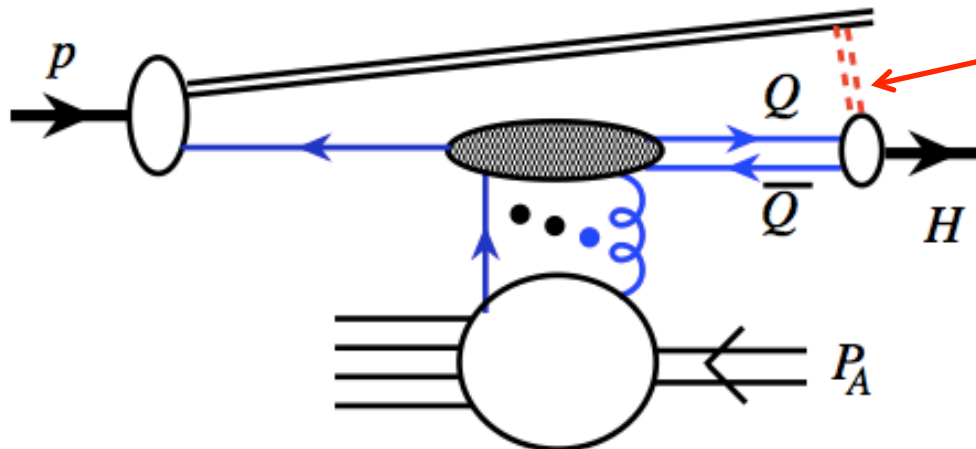
□ *Backward* production in p(d)+A collisions:



*J/ψ could be formed
Inside nucleus*

*Multiple scattering interfere
with the non-perturbative
hadronization
– no factorization!!*

□ Production at low $P_T (\rightarrow 0)$ in p(d)+A collisions:



Co-mover interaction

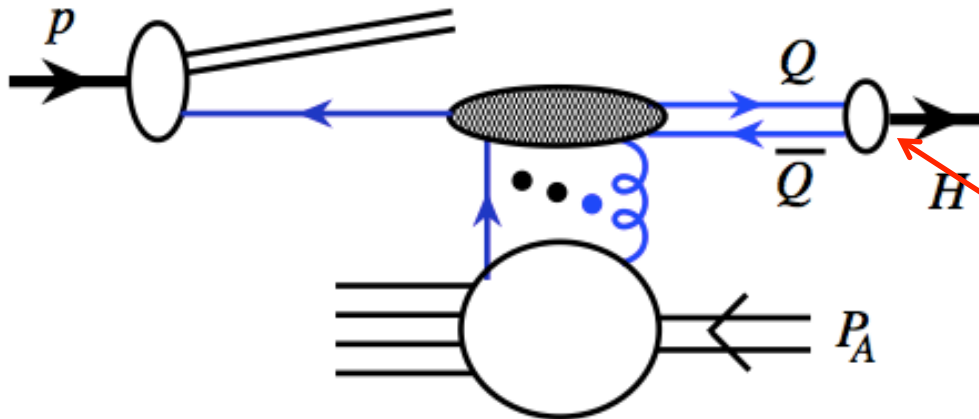
*to interfere with
quarkonium formation
– Break of factorization!!*

NOT a problem for e+A!

Production with multiple scattering

Brodsky and Mueller, PLB 1988

□ *Forward* production in $p(d)+A$ collisions:



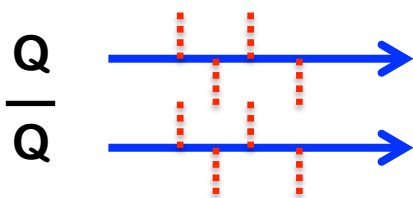
✧ Time dilation

Non-perturbative formation of J/ψ is far outside of nucleus

✧ SAME for $e+A$!

✧ Multiple scattering between partons & heavy quarks, not J/ψ

- ◆ Induced gluon radiation – energy loss – **suppression at large y**
- ◆ Modified P_T spectrum – **transverse momentum broadening**
- ◆ De-coherence of the pair – different $Q\bar{Q}$ state to hadronize – **lower rate**



Soft multiple scattering – “random walk”



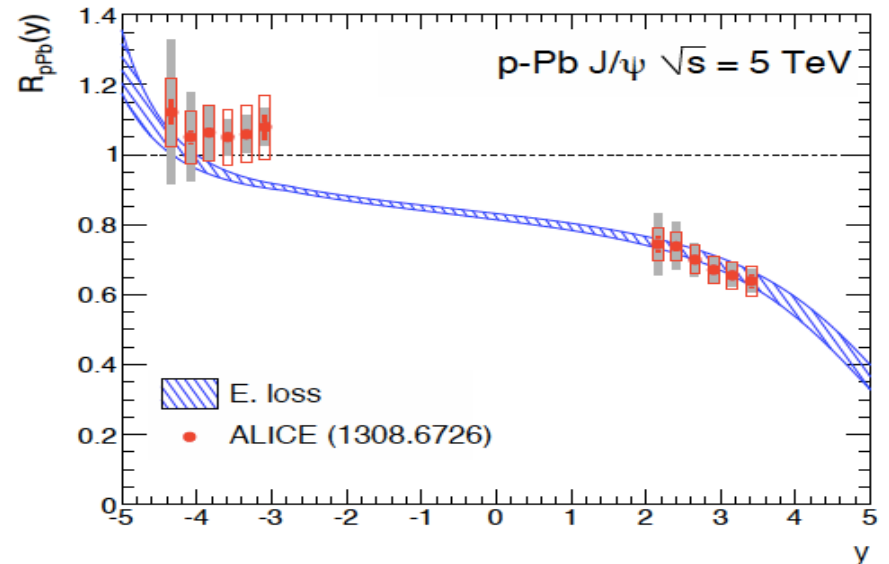
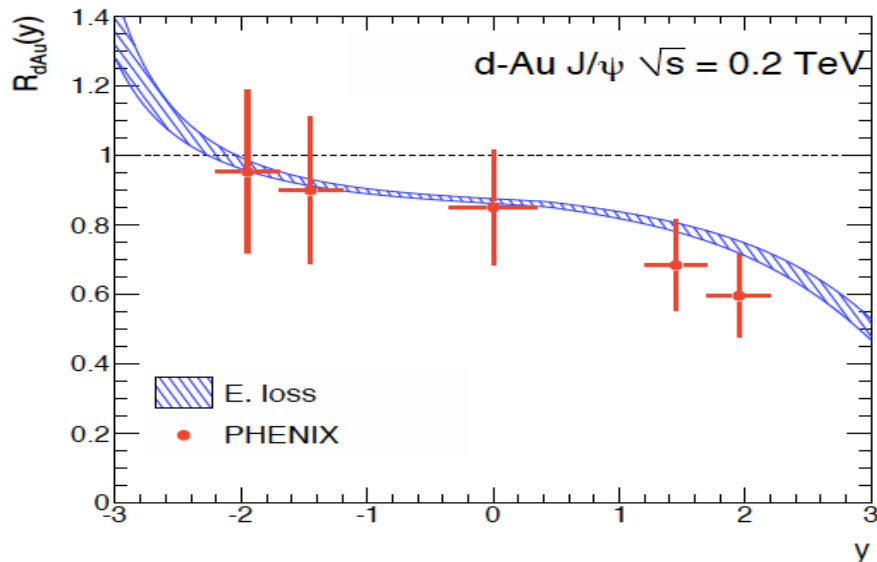
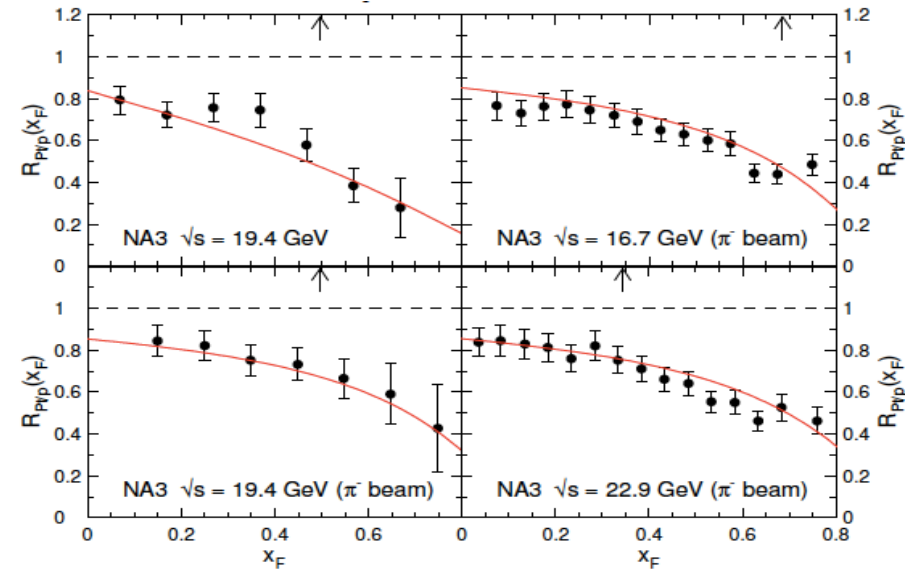
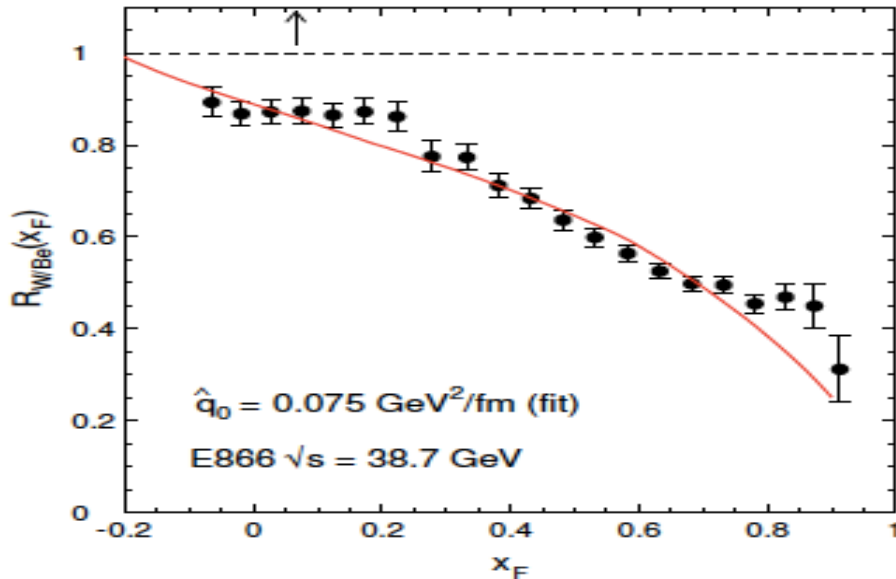
Momentum imbalance – larger invariant mass



Match to the tail of wave function - “suppression”

A-dependence in rapidity y (x_F) in p+A

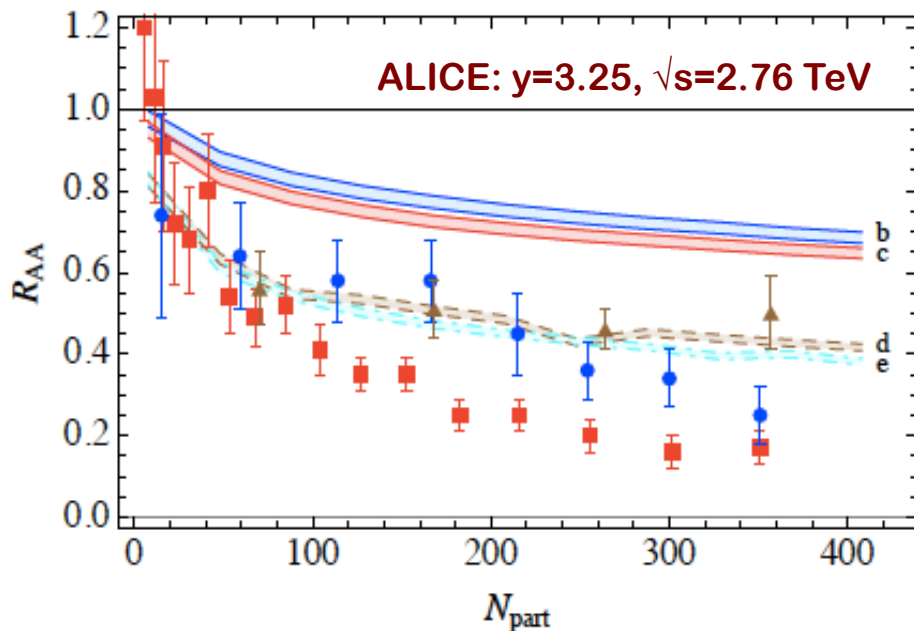
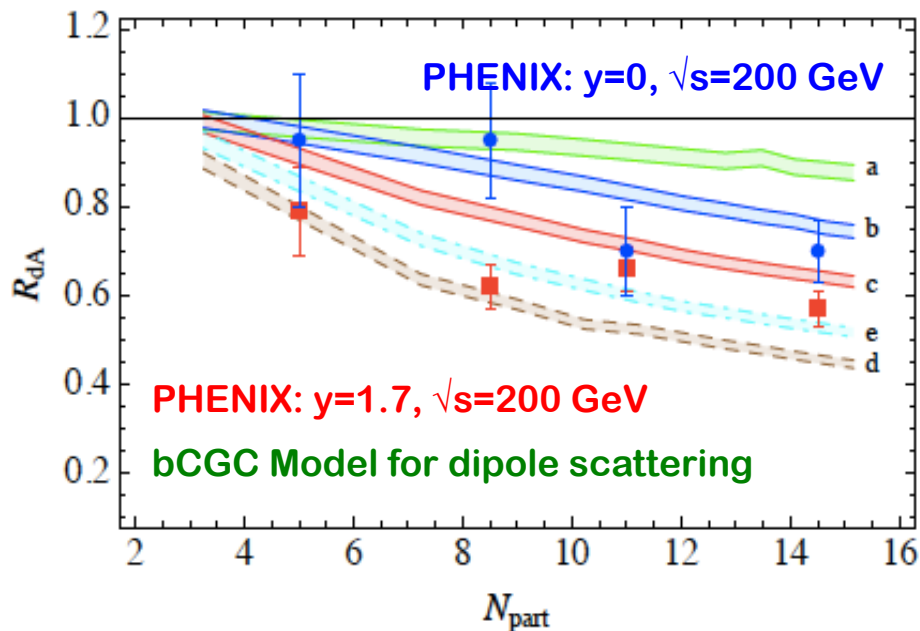
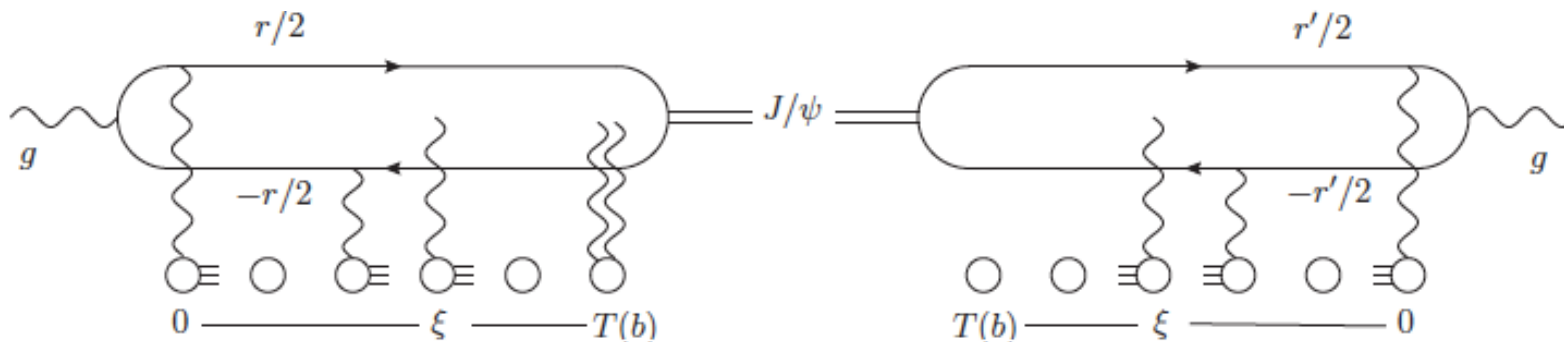
Arleo, Peigne, 2012, Arleo, Kolevator, Peigne, 2014



Multiple scattering in pA collisions

Dominguez, Kharzeev, Levin, Mueller, and Tuchin, 2011

$$\frac{d\sigma_{pA \rightarrow J/\psi X}}{d^2b dy} = x_1 G(x_1, m_c^2) \frac{d\sigma_{gA \rightarrow J/\psi X}}{d^2b}$$

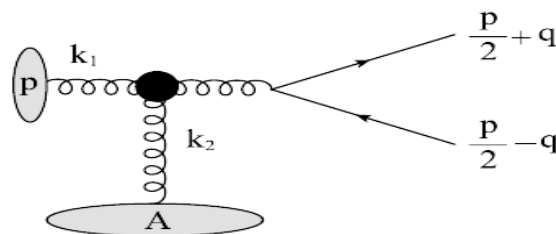
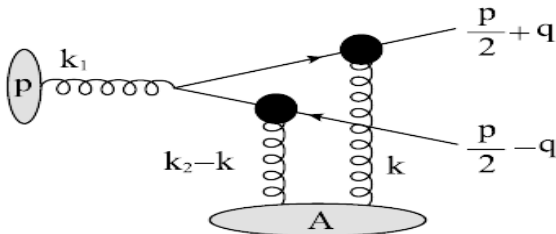


OK for pA, but, far off for AA – J/ψ melting in QGP (MS 1986)?

Forward quarkonium production in p(d)+A

□ Calculation of multiple scattering:

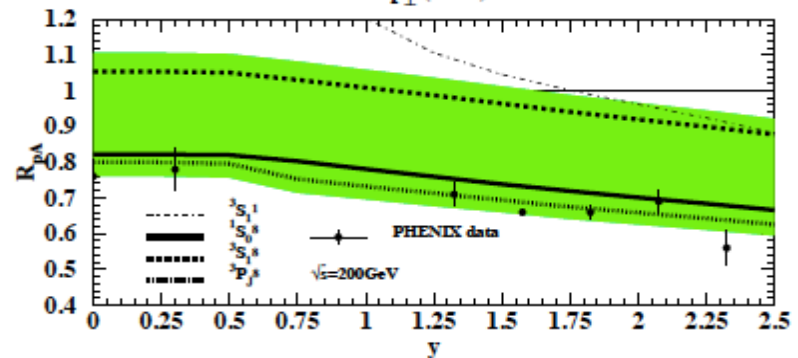
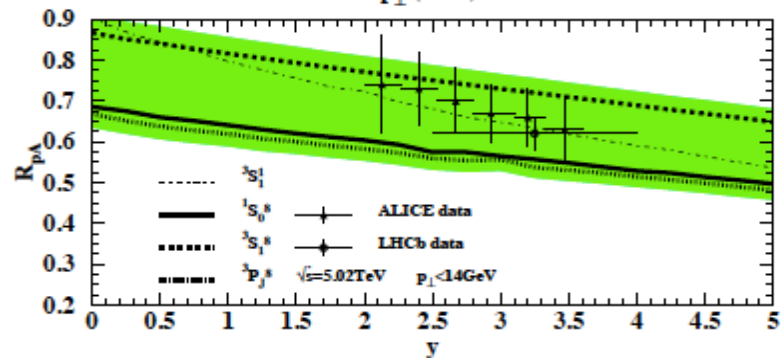
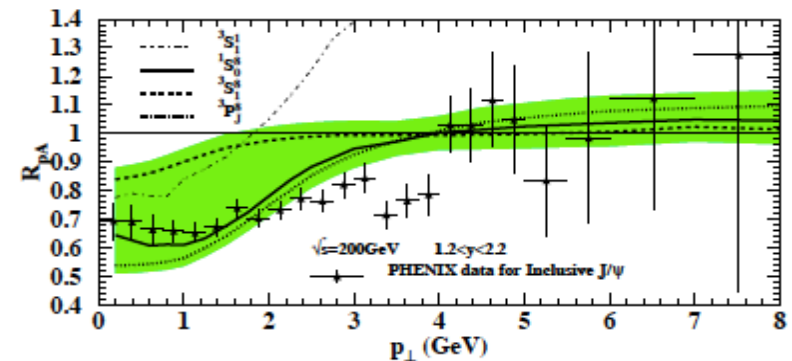
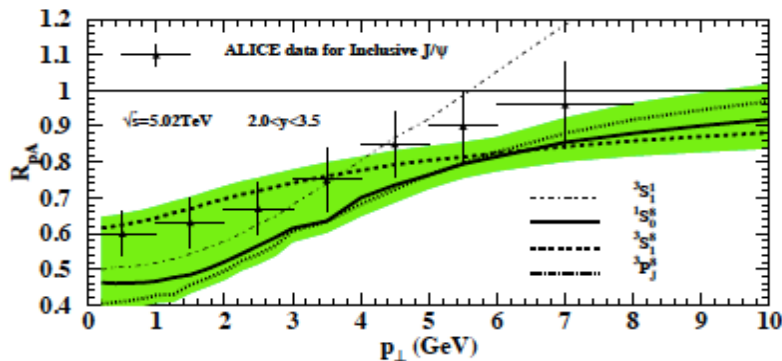
Kang, Ma, Venugopalan, JHEP (2014)
Qiu, Sun, Xiao, Yuan PRD89 (2014)



Coherent multiple scattering



suppression at large y



Ma, Venugopalan, Zhang, PRD92, 071901 (2015)

Quarkonium p_T distribution

□ Quarkonium production is dominated by low p_T region

□ Low p_T distribution at collider energies:

determined mainly by gluon shower of incoming partons

– initial-state effect

Qiu, Zhang, PRL, 2001

□ Final-state interactions suppress the formation of J/ψ :

Also modify the p_T spectrum – move low p_T to high p_T – broadening

– Final-state effect

□ Broadening:

✧ Sensitive to the medium properties

✧ Perturbatively calculable

$$\langle (q_T^2)^n \rangle = \frac{\int dq_T^2 (q_T^2)^n d\sigma/dq_T^2}{\int dq_T^2 d\sigma/dq_T^2}$$

$$\Delta \langle q_T^2 \rangle = \langle q_T^2 \rangle_{AB} - \langle q_T^2 \rangle_{NN}$$

□ R_{pA} at low q_T :

Guo, Qiu, Zhang, PRL, PRD 2002

$$R(A, q_T) \equiv \frac{1}{A} \frac{d\sigma^{hA}}{dQ^2 dq_T^2} \bigg/ \frac{d\sigma^{hN}}{dQ^2 dq_T^2} \equiv A^{\alpha(A, q_T) - 1} \approx 1 + \frac{\Delta \langle q_T^2 \rangle}{A^{1/3} \langle q_T^2 \rangle_{hN}} \left[-1 + \frac{q_T^2}{\langle q_T^2 \rangle_{hN}} \right]$$

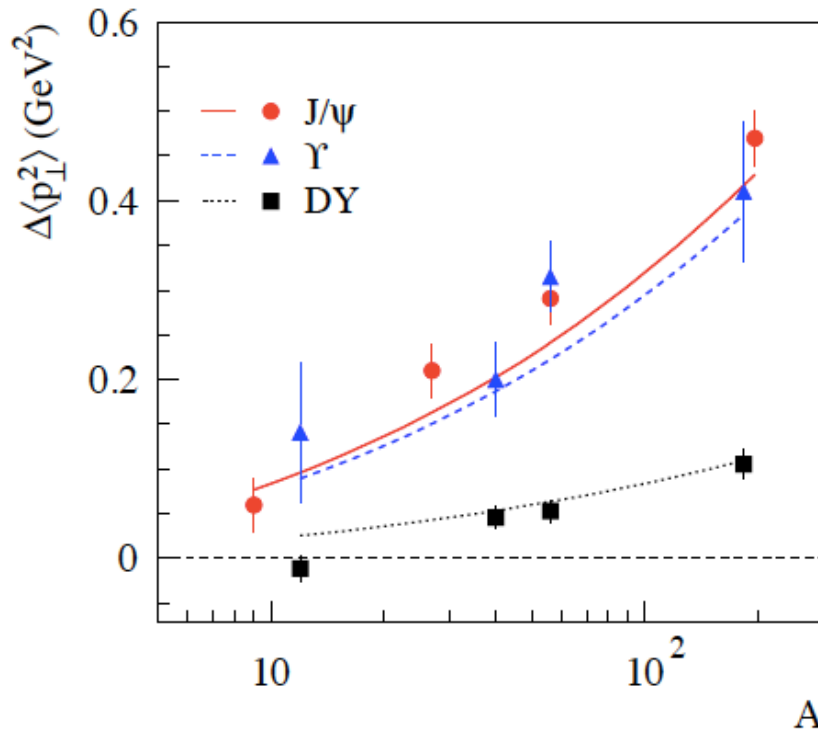
Quarkonium P_T -broadening in p(d)+A

Kang, Qiu, PRD77(2008)

□ Broadening:

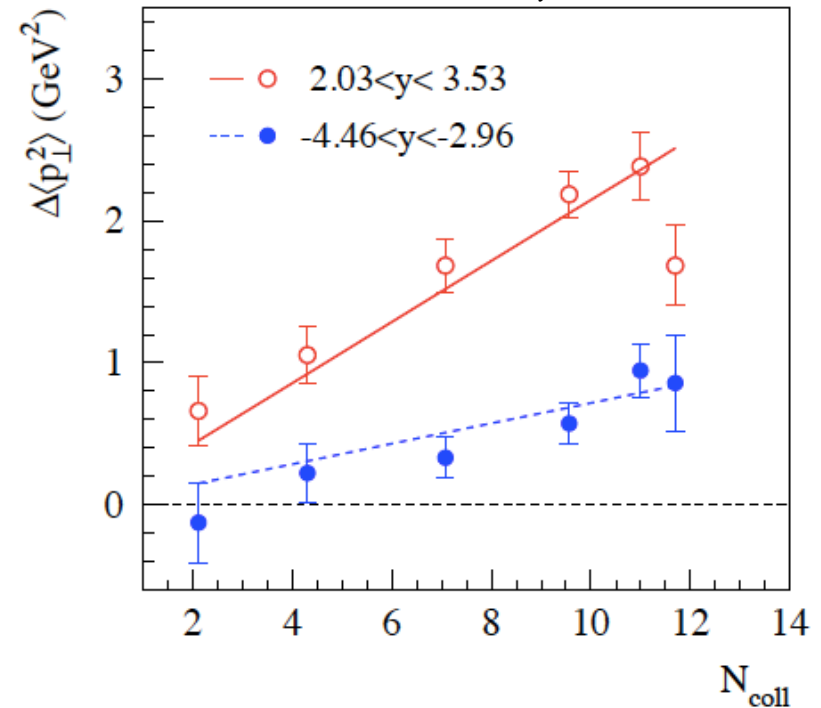
$$\Delta \langle q_T^2 \rangle_{J/\psi}^{(I)} = C_A \left(\frac{8\pi^2 \alpha_s}{N_c^2 - 1} (A^{1/3} - 1) \lambda^2 \right) \approx \Delta \langle q_T^2 \rangle_{J/\psi}^{(F)} \quad \text{Calculated in both NRQCD and CEM}$$

$$\lambda^2 = \kappa \ln(Q) x^{-\delta} \propto \hat{q}, \quad \kappa = 3.51 \times 10^{-3} \text{ 1/GeV}^2, \quad \delta = 1.71 \times 10^{-1}$$



$$(A^{1/3} - 1) \rightarrow (A^{1/3} - 1) N_{\text{coll}} / N_{\text{coll}}^{\text{min.bias}}$$

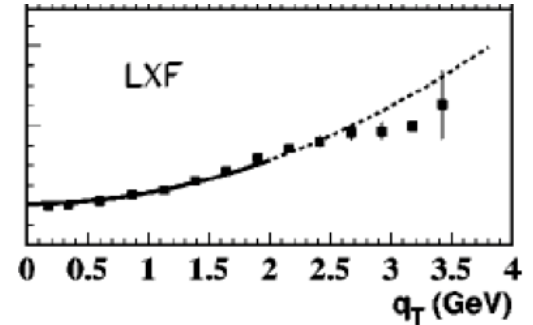
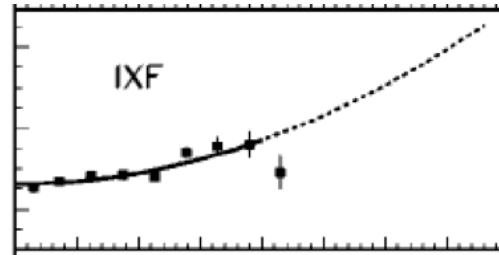
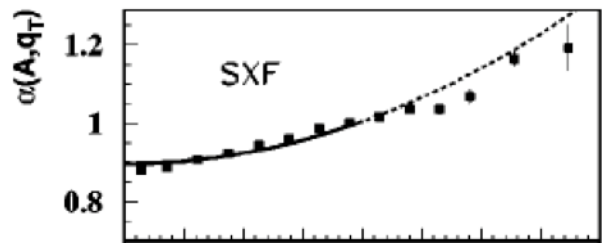
ALiCE: I. Lakomov, QWG2014



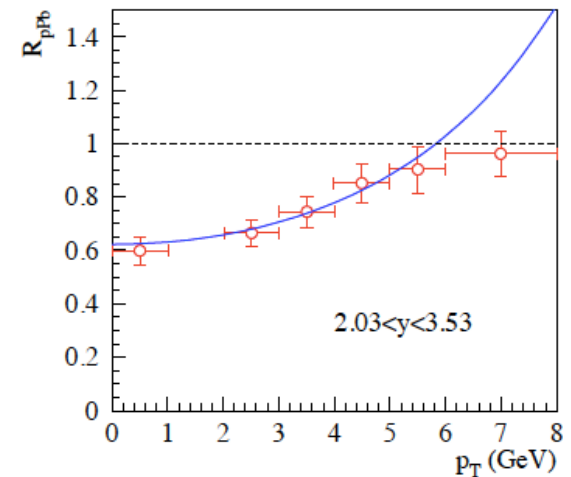
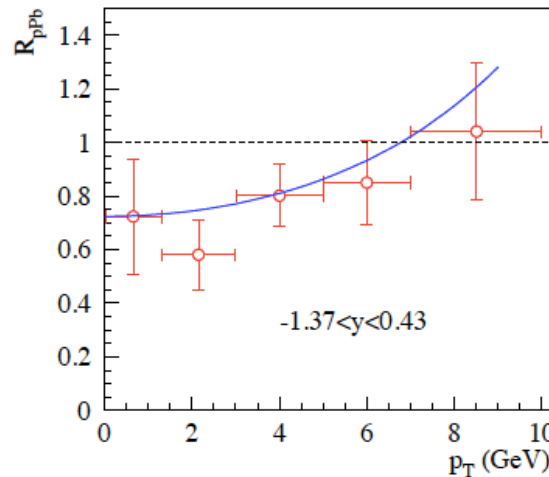
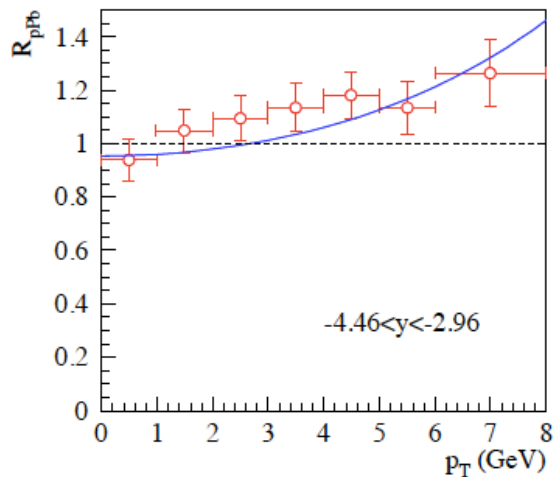
Quarkonium P_T -distribution in p(d)+A

□ Nuclear modification – low p_T region:

$$\frac{d\sigma_{AB}}{dyd^2p_T} \approx \frac{d\sigma_{AB}}{dy} \left[\frac{1}{\pi(\langle p_T^2 \rangle_{NN} + \Delta \langle p_T^2 \rangle_{AB})} e^{-p_T^2 / (\langle p_T^2 \rangle_{NN} + \Delta \langle p_T^2 \rangle_{AB})} \right]$$



E772 data – consistent with theory



ALICE data – Theory prediction

Summary

- ❑ It has been over 40 years since the discovery of J/ψ , but, still not completely sure about its production mechanism
- ❑ EIC kinematics covers all potential issues/physics of heavy quarkonium production + opportunity for the threshold production

Connection to the trace anomaly (proton mass), XYZ states, ...

- ❑ NRQCD factorization is expected to work for $P_T \sim Q$, and QCD factorization works for both LP and NLP at high P_T
Challenge for low P_T region
- ❑ Exclusive production could be a golden process for imagining glue
- ❑ Nuclear medium could be a good “filter” or a fermi-scale detector for studying how a heavy quarkonium is emerged from a pair of heavy quarks – special role of different rapidity regions

Thank you!