



# Nucleon structure from global QCD analysis of parton distributions\*

*Wally Melnitchouk*



CTEQ-JLab (CJ) collaboration: <http://www.jlab.org/CJ>

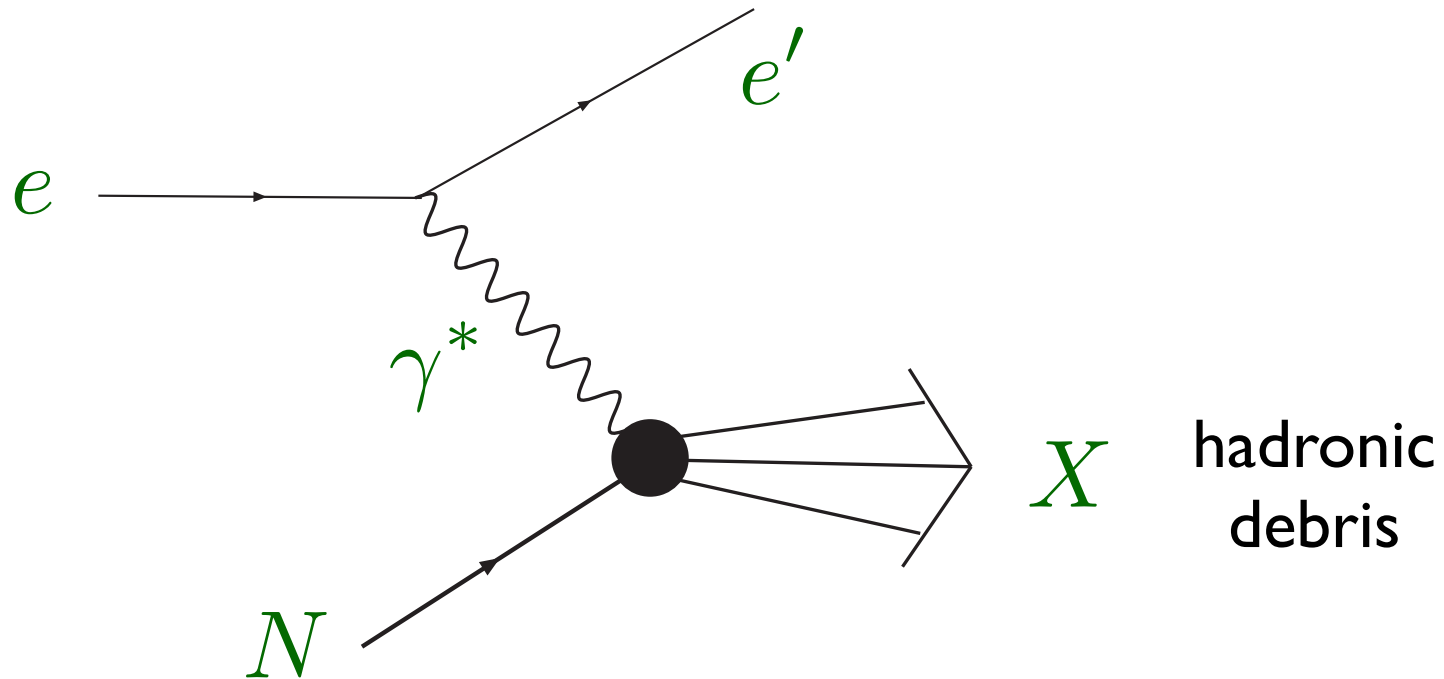
JLab Angular Momentum (JAM) collaboration: <http://www.jlab.org/JAM>

# Outline

- Introduction to PDFs
- Unpolarised distributions
  - new “CJ” global analysis (including high- $x$ , low- $Q^2$  region)
  - $d/u$  ratio and nuclear effects (tested in  $ed$  QE scattering)
  - implications of PDF uncertainties for high-energy colliders
- Spin structure of the nucleon
  - new “JAM” global analysis of polarised PDFs
  - $x \rightarrow 1$  behavior of polarised to unpolarised ratios  $\Delta q/q$
- Outlook

# Electron-nucleon scattering

- Inclusive cross section for  $eN \rightarrow eX$

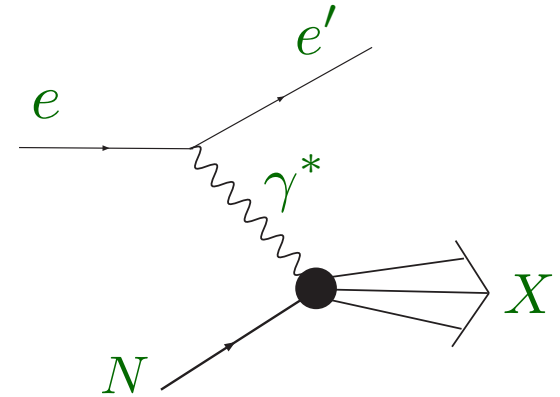


→ one-photon exchange approximation

# Electron-nucleon scattering

- Inclusive cross section for  $eN \rightarrow eX$

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left( 2 \tan^2 \frac{\theta}{2} \frac{F_1}{2M} + \frac{F_2}{\nu} \right)$$



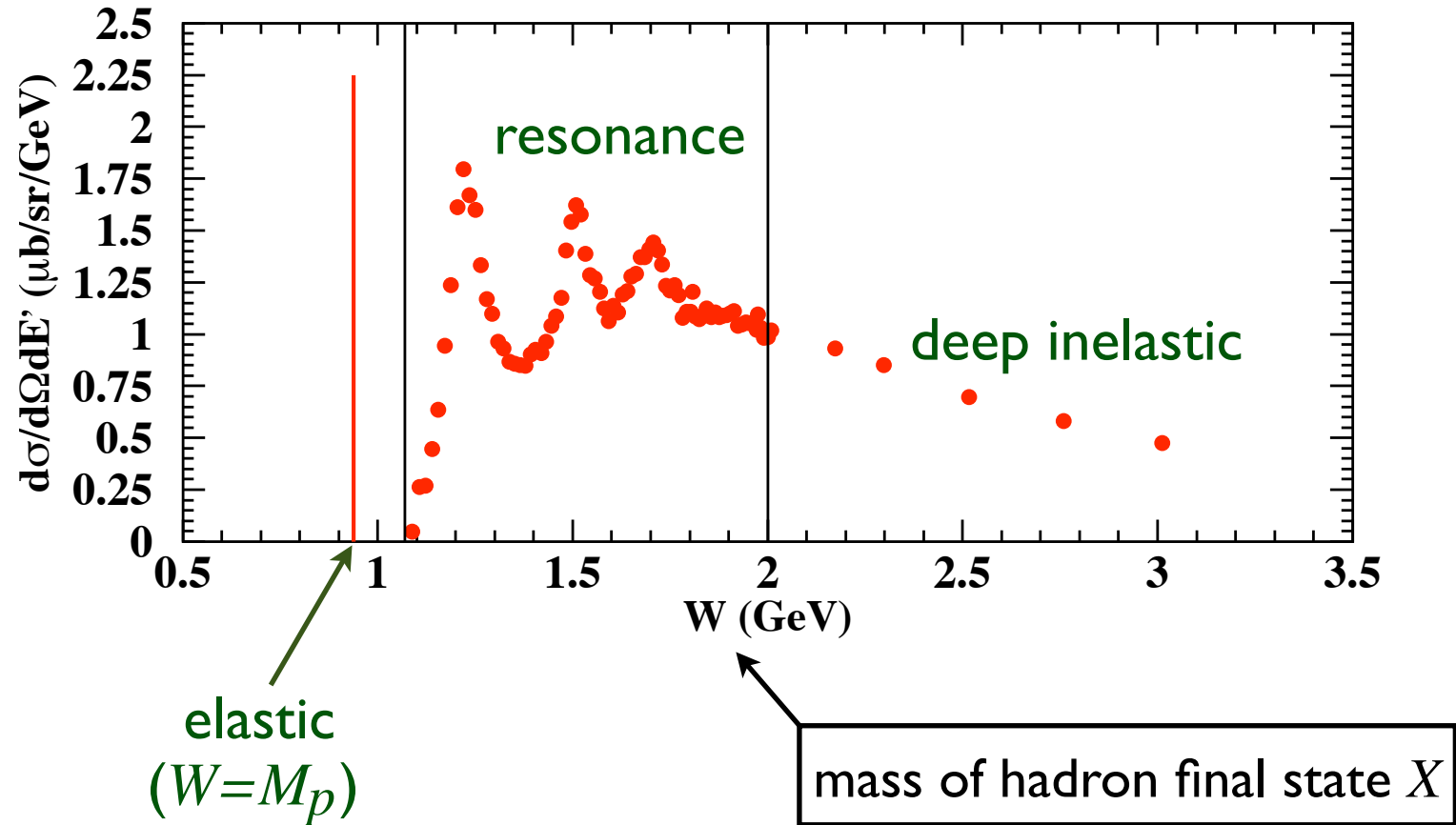
$$\left. \begin{aligned} \nu &= E - E' \\ Q^2 &= \vec{q}^2 - \nu^2 = 4EE' \sin^2 \frac{\theta}{2} \end{aligned} \right\} x = \frac{Q^2}{2M\nu}$$

Bjorken scaling variable

- Structure functions  $F_1, F_2$

→ contain all information about structure of nucleon  
( $\delta$ -functions for point-like particles)

# Electron-nucleon scattering

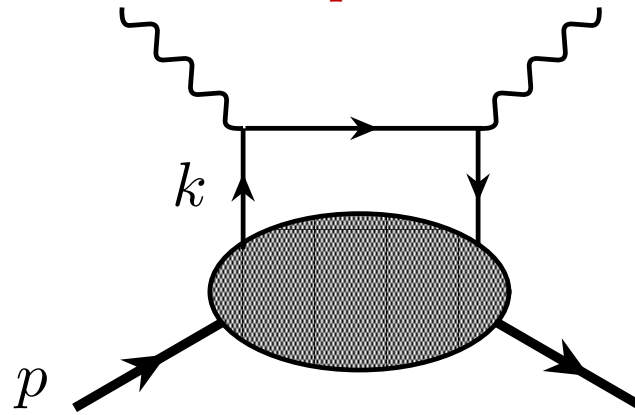


Bjorken variable in terms of  $Q^2$  &  $W$ : 
$$x = \frac{Q^2}{W^2 - M^2 + Q^2}$$

## ■ Parton model

→ scatter from individual quarks (“partons”) in nucleon

$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u, d, s\dots)$$



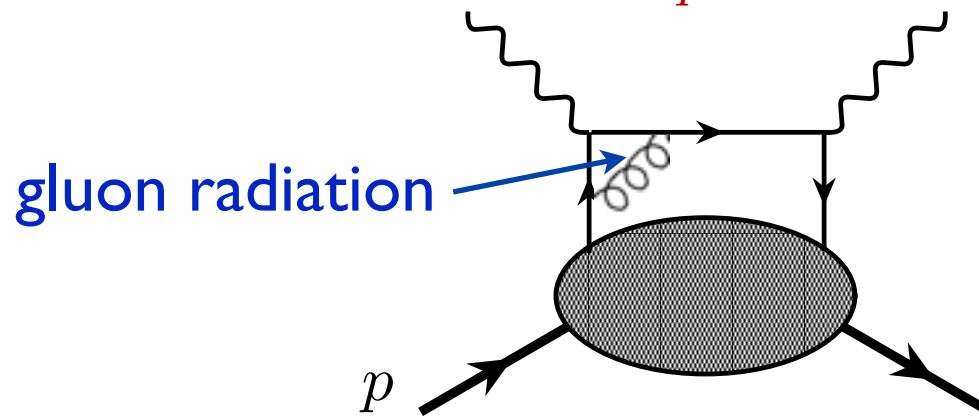
→  $q(x, Q^2)$  = probability to find quark type “ $q$ ” in nucleon, carrying (light-cone) momentum fraction  $x$

$$x = \frac{k^+}{p^+} = \frac{k^0 + k^z}{p^0 + p^z}$$

## ■ Parton model

→ scatter from individual quarks (“*partons*”) in nucleon

$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u, d, s\dots)$$

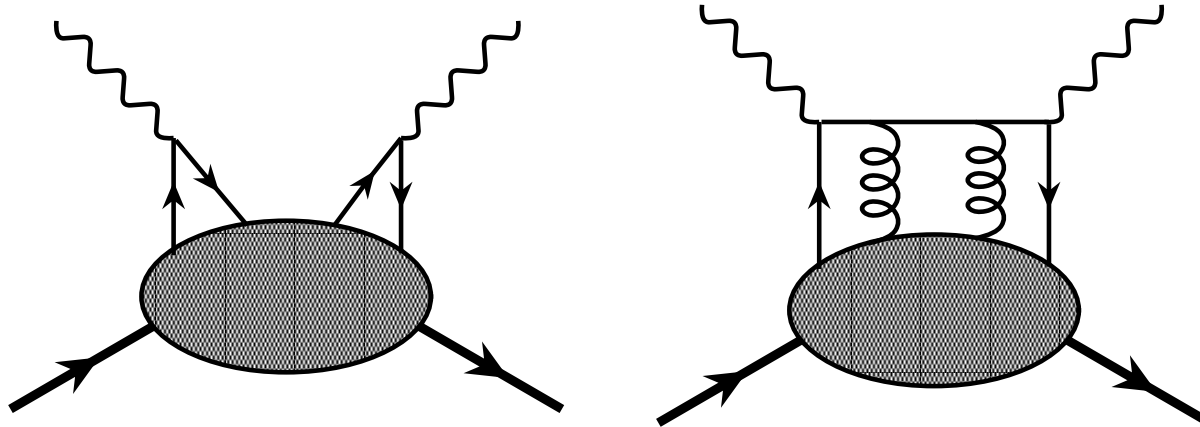


→ at finite energy,  $Q^2$  dependence given by (perturbatively calculable) QCD evolution equations

$$F_2 \rightarrow F_2(x, \log Q^2)$$

## ■ Parton model – higher twist corrections

→ scattering from *different* quarks in nucleon



“cat’s ears” diagram

quark-gluon correlations

→ gives rise to  $1/Q^2$  corrections

$$F_2(x, Q^2) = F_2^{\text{LT}}(x, Q^2) \left( 1 + \frac{C(x)}{Q^2} \right)$$

→ important at high  $x$  and low  $Q^2$



## ■ Parton model – target mass corrections

→ kinematical corrections from derivative operators

$$\sim Q^2/\nu^2 = 4M^2x^2/Q^2 \quad (\text{hence “target mass”})$$

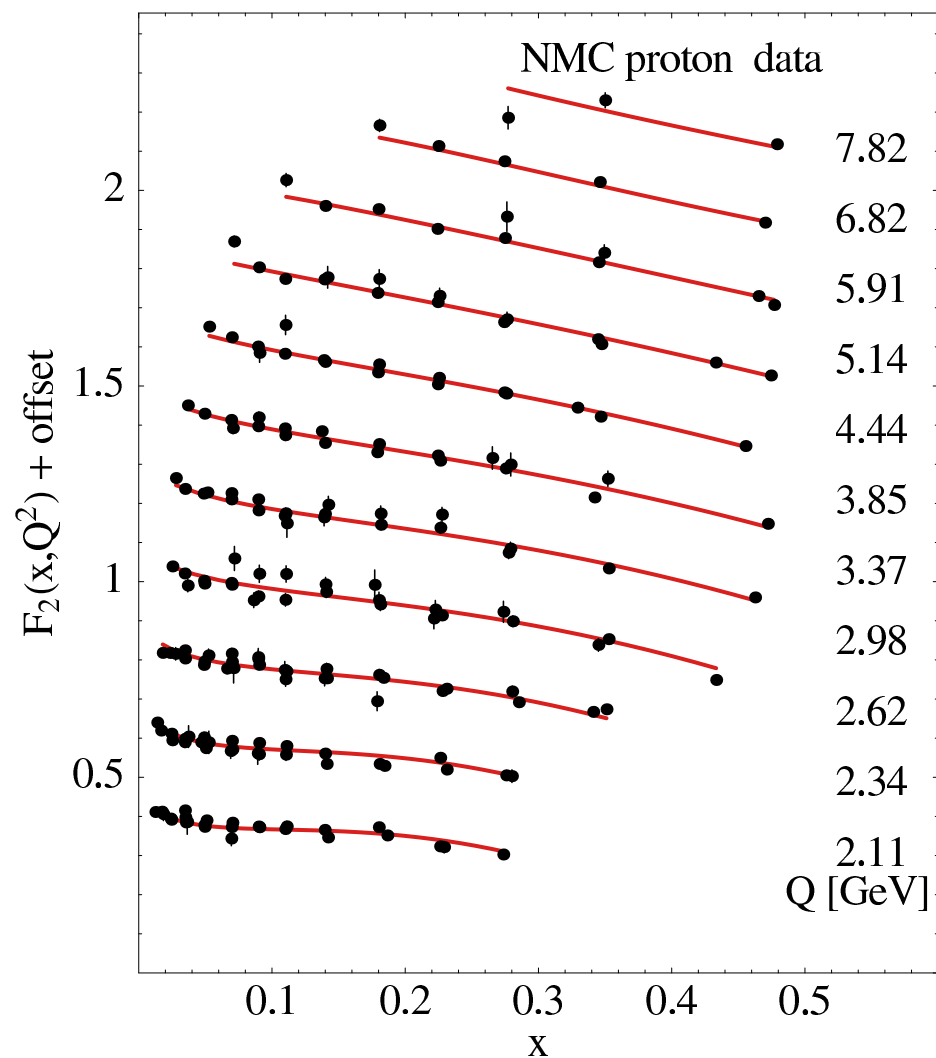
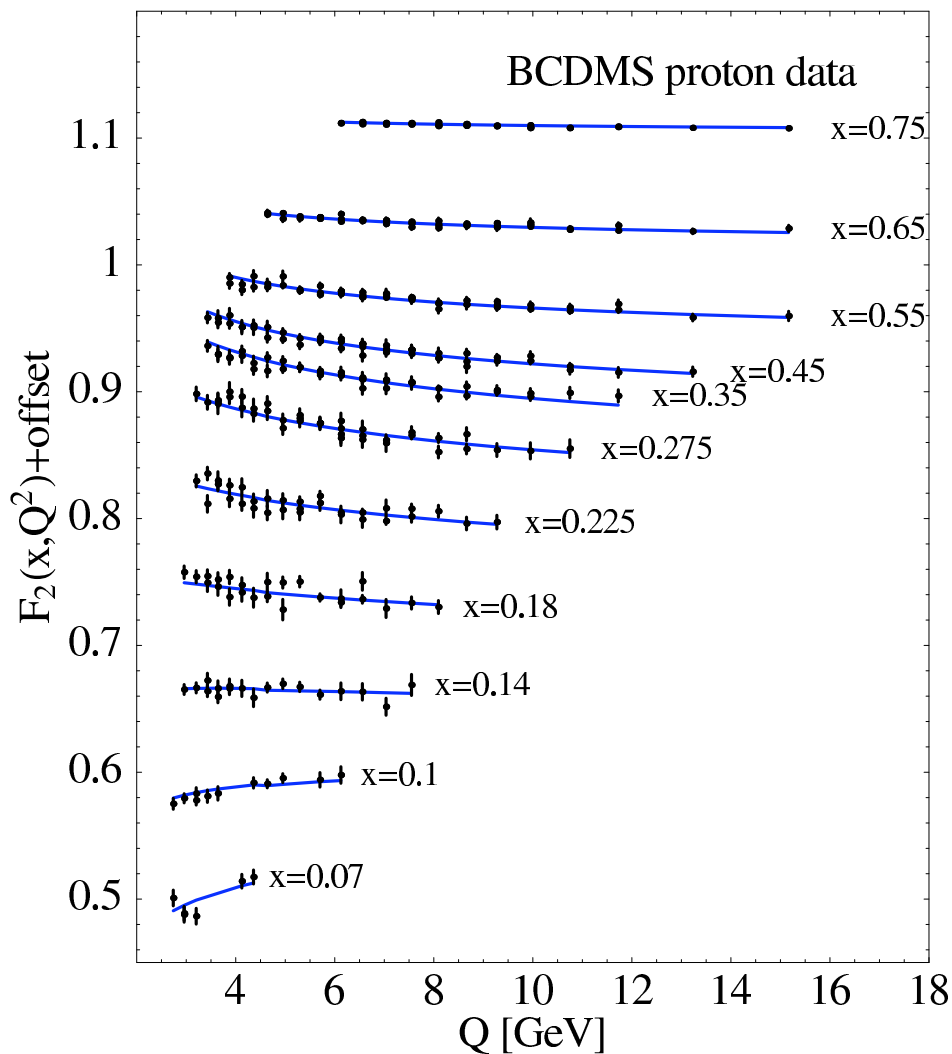
→ target mass corrected structure function

$$F_2^{\text{TMC}}(x, Q^2) = \frac{x^2}{\xi^2 \gamma^3} F_2^{(0)}(\xi, Q^2) + \frac{6M^2 x^3}{Q^2 \gamma^4} \int_{\xi}^1 du \frac{F_2^{(0)}(u, Q^2)}{u^2} \\ + \frac{12M^4 x^4}{Q^4 \gamma^5} \int_{\xi}^1 dv (v - \xi) \frac{F_2^{(0)}(v, Q^2)}{v^2}$$

●  $F_2^{(0)}$  = structure function in massless (Bjorken) limit

● new “Nachtmann” scaling variable  $\xi = \frac{2x}{1 + \sqrt{1 + 4M^2x^2/Q^2}}$

# $F_2^p$ structure function data



*Lai et al., EPJ C12, 375 (2000)*

→ describes data over many orders of magnitude in  $x$  and  $Q^2$

# Parton distribution functions (PDFs)

- PDFs extracted in global QCD analyses (CTEQ, MSTW, ...) of structure function data from  $e$ ,  $\mu$  &  $\nu$  scattering (also from lepton-pair &  $W$ -boson production in hadronic collisions)

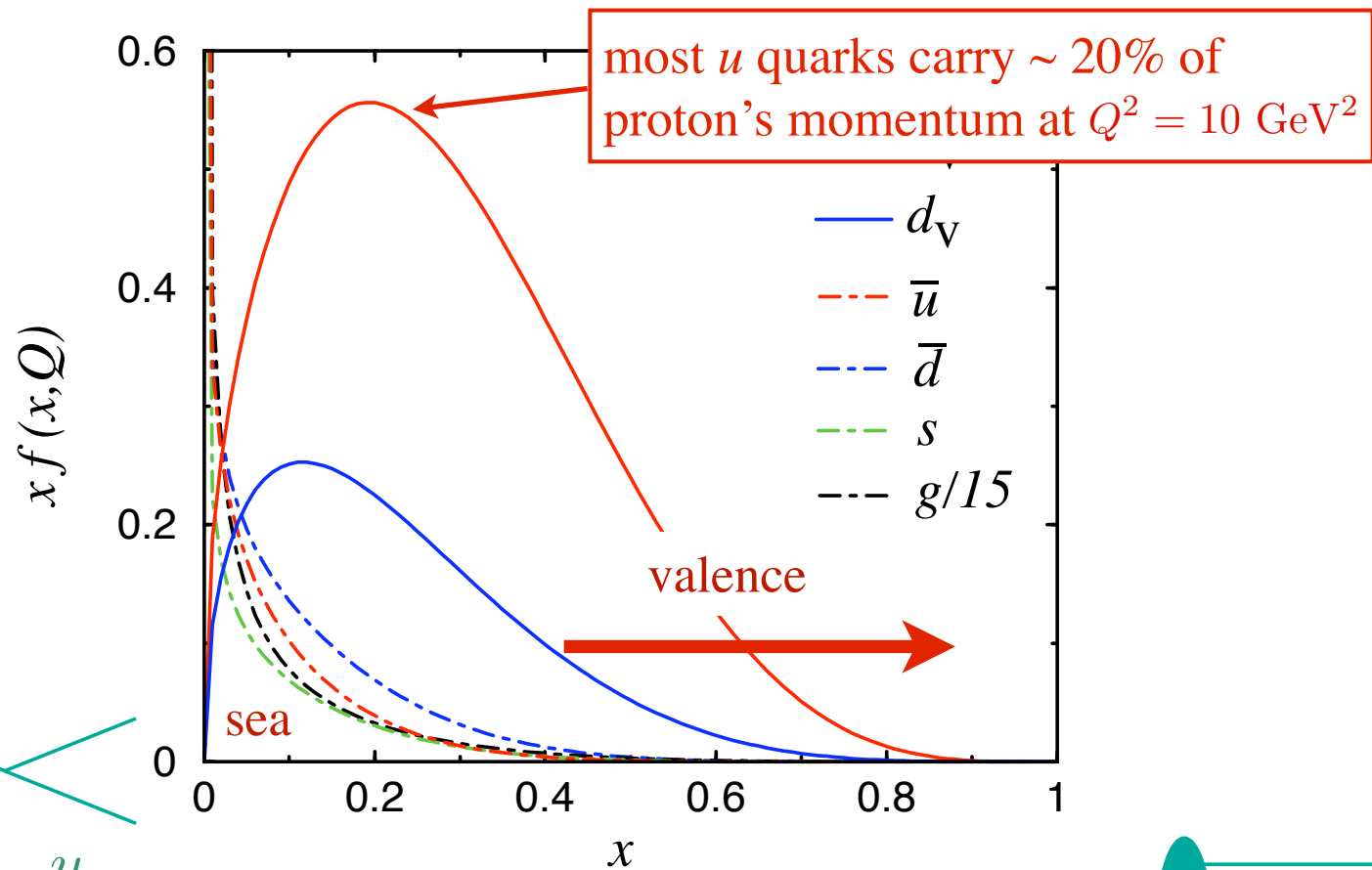
→ determined over large range of  $x$  and  $Q^2$

$$xf(x, Q_0^2) = Nx^\alpha(1-x)^\beta(1 + \epsilon\sqrt{x} + \eta x)$$

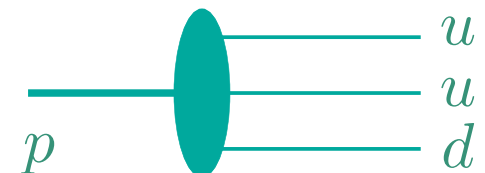
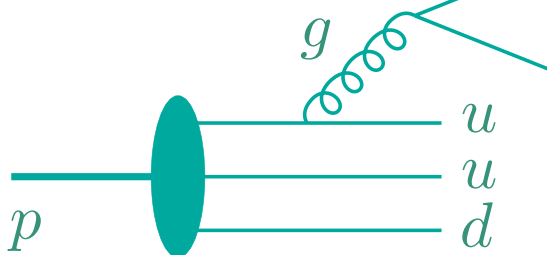
- Provide basic information on structure of QCD bound states
  - Needed to understand backgrounds in searches for physics *beyond the Standard Model* in high-energy colliders *e.g.* the LHC
- $Q^2$  evolution feeds low  $x$ , high  $Q^2$  from high  $x$ , low  $Q^2$

# Parton distribution functions (PDFs)

- Most direct connection between quark distributions and models of nucleon structure is via *valence* quarks
  - most cleanly revealed at  $x > 0.4$



structure of *hadron*  
or structure of *probe*?



## PDFs at large $x$

- At large  $x$ , valence  $u$  and  $d$  distributions extracted from  $p$  and  $n$  structure functions

$$F_2^p \approx \frac{4}{9}xu_v + \frac{1}{9}xd_v$$

$$F_2^n \approx \frac{4}{9}xd_v + \frac{1}{9}xu_v$$

- $u$  quark distribution well determined from *proton* data
- $d$  quark distribution requires *neutron* structure function

$$\longrightarrow \frac{d}{u} \approx \frac{4 - F_2^n / F_2^p}{4F_2^n / F_2^p - 1}$$

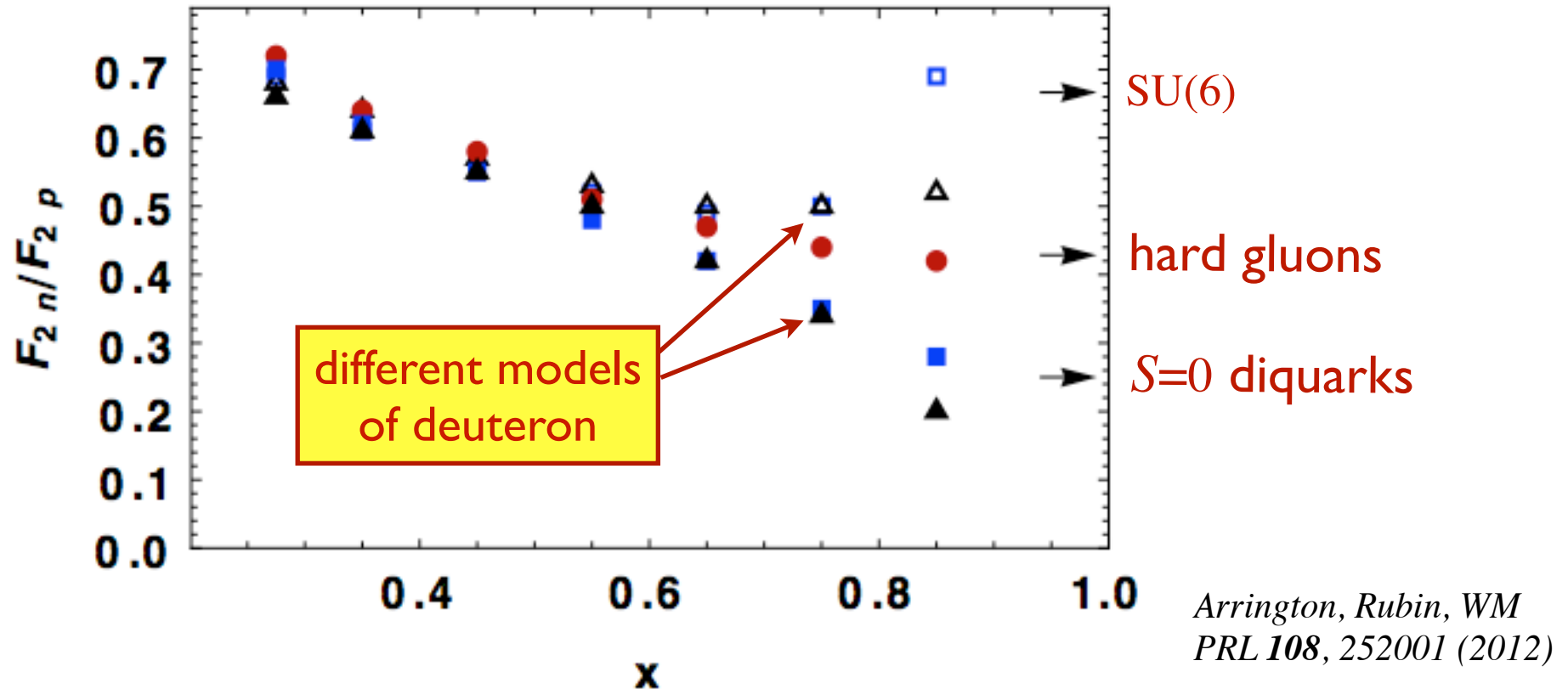
# PDFs at large $x$

- Ratio of  $d$  to  $u$  quark distributions particularly sensitive to nonperturbative quark-gluon dynamics in nucleon
  - $d/u \rightarrow 1/2$  SU(6) symmetry
  - $d/u \rightarrow 0$   $S = 0$   $qq$  dominance
  - $d/u \rightarrow 1/5$   $S_z = 0$   $qq$  dominance (pQCD-inspired)
  - $d/u \rightarrow \frac{4 \mu_n^2 / \mu_p^2 - 1}{4 - \mu_n^2 / \mu_p^2}$  local quark-hadron duality\*  
 $\approx 0.42$  ( $\mu_{p,n}$  magnetic moments)  
\*structure function at  $x \rightarrow 1$  given by elastic form factor at  $Q^2 \rightarrow \infty$

# Neutron structure

## ■ Absence of free neutron targets

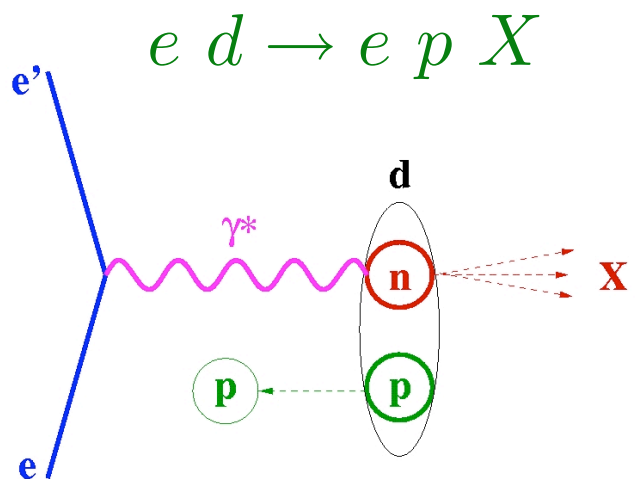
→ deuterium (weakly bound state of  $p$  and  $n$ ) used instead



→ deuteron model dependence obscures free neutron structure information at large  $x$

# Neutron structure

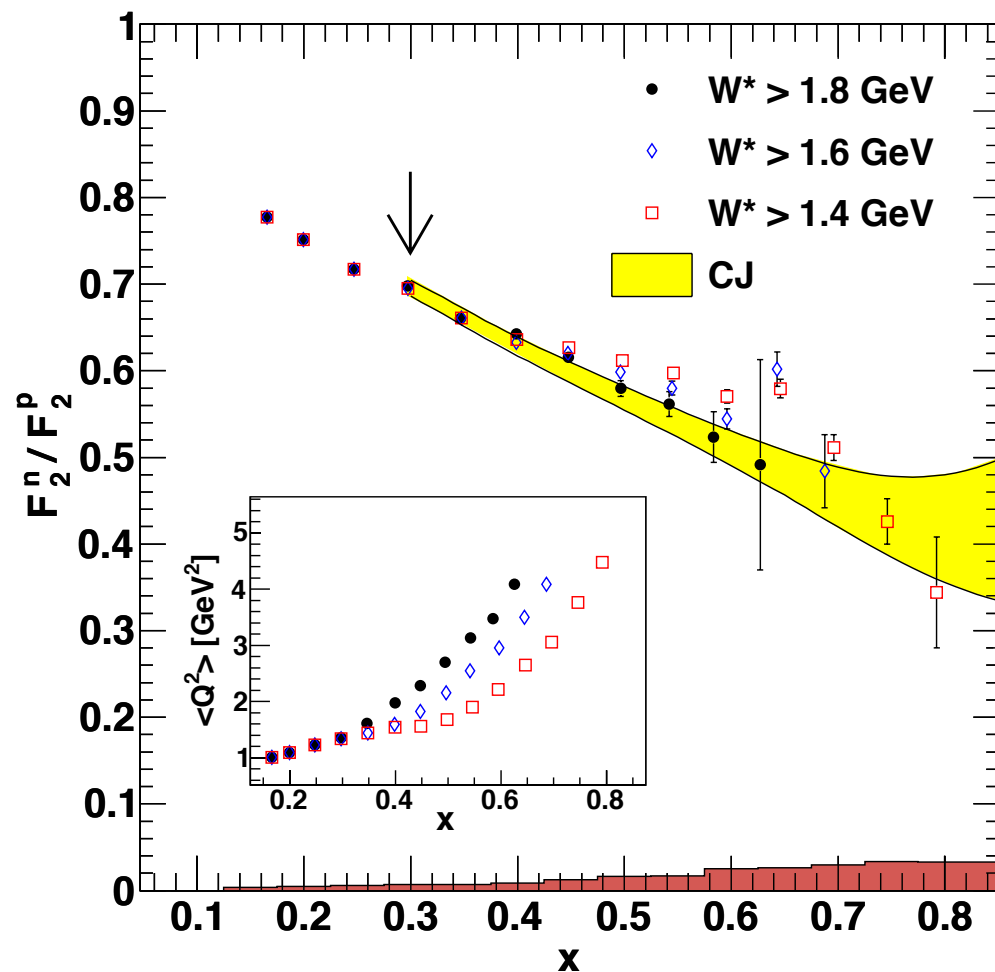
## ■ BONuS: slow spectator tagging



slow backward  $p$

→ neutron nearly on-shell

→ minimize rescattering



*Baillie et al., PRL 108, 199902 (2012)*

## ■ Need for global analysis to investigate these aspects of PDFs



# CJ global analysis of spin-averaged PDFs

A. Accardi, J. Owens, WM  
E. Christy, C. Keppel, P. Monaghan

“CJ12” PDFs: *PRD 87, 094012 (2013)*  
<http://www.jlab.org/CJ>

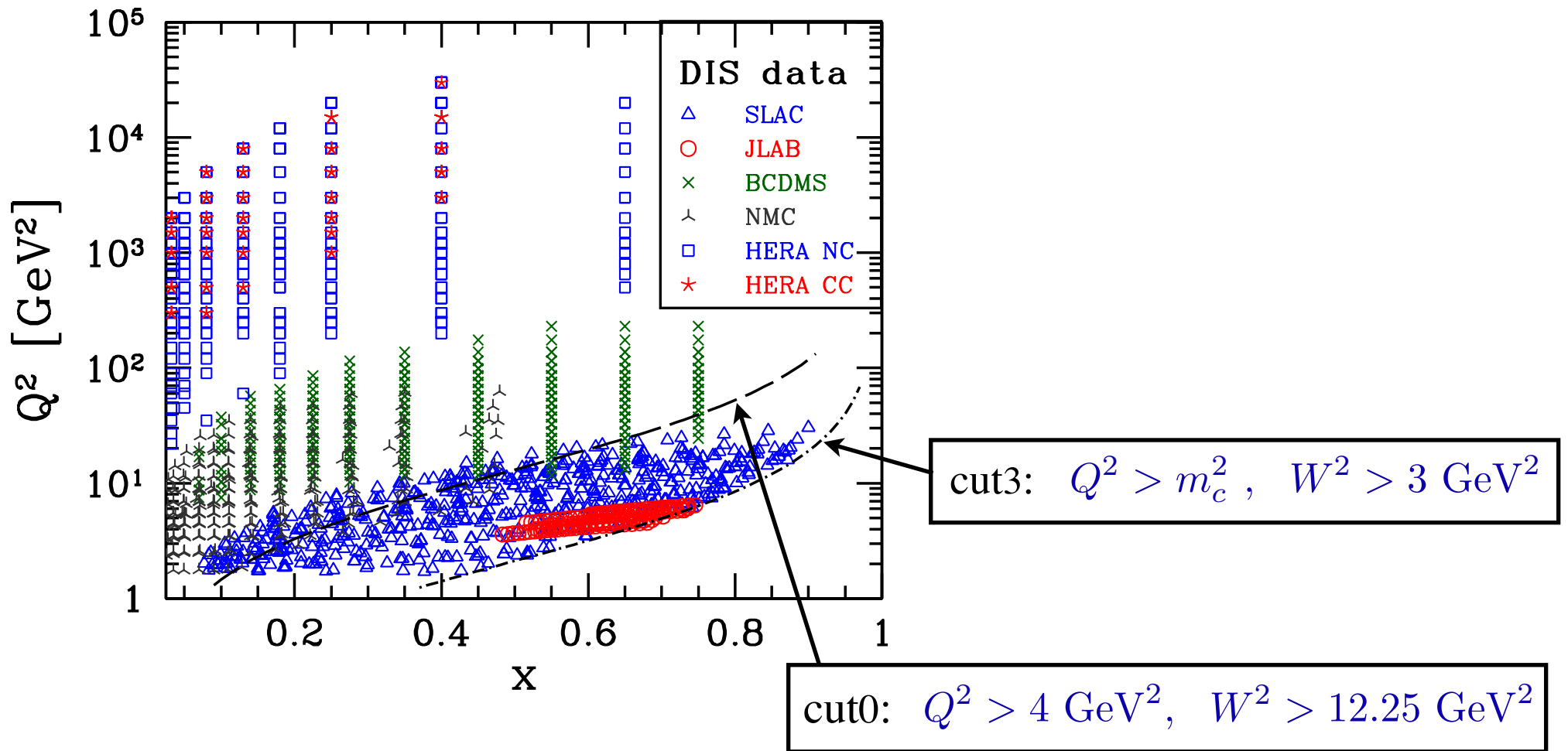
- Next-to-leading order (NLO) analysis of expanded set of *proton* and *deuterium* data (no heavy nuclei)
  - include large- $x$ , low- $Q^2$  region
- Systematically study effects of  $Q^2$  &  $W$  cuts
  - as low as  $Q \sim m_c$  and  $W \sim 1.7$  GeV
- Include subleading  $1/Q^2$  corrections
  - target mass corrections & dynamical higher twists
- Correct for nuclear effects in deuteron (binding + off-shell)
  - most global analyses assume *free* nucleons

## ■ CJ database

~ 4,000 data points  
over large range  
of  $x$  and  $Q^2$

	Experiment	Ref.	# points	$\chi^2$		
				CJ12min	CJ12mid	CJ12max
DIS $F_2$	BCDMS ( $p$ )	[13]	351	434	436	437
	BCDMS ( $d$ )	[13]	254	294	297	302
	NMC ( $p$ )	[14]	275	434	432	430
	NMC ( $d/p$ )	[15]	189	179	177	182
	SLAC ( $p$ )	[16]	565	456	455	456
	SLAC ( $d$ )	[16]	582	394	388	396
	JLab ( $p$ )	[17]	136	170	169	170
	JLab ( $d$ )	[17]	136	124	125	126
DIS $\sigma$	HERA (NC $e^-$ )	[18]	145	117	117	118
	HERA (NC $e^+$ )	[18]	384	595	596	596
	HERA (CC $e^-$ )	[18]	34	19	19	19
	HERA (CC $e^+$ )	[18]	34	32	32	32
Drell-Yan	E866 ( $p$ )	[19]	184	220	221	221
	E866 ( $d$ )	[19]	191	297	307	306
W asymmetry	CDF 1998 ( $\ell$ )	[20]	11	14	16	18
	CDF 2005 ( $\ell$ )	[21]	11	11	11	10
	DØ 2008 ( $\ell$ )	[22]	10	4	4	4
	DØ 2008 ( $e$ )	[23]	12	40	36	34
	CDF 2009 ( $W$ )	[24]	13	20	25	41
Z rapidity	CDF ( $Z$ )	[25]	28	29	27	27
	DØ ( $Z$ )	[26]	28	16	16	16
jet	CDF run 1	[27]	33	52	52	52
	CDF run 2	[28]	72	14	14	14
	DØ run 1	[29]	90	21	20	19
	DØ run 2	[30]	90	19	19	20
$\gamma$ +jet	DØ 1	[31]	16	6	6	6
	DØ 2	[31]	16	13	13	12
	DØ 3	[31]	12	17	17	17
	DØ 4	[31]	12	17	16	17
TOTAL			3958	4059	4055	4096
TOTAL + norm				4075	4074	4117

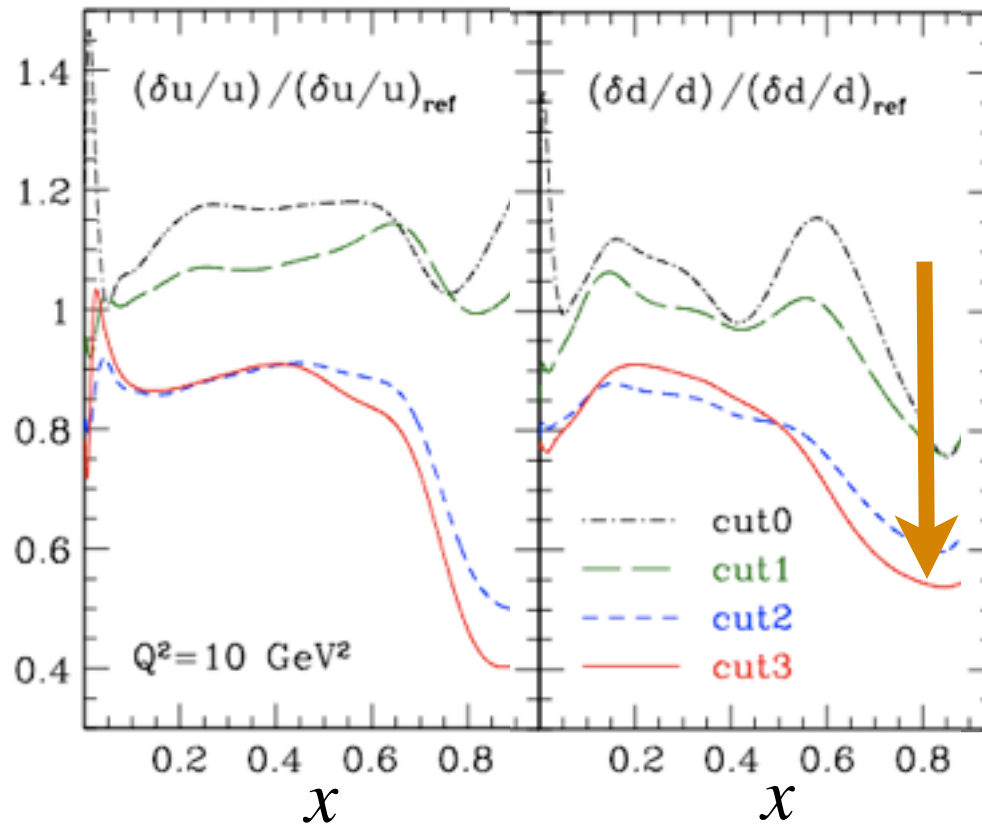
# Kinematic cuts



→ factor 2 increase in DIS data from cut0 → cut3 compared to most global analyses

# Kinematic cuts

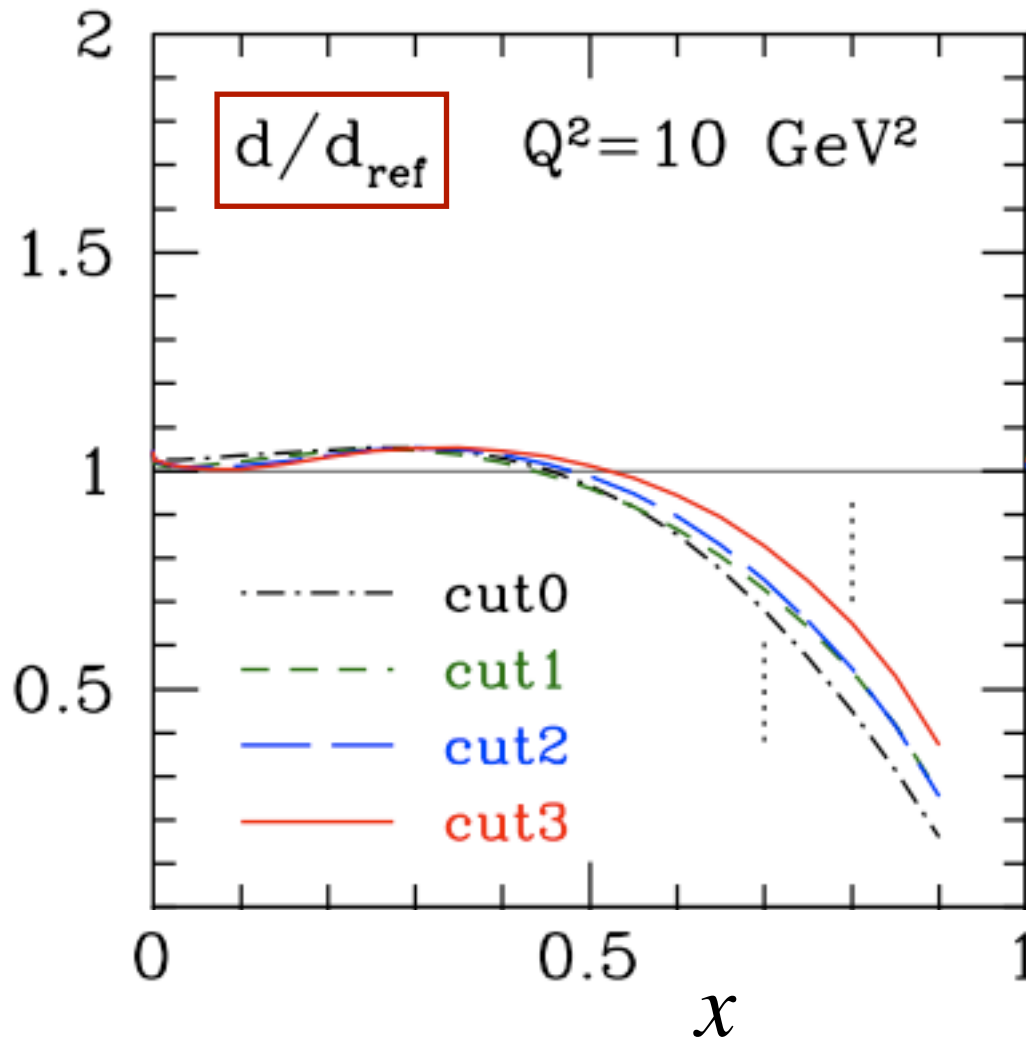
- Larger database with weaker cuts leads to significantly reduced errors, especially at large  $x$



→ up to 40–60% error reduction when cuts extended into resonance region

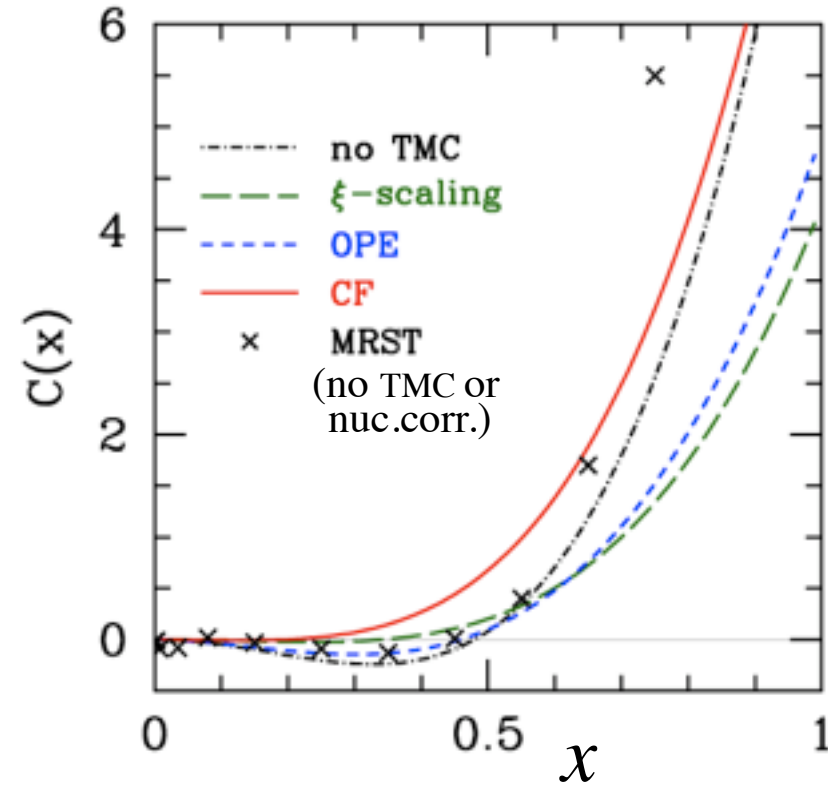
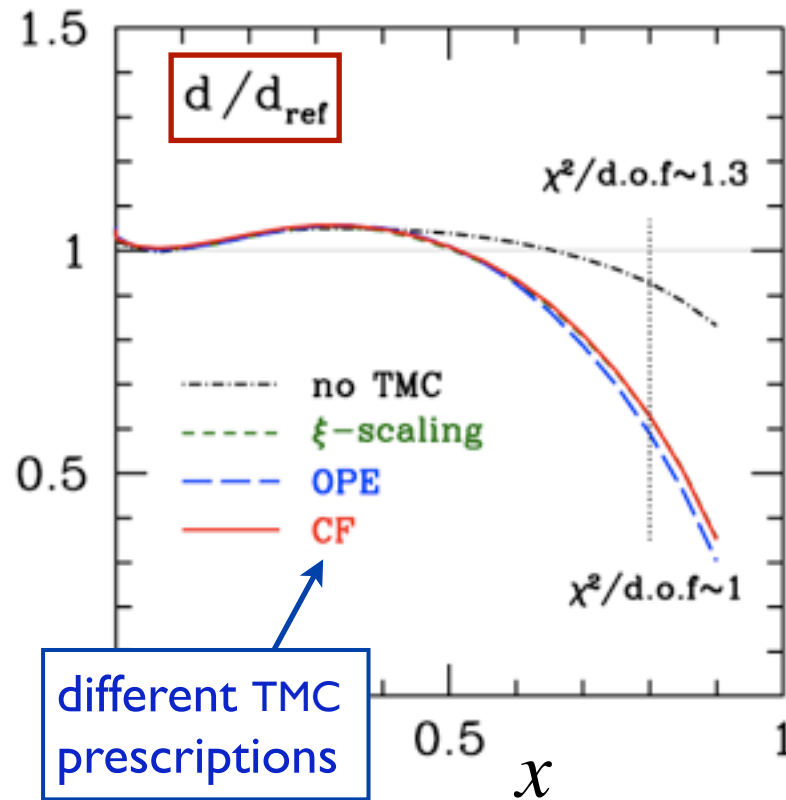
# Kinematic cuts

- Fits stable with respect to  $Q^2$  and  $W$  cut reduction, as long as subleading  $1/Q^2$  corrections included



→  $d$  quark suppressed by  $\sim 50\%$  for  $x > 0.5$  (driven by nuclear corrections)

# Finite- $Q^2$ corrections

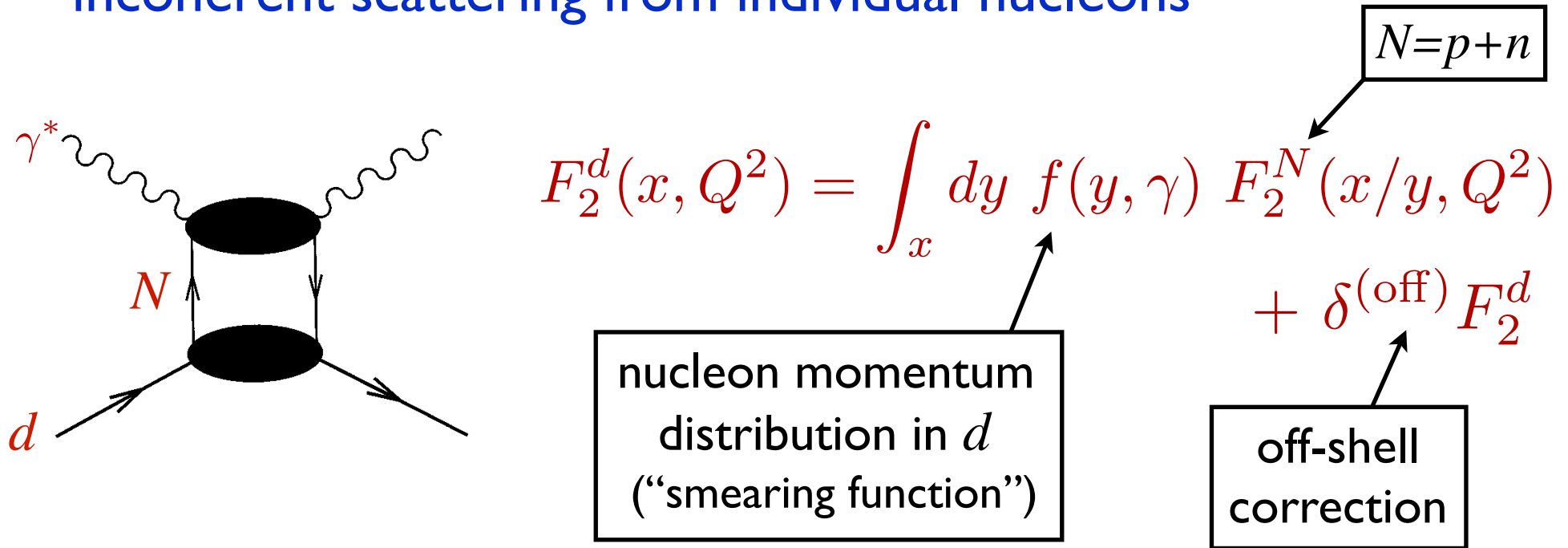


*Accardi et al., PRD 81, 034016 (2010)*

- interplay between TMCs and higher twist
  - stable LT when both TMCs and HTs included
- growing importance of HTs as large  $x$

# Nuclear corrections

- Nuclear structure function at  $x \gg 0$  dominated by incoherent scattering from individual nucleons



→  $y =$  light-cone momentum fraction of  $d$  carried by  $N$

→ at finite  $Q^2$ , smearing function depends also on parameter

$$\gamma = |\mathbf{q}|/q_0 = \sqrt{1 + 4M^2 x^2 / Q^2}$$

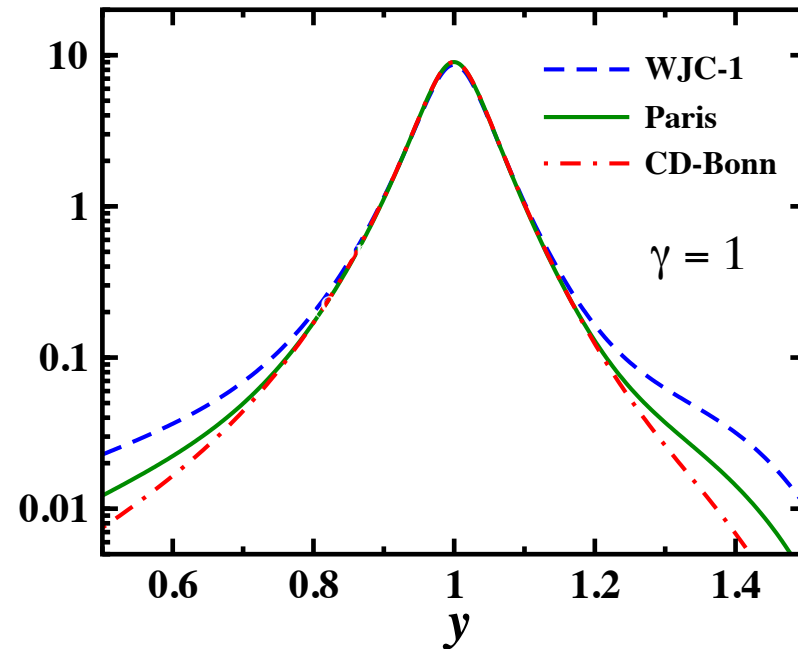
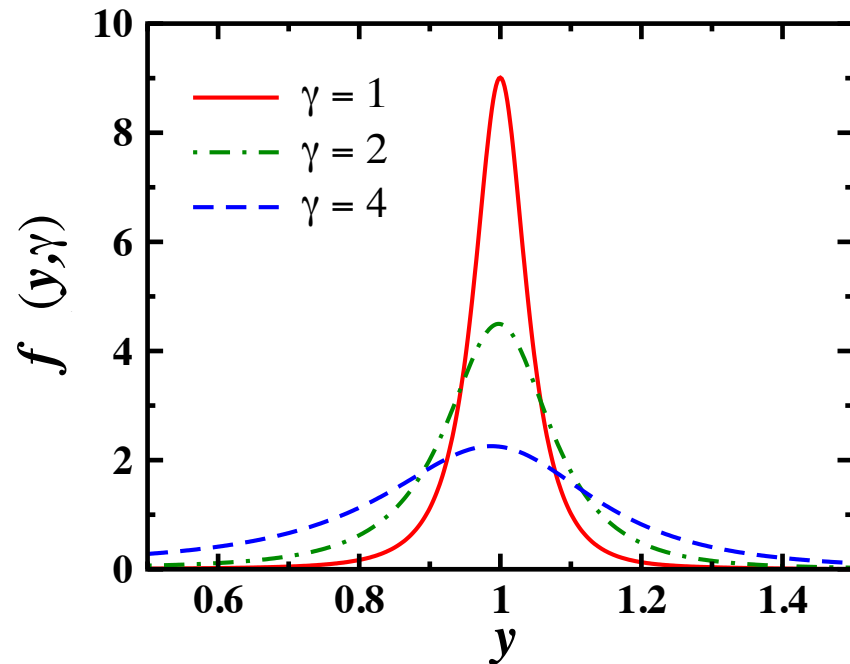


# Nuclear corrections

- Smearing function in the deuteron computed in “weak binding approximation” – expand in powers of  $\vec{p}^2/M^2$

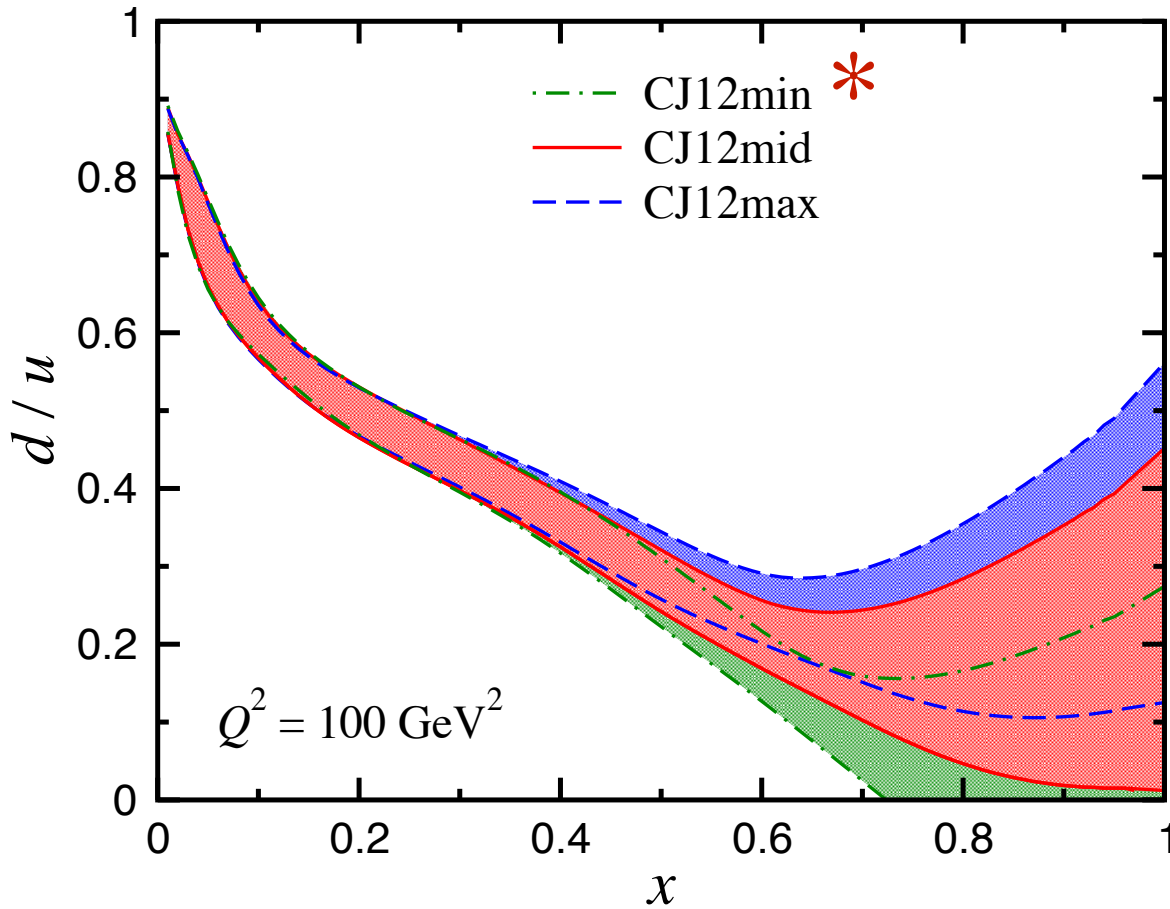
$$f(y, \gamma) = \int \frac{d^3p}{(2\pi)^3} |\psi_d(p)|^2 \delta\left(y - 1 - \frac{\varepsilon + \gamma p_z}{M}\right) \times \frac{1}{\gamma^2} \left[ 1 + \frac{\gamma^2 - 1}{y^2} \left( 1 + \frac{2\varepsilon}{M} + \frac{\vec{p}^2}{2M^2} (1 - 3\hat{p}_z^2) \right) \right]$$

$\psi_d(p) = d \text{ wave function}$   
 $\varepsilon = \varepsilon_d - \frac{\vec{p}^2}{2M}$



- effectively more smearing for larger  $x$  and lower  $Q^2$
- greater wave function dependence at large  $y$  ( $\rightarrow$  large  $x$ )

# Nuclear corrections



Owens, Accardi WM  
PRD 87, 094012 (2013)

- flexible parametrization for  $x \rightarrow 1$  behavior

$$d \rightarrow d + a x^b u$$

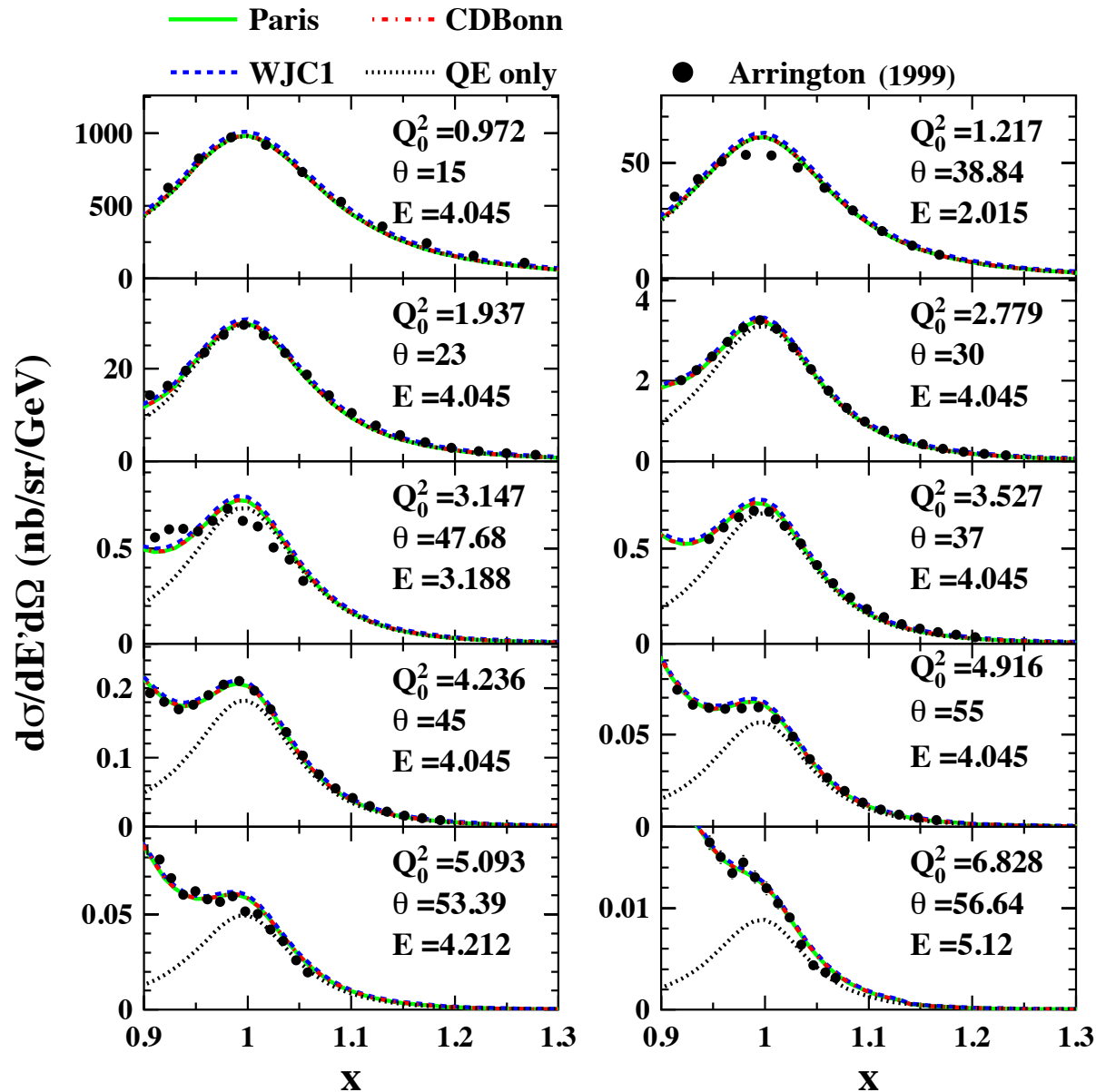
- allows finite, nonzero  $x = 1$  limit

$$\begin{aligned} d/u &\rightarrow 0.22 \\ &\pm 0.20 \text{ (PDF)} \\ &\pm 0.10 \text{ (nucl)} \end{aligned}$$

- \* CJ12min: WJC-1 + mild off-shell (0.3% nucleon swelling)
- CJ12mid: AV18 + medium off-shell (1.2% swelling)
- CJ12max: CD-Bonn + large off-shell (2.1% swelling)

# Quasi-elastic *ed* scattering

- Smearing functions can be tested in quasi-elastic (QE) electron–deuteron scattering



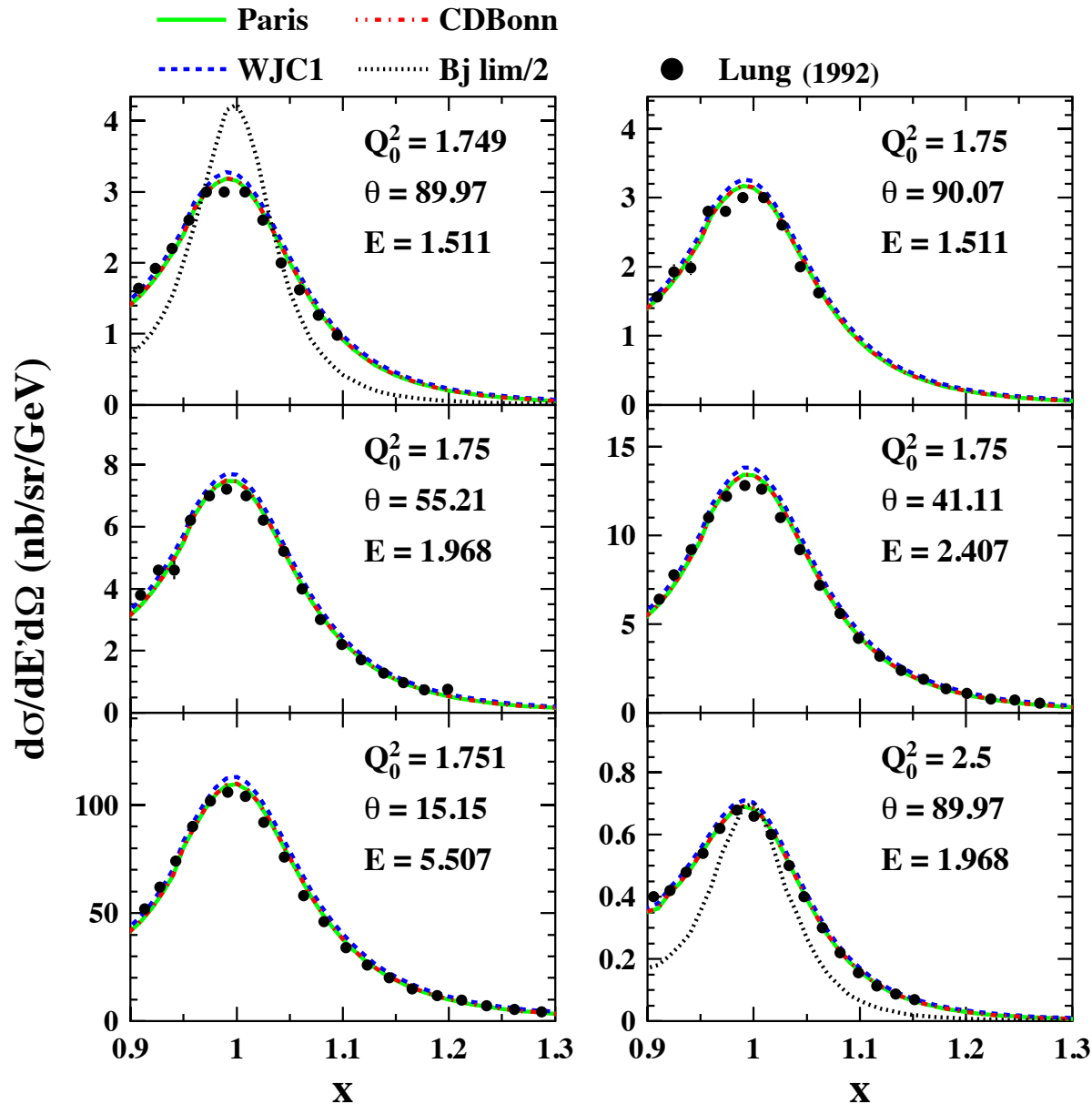
$$\sigma_{(QE)} \sim f_{N/d}(y, \gamma) \times G_N(Q^2)$$

↑  
elastic *eN*  
form factors

*Ethier, Doshi, Malace, WM*  
*arXiv:1402.3910*

# Quasi-elastic *ed* scattering

- Smearing functions can be tested in quasi-elastic (QE) electron–deuteron scattering

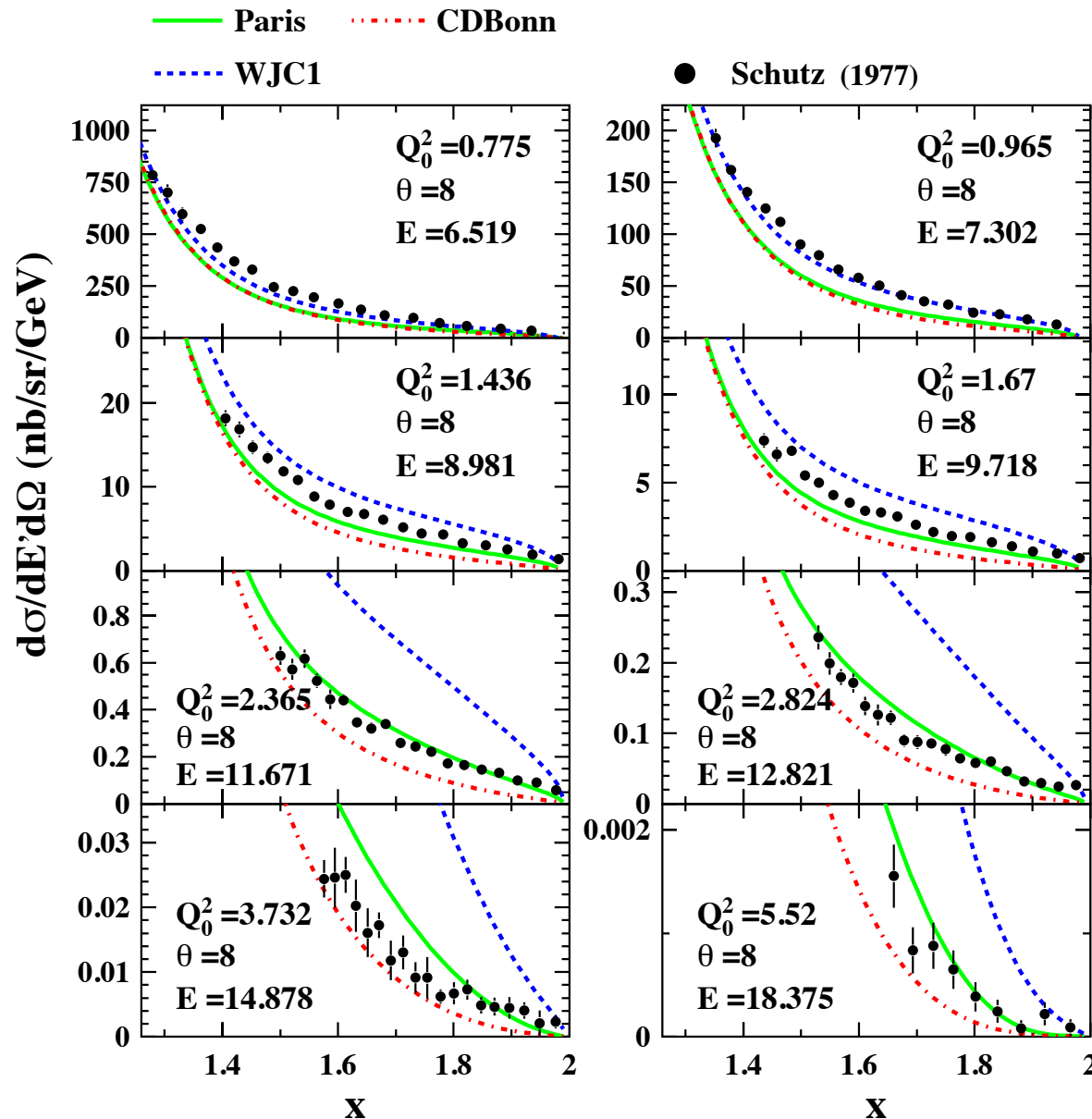


→ importance of correct  $Q^2$  dependence in  $f(y, \gamma)$

*Ethier, Doshi, Malace, WM*  
*arXiv:1402.3910*

# Quasi-elastic *ed* scattering

- Smearing functions can be tested in quasi-elastic (QE) electron–deuteron scattering



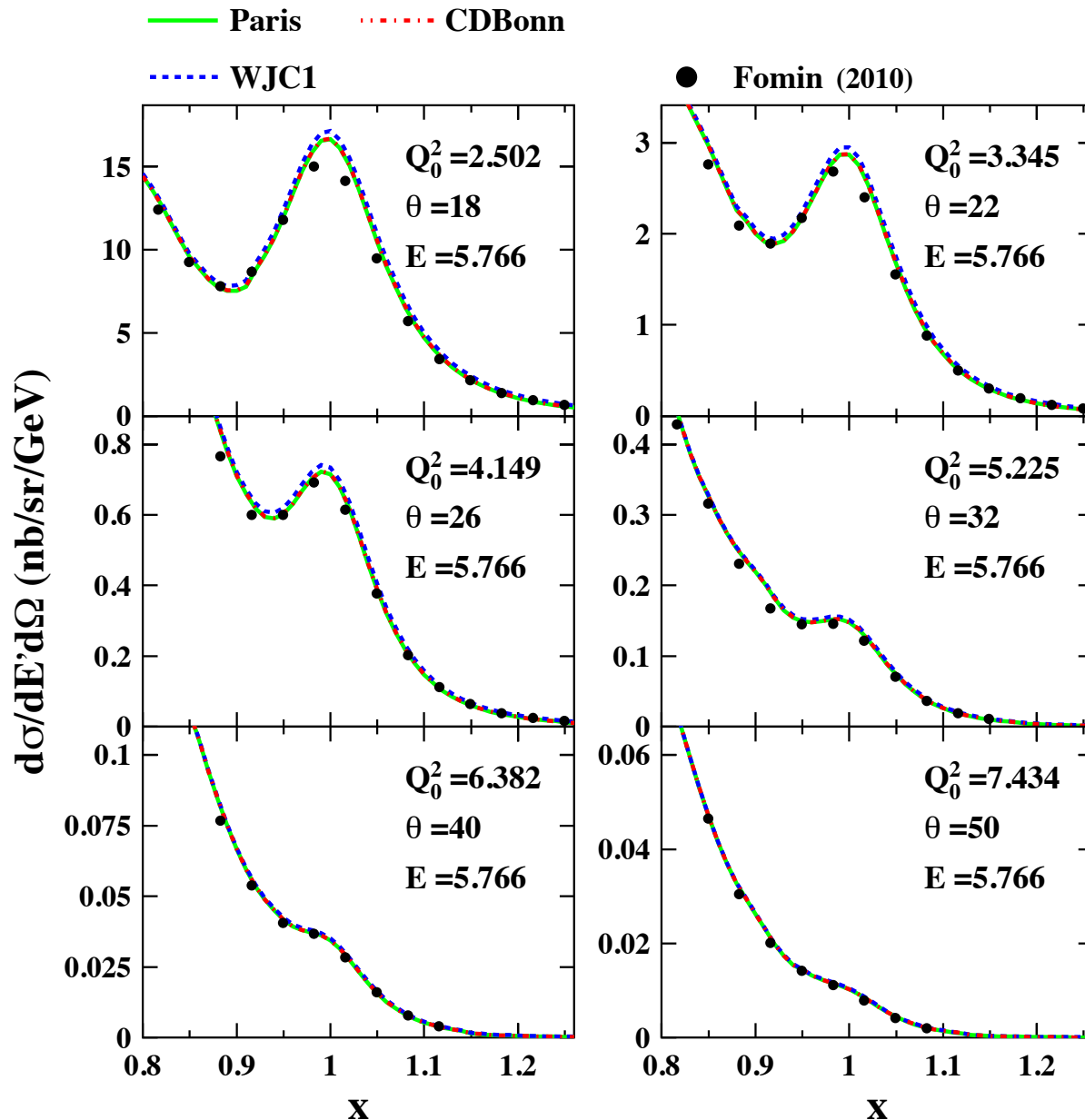
→ importance of correct  $Q^2$  dependence in  $f(y, \gamma)$

→ strong sensitivity to  $d$  wfn. at  $x \gg 1$

Ethier, Doshi, Malace, WM  
arXiv:1402.3910

# Quasi-elastic *ed* scattering

- Smearing functions can be tested in quasi-elastic (QE) electron–deuteron scattering



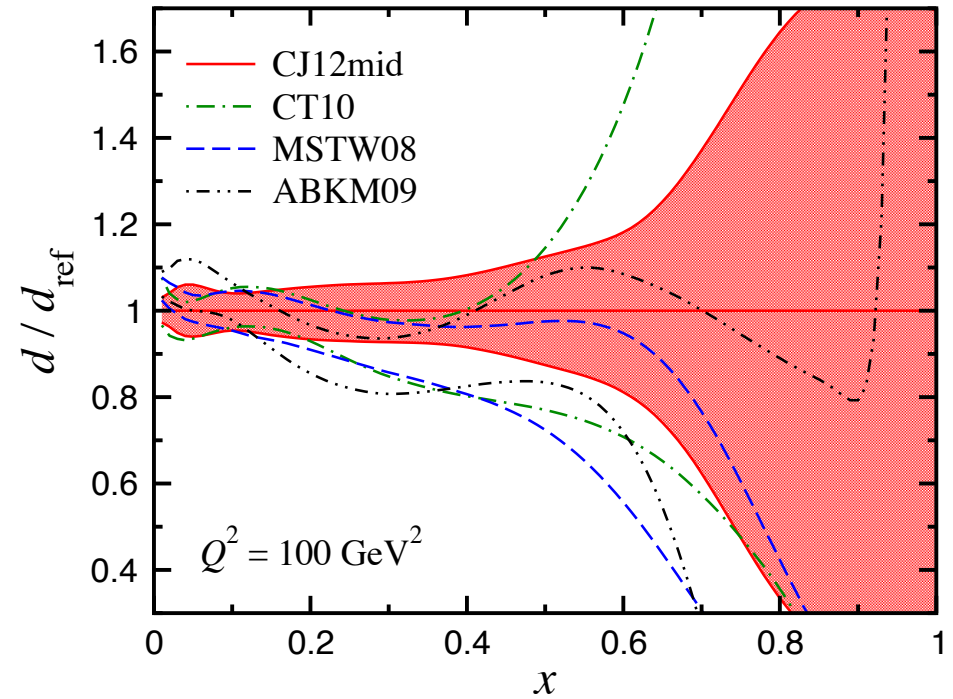
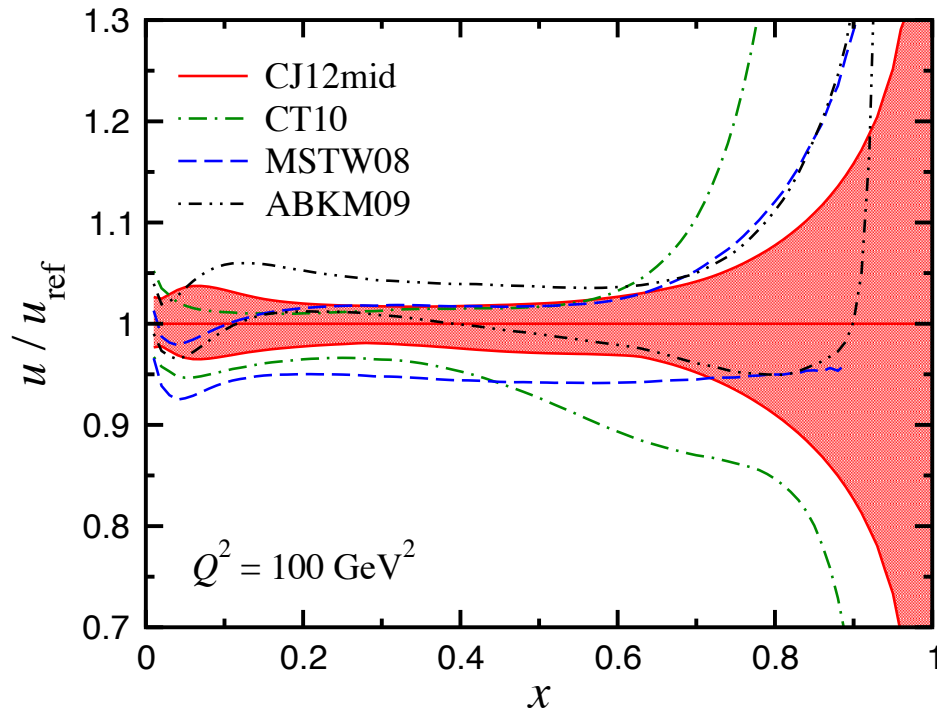
→ importance of correct  $Q^2$  dependence in  $f(y, \gamma)$

→ strong sensitivity to  $d$  wfn. at  $x \gg 1$

→ excellent agreement with data near QE peak (~ 2,000 data points)

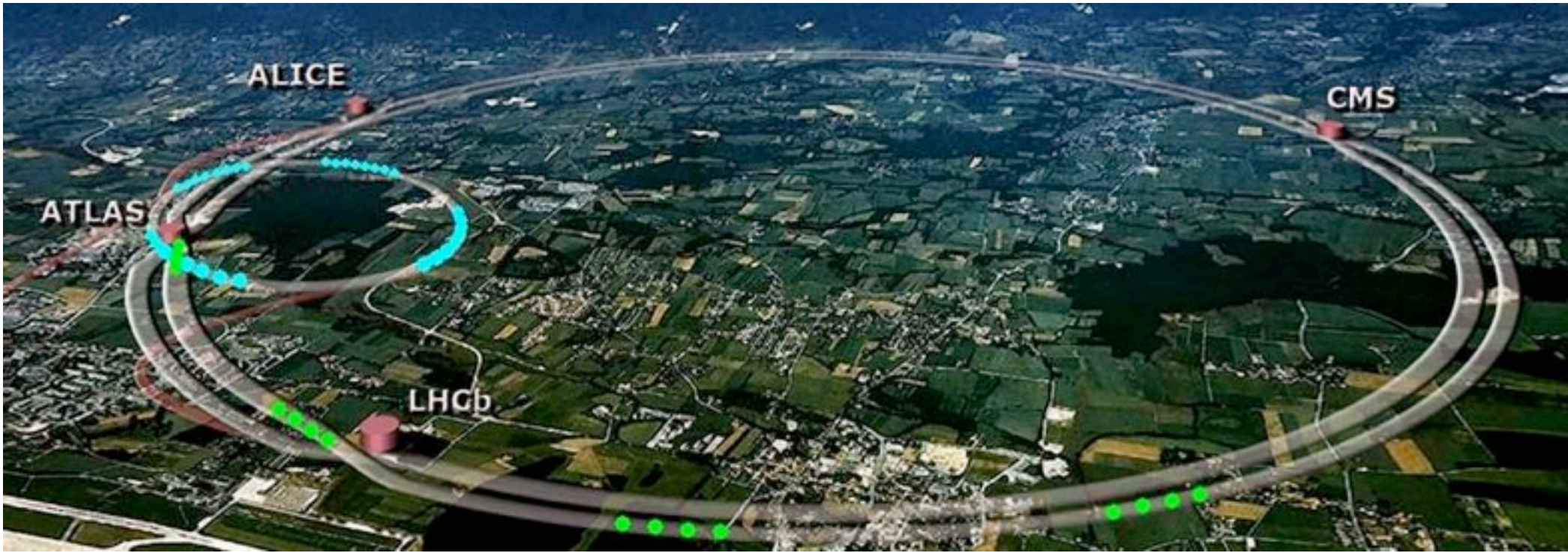
*Ethier, Doshi, Malace, WM*  
*arXiv:1402.3910*

# Comparison with other PDFs fits

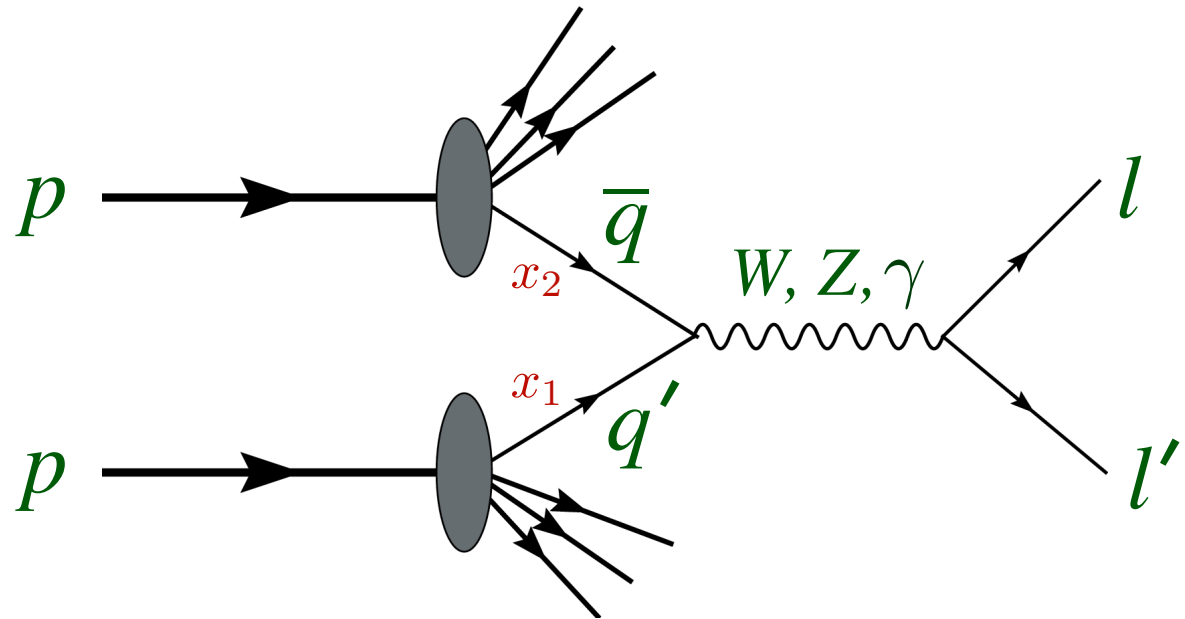


- *increase* in PDF error from more realistic treatment of nuclear corrections
- *reduction* of error from larger database

# Implications for colliders



lepton pair production  
in  $pp$  collisions





# Implications for colliders

- Large- $x$  PDF uncertainties affect observables at large rapidity  $y$ , with

$$y = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \rightarrow x_{1,2} = \frac{M}{\sqrt{s}} e^{\pm y}$$

e.g.  $W^{\pm}$  asymmetry

$$A_W(y) = \frac{\sigma_{W^+} - \sigma_{W^-}}{\sigma_{W^+} + \sigma_{W^-}} \approx \frac{d(x_2)/u(x_2) - d(x_1)/u(x_1)}{d(x_2)/u(x_2) + d(x_1)/u(x_1)} \quad [x_1 \gg x_2]$$

where

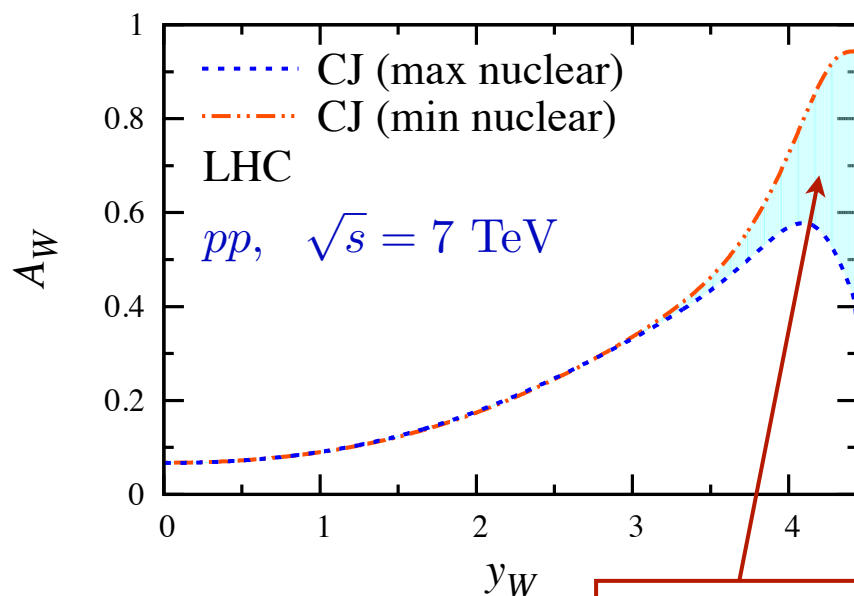
$$\sigma_{W^+} \equiv \frac{d\sigma}{dy}(pp \rightarrow W^+ X) = \frac{2\pi G_F}{3\sqrt{2}} x_1 x_2 (u(x_1)\bar{d}(x_2) + \dots)$$

# Implications for colliders

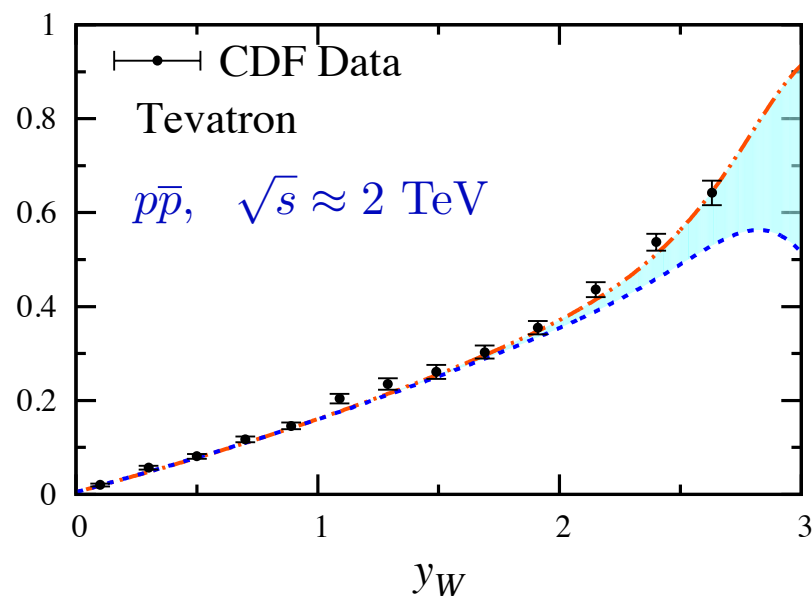
- Large- $x$  PDF uncertainties affect observables at large rapidity  $y$ , with

$$y = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \rightarrow x_{1,2} = \frac{M}{\sqrt{s}} e^{\pm y}$$

e.g.  $W^\pm$  asymmetry



sensitive to  
 $d$  at high  $x$

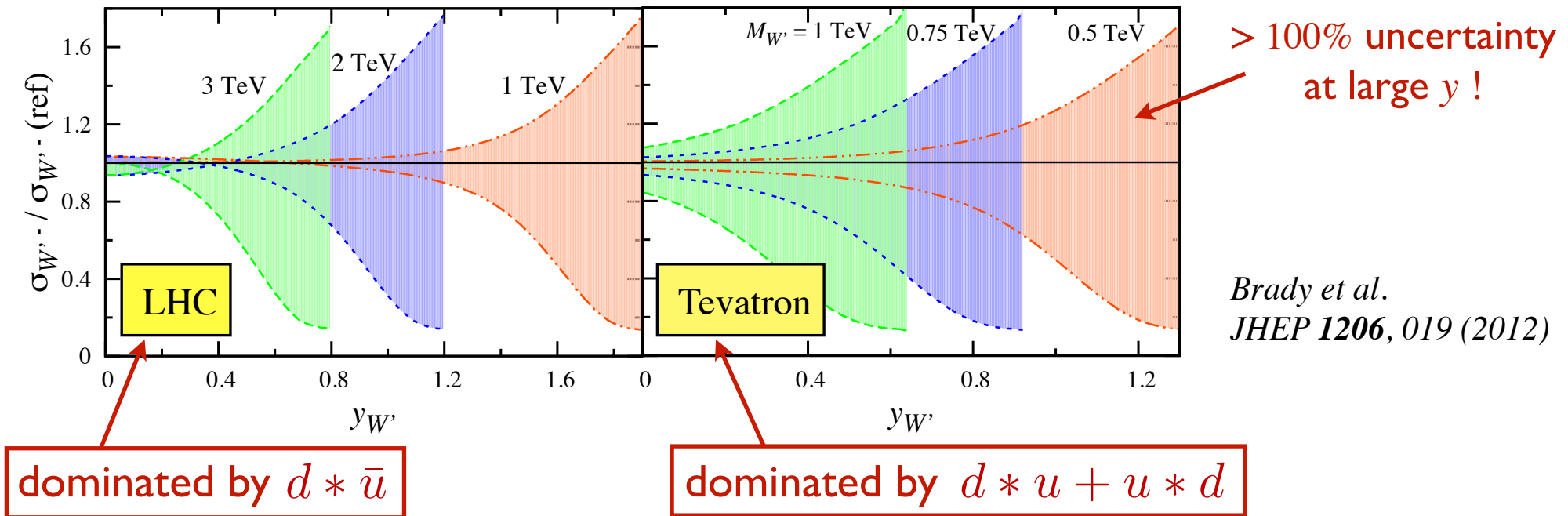


Brady, Accardi, WM, Owens  
*JHEP* **1206**, 019 (2012)

# Implications for colliders

- Uncertainty in  $d$ -quark feeds into larger uncertainty in  $gluon$  at high  $x$  (relevant for LHC physics)

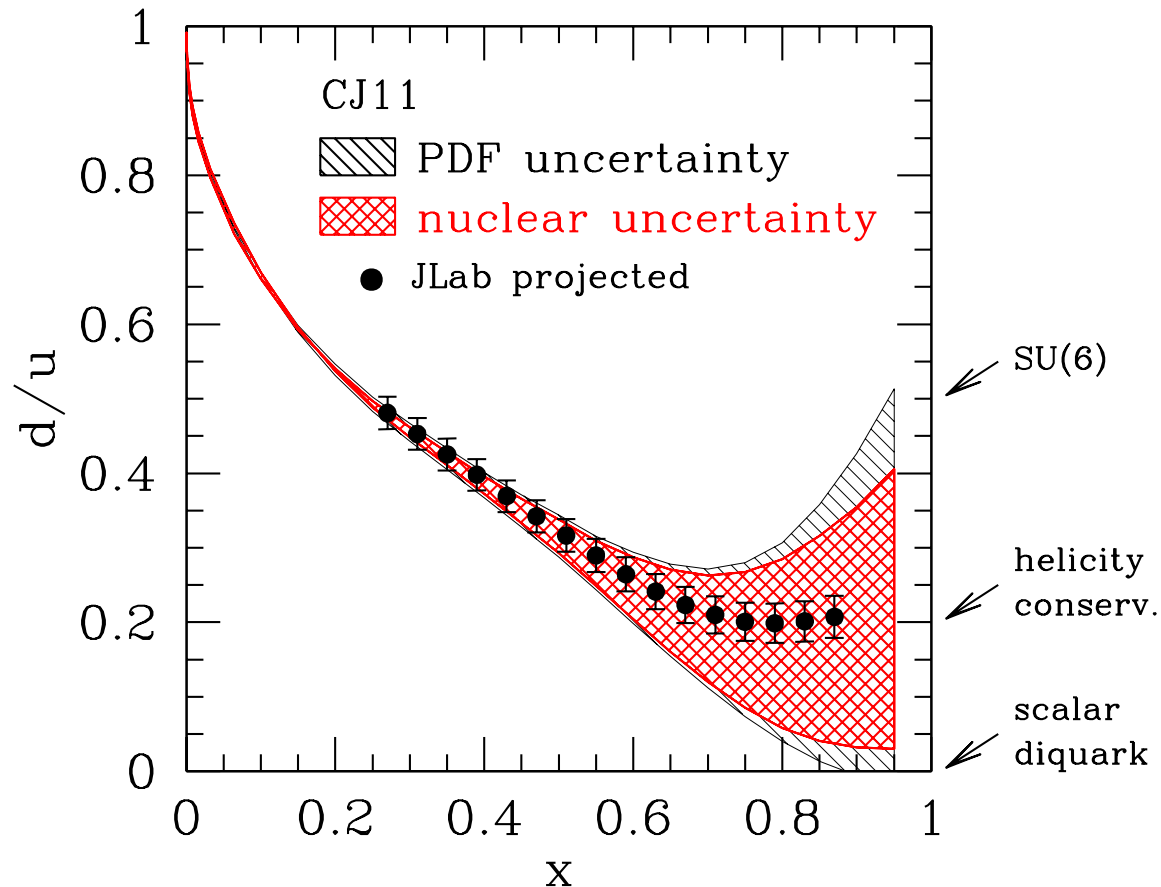
## heavy $W'^-$ production



→ observation of new physics signals requires accurate determination of QCD backgrounds → depend on PDFs!

# JLab 12 GeV plans

- Several planned experiments at JLab with 12 GeV will measure  $d/u$  to  $x \sim 0.85$  with minimal nuclear corrections
  - SIDIS from D with slow backward proton (“BoNuS”); inclusive  ${}^3\text{He} / {}^3\text{H}$  ratio; and PVDIS from proton



*Accardi et al., PRD 84, 014008 (2011)*

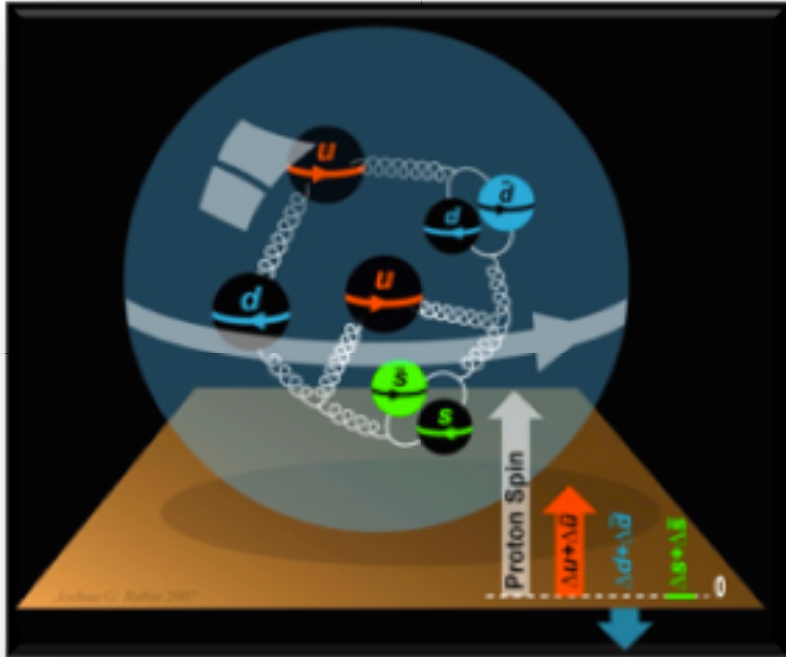
# Spin-dependent PDFs

P. Jimenez-Delgado, A. Accardi, WM  
H. Avakian, B. Sawatzky, ...

**“JAM” PDFs:** *arXiv:1310.3734, to appear PRD (2014)*

<http://www.jlab.org/JAM>

# Nucleon spin structure

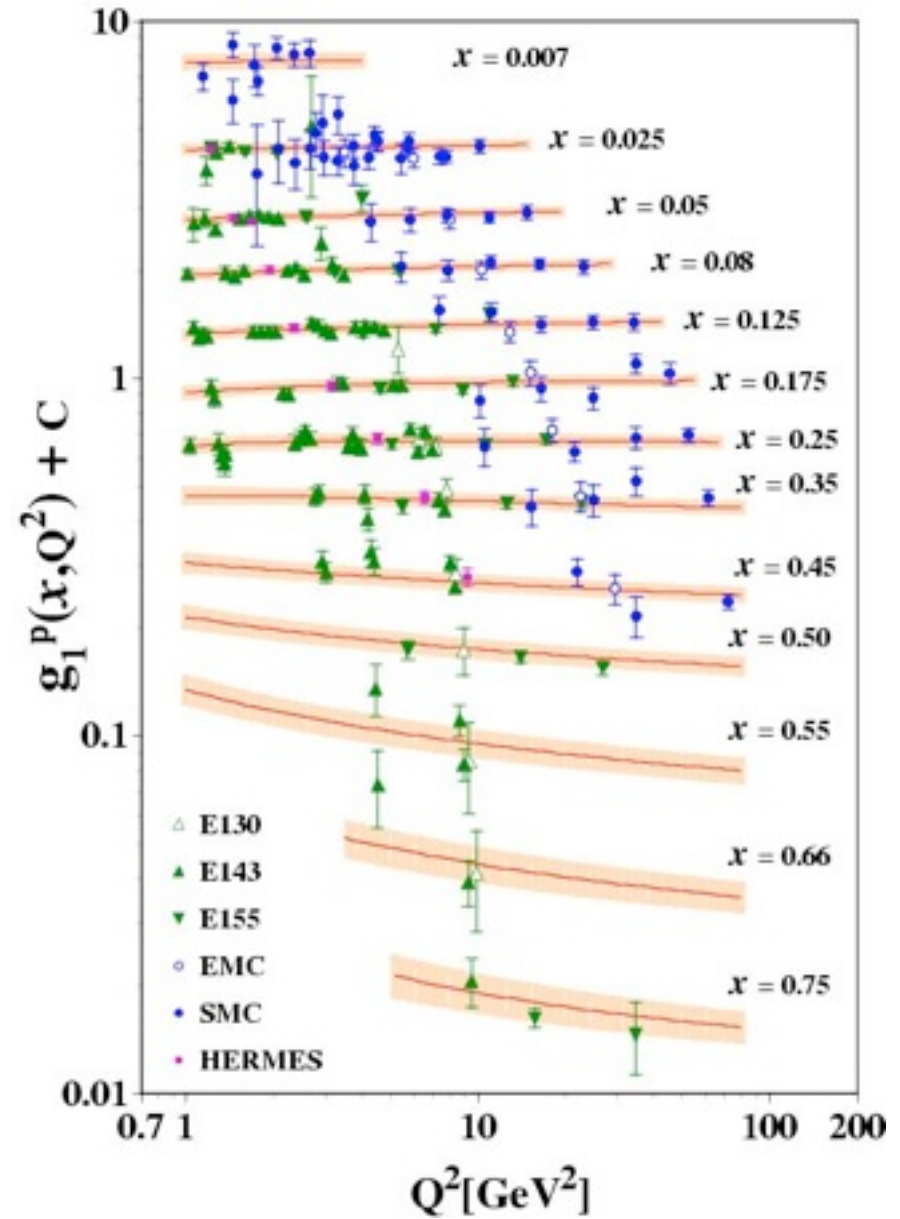


$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + L_q + \Delta G + L_g$$

$$\Delta \Sigma \sim 0.25 \quad (\text{DIS})$$

$$\Delta G \ll 1 \quad (\text{DIS} + pp)$$

$$L_{q,g} = ? \quad (\text{GPDs})$$



→ fewer data *cf.* unpolarised

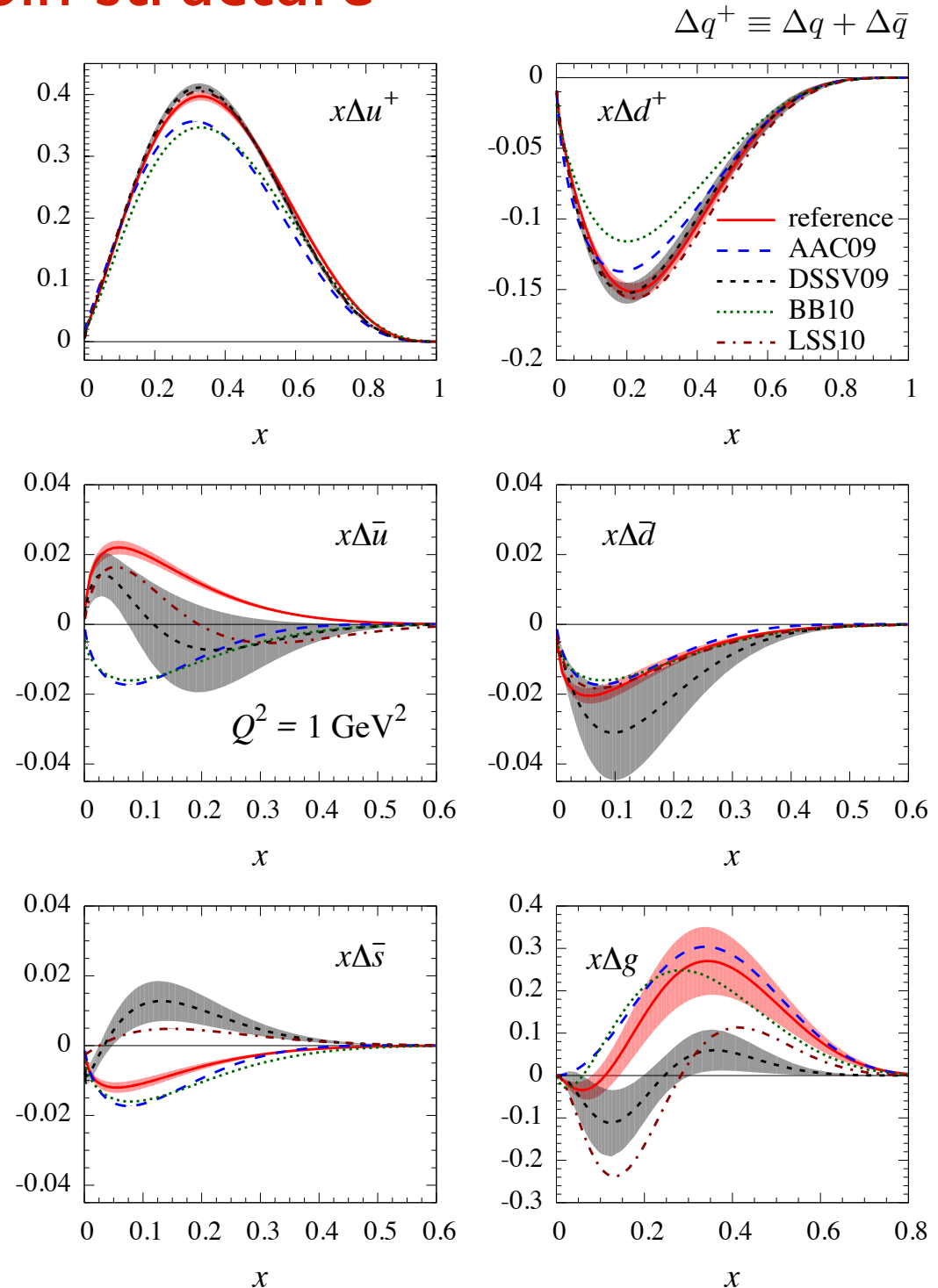
# Nucleon spin structure

- Global PDF analyses performed by several groups
  - focus on small- $x$  region (sum rules)

- Data from many experiments at JLab recently collected at low  $Q^2$  and  $W$

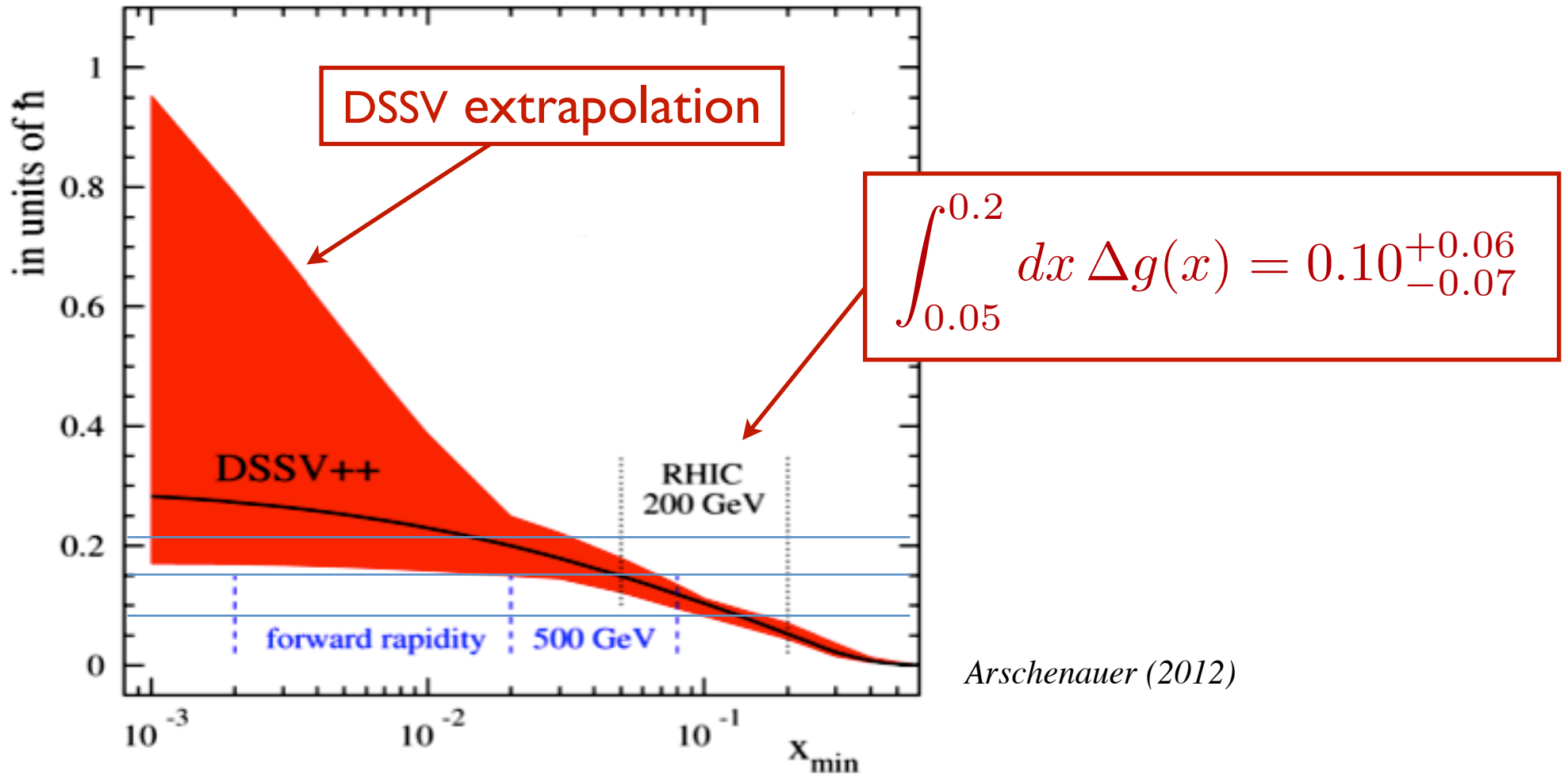
- need for synthesis of results (current & future) from Halls A, B & C, including finite- $Q^2$  & nuclear corrections

- JAM global analysis



# Nucleon spin structure

- Recent RHIC  $pp$  data claimed to imply large gluon polarisation



→ important to confirm claim through independent global analysis



# JAM database

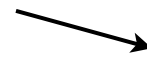
- Complete collection of world's inclusive polarised DIS data (interactive database at <http://www.jlab.org/JAM>)

$$Q^2 > 1 \text{ GeV}^2, \quad W^2 > 3.5 \text{ GeV}^2$$

- Fit experimental asymmetries (longitudinal & transverse) rather than derived  $g_1$  and  $g_2$  structure functions

$$g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \Delta q(x, Q^2)$$

several high-statistics experiments still being analysed



experiment	reference	observable	target	$N_{\text{data}}$	$\chi^2(\text{LT})/N_{\text{dat}}$	$\chi^2(\text{JAM})/N_{\text{dat}}$
EMC	[1]	$A_1$	p	10	0.42	0.39
SMC	[30]	$A_1$	p	12	0.36	0.36
	[30]	$A_1$	d	12	1.59	1.66
	[31]	$A_1$	p	8	1.37	1.35
	[31]	$A_1$	d	8	0.54	0.56
COMPASS	[32]	$A_1$	p	15	0.95	0.97
	[33]	$A_1$	d	15	0.57	0.51
SLAC E80/E130	[34]	$A_{  }$	p	23	0.52	0.54
SLAC E142	[35]	$A_1$	$^3\text{He}$	8	0.58	0.70
	[35]	$A_2$	$^3\text{He}$	8	0.70	0.70
SLAC E143	[36]	$A_{  }$	p	85	0.85	0.81
	[36]	$A_{\perp}$	p	48	0.95	0.91
	[36]	$A_{  }$	d	85	1.05	0.85
	[36]	$A_{\perp}$	d	48	0.92	0.91
SLAC E154	[37]	$A_{  }$	$^3\text{He}$	18	0.43	0.42
	[37]	$A_{\perp}$	$^3\text{He}$	18	1.00	1.00
SLAC E155	[38]	$A_{  }$	p	73	1.00	0.92
	[38, 39]	$A_{\perp}$	p	66	1.00	0.96
	[40]	$A_{  }$	d	73	0.98	0.97
	[39, 40]	$A_{\perp}$	d	66	1.51	1.49
SLAC E155x	[41]	$\bar{A}_{\perp}$	p	117	2.17	1.64
	[41]	$\bar{A}_{\perp}$	d	117	0.90	0.84
HERMES	[42]	$A_{  }$	p	37	0.38	0.39
	[42]	$A_{  }$	d	37	0.86	0.85
	[43]	$A_1$	"n"	9	0.29	0.30
	[44]	$A_2$	p	20	1.07	1.16
JLab E99-117	[45]	$A_{  }$	$^3\text{He}$	3	0.62	0.06
	[45]	$A_{\perp}$	$^3\text{He}$	3	1.08	0.87
COMPASS	[49]	$\Delta g/g$	p	1	5.27	2.71
total				1043	1.07	0.98
JLab E97-103*	[46]	$A_{  }$	$^3\text{He}$	2	—	—
	[46]	$A_{\perp}$	$^3\text{He}$	2	—	—
JLab EG1b*	[48]	$A_1$	p	766	—	—
(prelim.)	[48]	$A_1$	d	767	—	—

# JAM database

- Complete collection of world's inclusive polarised DIS data (interactive database at <http://www.jlab.org/JAM>)

$$Q^2 > 1 \text{ GeV}^2, \quad W^2 > 3.5 \text{ GeV}^2$$

- Fit experimental asymmetries (longitudinal & transverse) rather than derived  $g_1$  and  $g_2$  structure functions

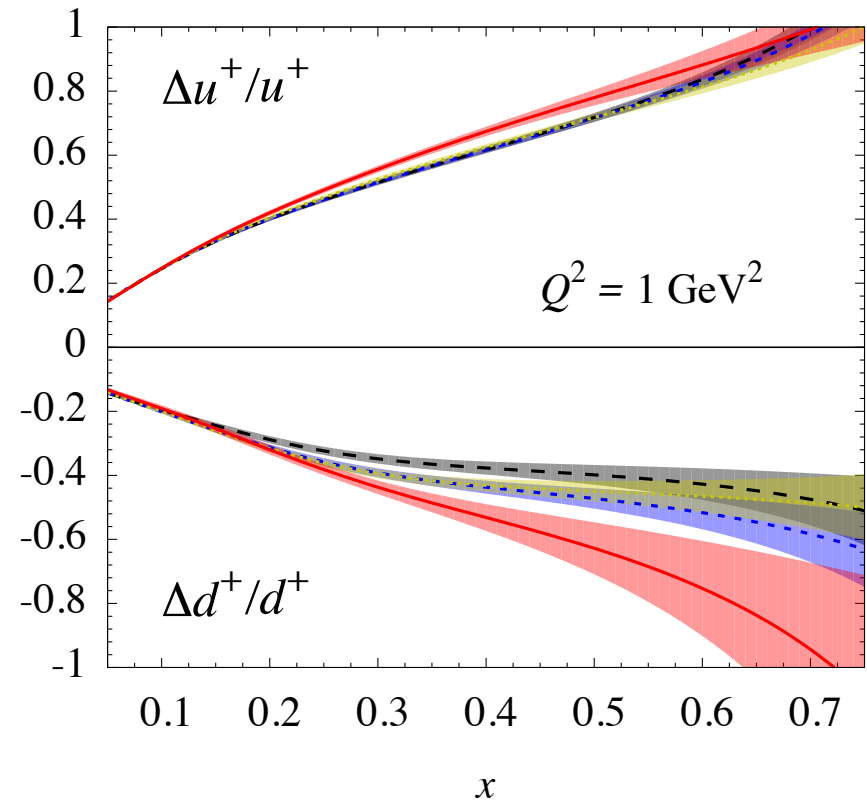
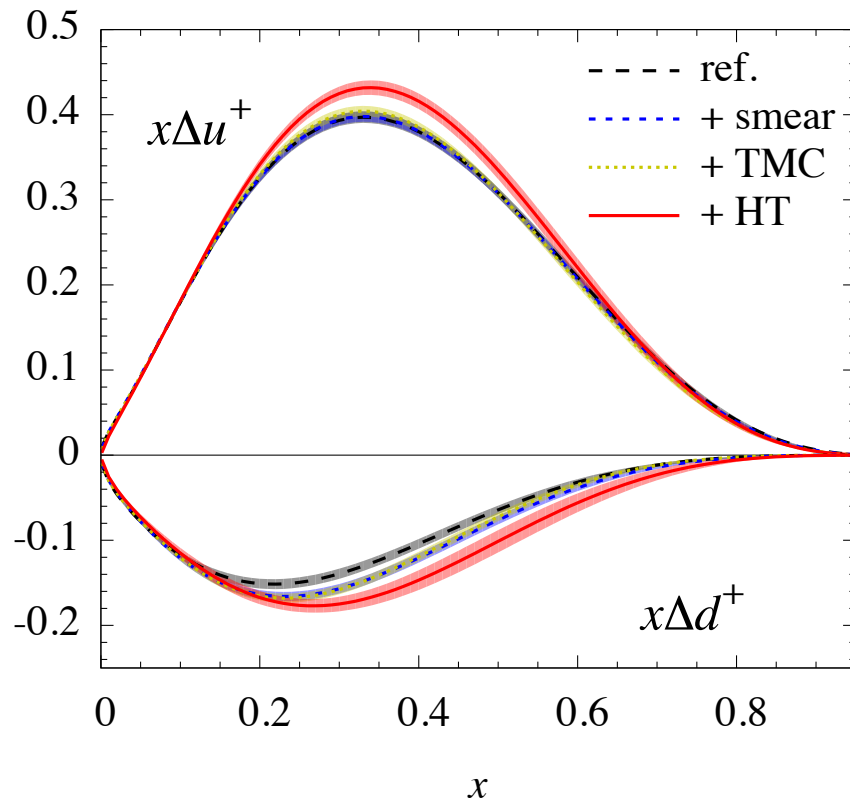
$$A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = D(A_1 + \eta A_2)$$

$$A_{\perp} = \frac{\sigma^{\uparrow\Rightarrow} - \sigma^{\uparrow\Leftarrow}}{\sigma^{\uparrow\Rightarrow} + \sigma^{\uparrow\Leftarrow}} = d(A_2 - \xi A_1)$$

$$A_1 = \frac{(g_1 - \gamma^2 g_2)}{F_1}, \quad A_2 = \gamma \frac{(g_1 + g_2)}{F_1}$$

experiment	reference	observable	target	$N_{\text{data}}$	$\chi^2(\text{LT})/N_{\text{dat}}$	$\chi^2(\text{JAM})/N_{\text{dat}}$
EMC	[1]	$A_{\parallel}$	p	10	0.42	0.39
SMC	[30]	$A_{\parallel}$	p	12	0.36	0.36
	[30]	$A_{\parallel}$	d	12	1.59	1.66
	[31]	$A_{\parallel}$	p	8	1.37	1.35
	[31]	$A_{\parallel}$	d	8	0.54	0.56
COMPASS	[32]	$A_{\parallel}$	p	15	0.95	0.97
	[33]	$A_{\parallel}$	d	15	0.57	0.51
SLAC E80/E130	[34]	$A_{\parallel}$	p	23	0.52	0.54
SLAC E142	[35]	$A_{\parallel}$	$^3\text{He}$	8	0.58	0.70
	[35]	$A_2$	$^3\text{He}$	8	0.70	0.70
SLAC E143	[36]	$A_{\parallel}$	p	85	0.85	0.81
	[36]	$A_{\perp}$	p	48	0.95	0.91
	[36]	$A_{\parallel}$	d	85	1.05	0.85
	[36]	$A_{\perp}$	d	48	0.92	0.91
SLAC E154	[37]	$A_{\parallel}$	$^3\text{He}$	18	0.43	0.42
	[37]	$A_{\perp}$	$^3\text{He}$	18	1.00	1.00
SLAC E155	[38]	$A_{\parallel}$	p	73	1.00	0.92
	[38, 39]	$A_{\perp}$	p	66	1.00	0.96
	[40]	$A_{\parallel}$	d	73	0.98	0.97
	[39, 40]	$A_{\perp}$	d	66	1.51	1.49
SLAC E155x	[41]	$\bar{A}_{\perp}$	p	117	2.17	1.64
	[41]	$\bar{A}_{\perp}$	d	117	0.90	0.84
HERMES	[42]	$A_{\parallel}$	p	37	0.38	0.39
	[42]	$A_{\parallel}$	d	37	0.86	0.85
	[43]	$A_{\parallel}$	"n"	9	0.29	0.30
	[44]	$A_2$	p	20	1.07	1.16
JLab E99-117	[45]	$A_{\parallel}$	$^3\text{He}$	3	0.62	0.06
	[45]	$A_{\perp}$	$^3\text{He}$	3	1.08	0.87
COMPASS	[49]	$\Delta g/g$	p	1	5.27	2.71
total				1043	1.07	0.98
JLab E97-103*	[46]	$A_{\parallel}$	$^3\text{He}$	2	—	—
	[46]	$A_{\perp}$	$^3\text{He}$	2	—	—
JLab EG1b*	[48]	$A_{\parallel}$	p	766	—	—
(prelim.)	[48]	$A_{\parallel}$	d	767	—	—

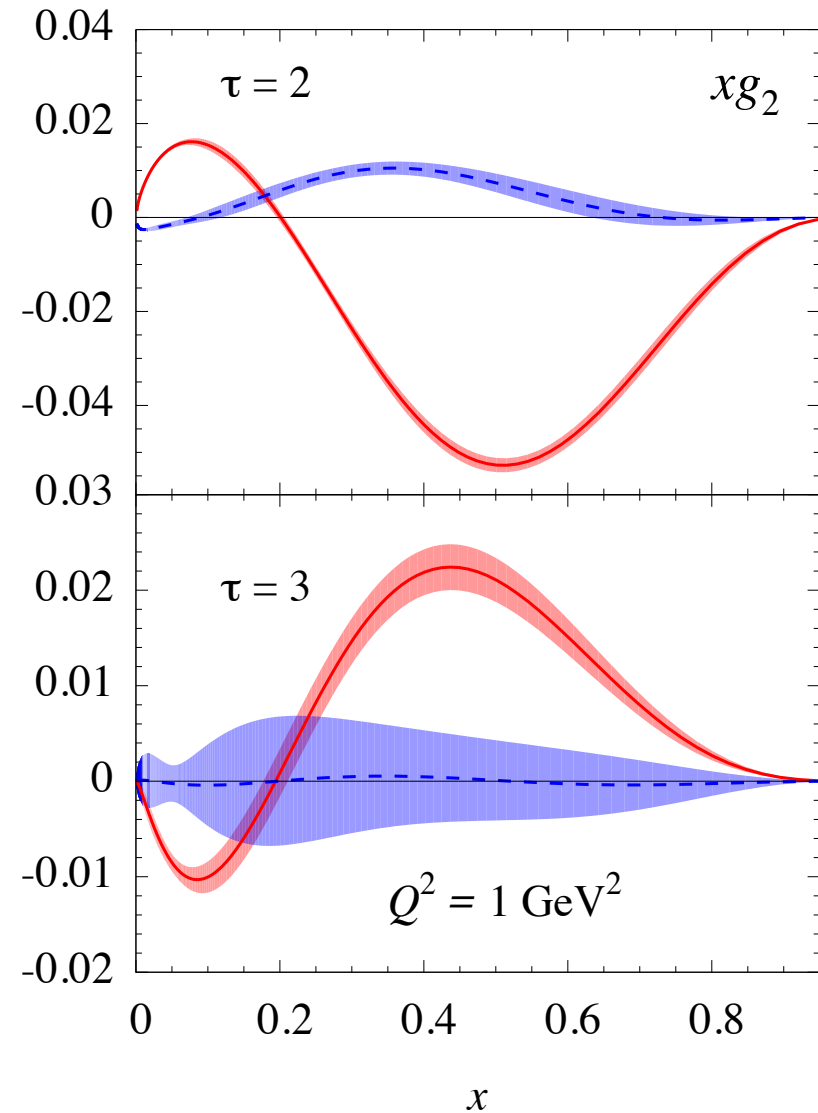
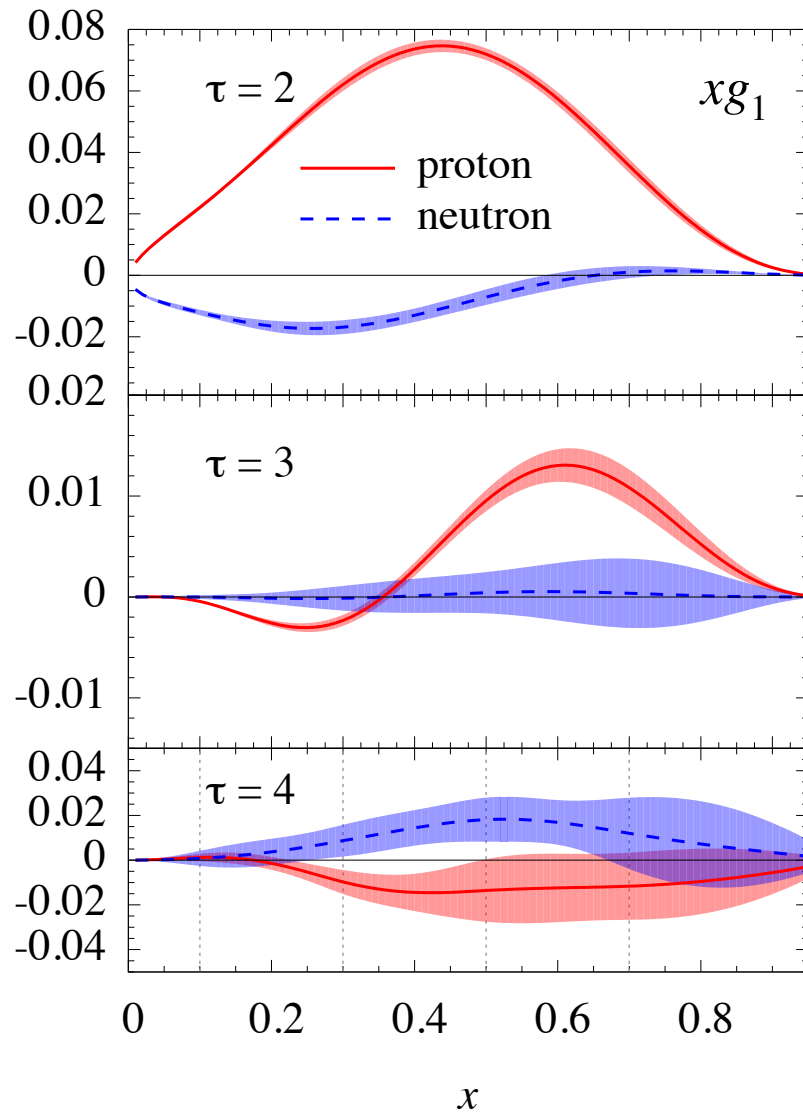
# JAM PDFs



→ significantly larger  $\Delta d$  at  $x \gtrsim 0.3$

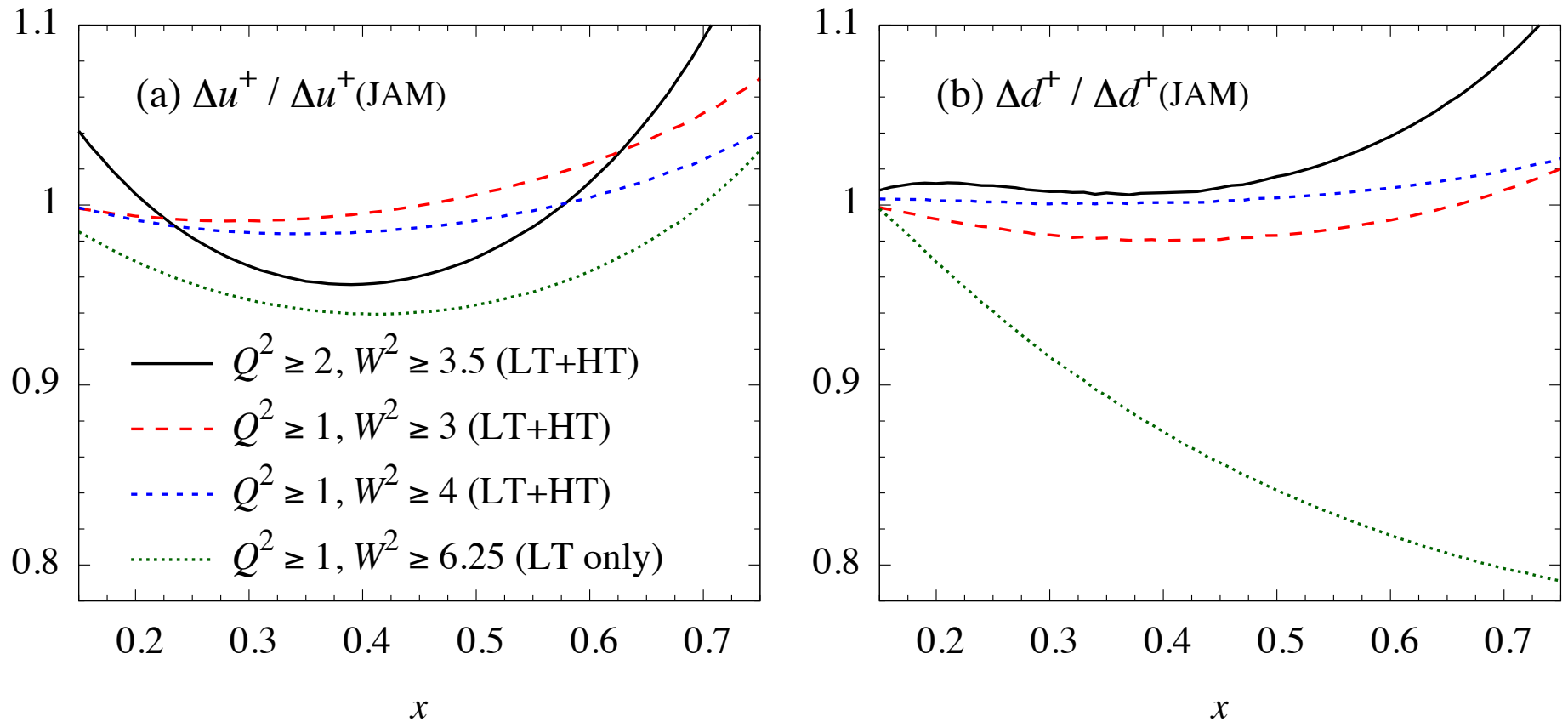
→ greatest effect on polarised PDFs from higher twist corrections

# JAM PDFs



→ important  $\tau = 3$  contributions to proton  $g_1$ ,  $g_2$   
and  $\tau = 4$  contributions to neutron  $g_1$

# JAM PDFs



- PDFs relatively stable w.r.t. cuts in  $Q^2$  and  $W$  (50% of all data points in  $Q^2 < 2 \text{ GeV}^2$  region)
- significant reduction in  $\Delta d$  with strong  $W$  cut (to avoid HT corrections) – cf. “NNPDF” analysis

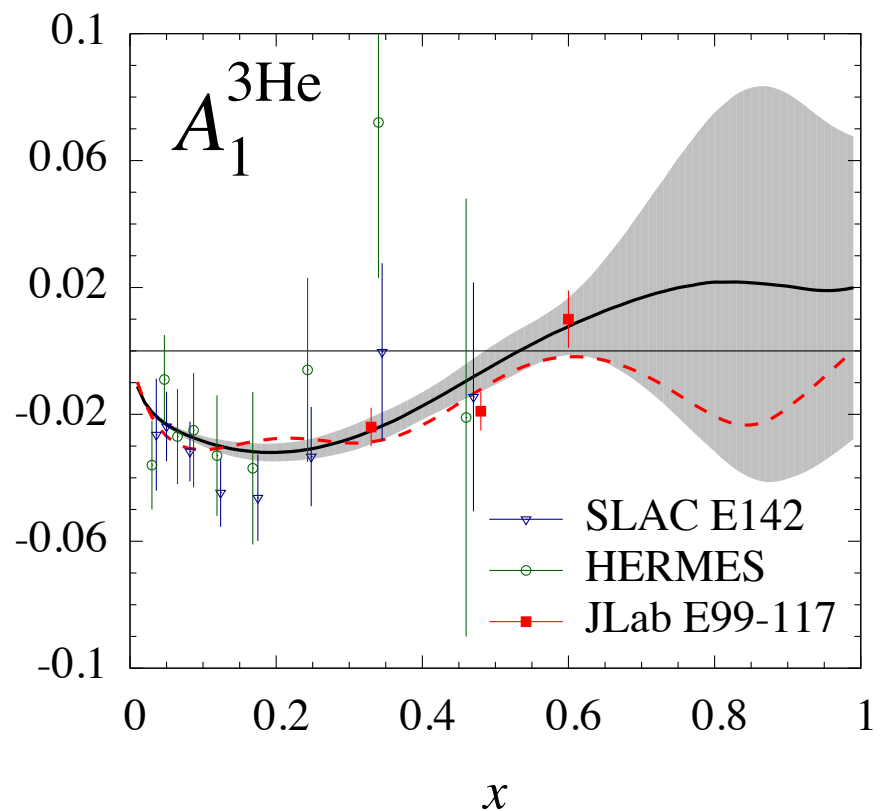
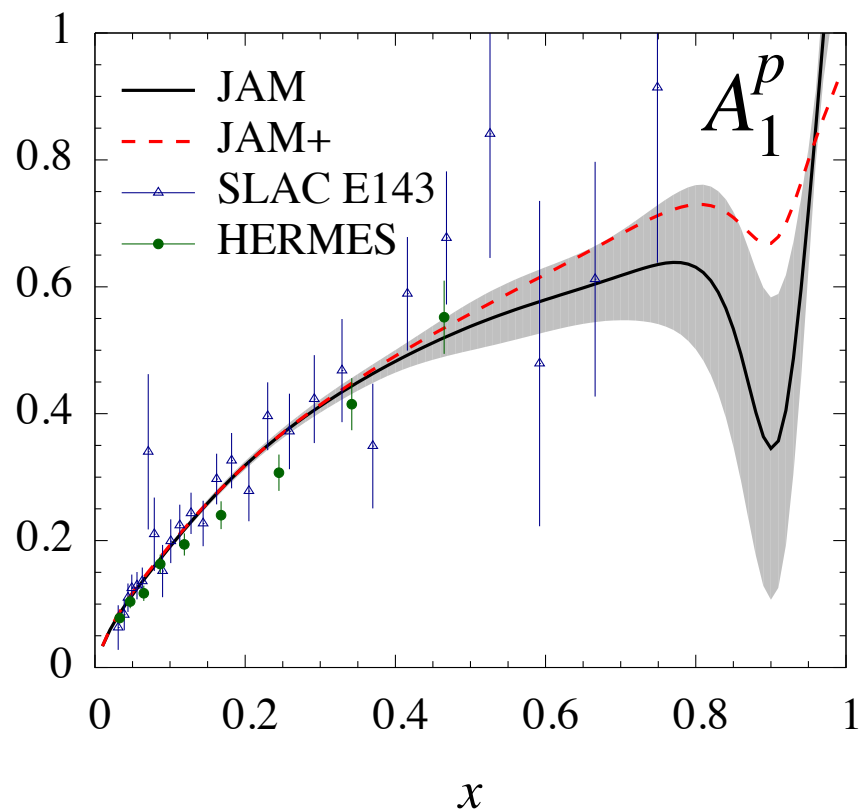
## PDFs at large $x$

- Ratio of polarised to unpolarised PDFs even more sensitive to nonperturbative quark-gluon dynamics in nucleon

- $\Delta u/u \rightarrow 2/3$   
 $\Delta d/d \rightarrow -1/3$  SU(6) symmetry
- $\Delta u/u \rightarrow 1$   
 $\Delta d/d \rightarrow -1/3$   $S = 0$   $qq$  dominance
- $\Delta u/u \rightarrow 1$   
 $\Delta d/d \rightarrow 1$   $S_z = 0$   $qq$  dominance (pQCD)  
or local duality

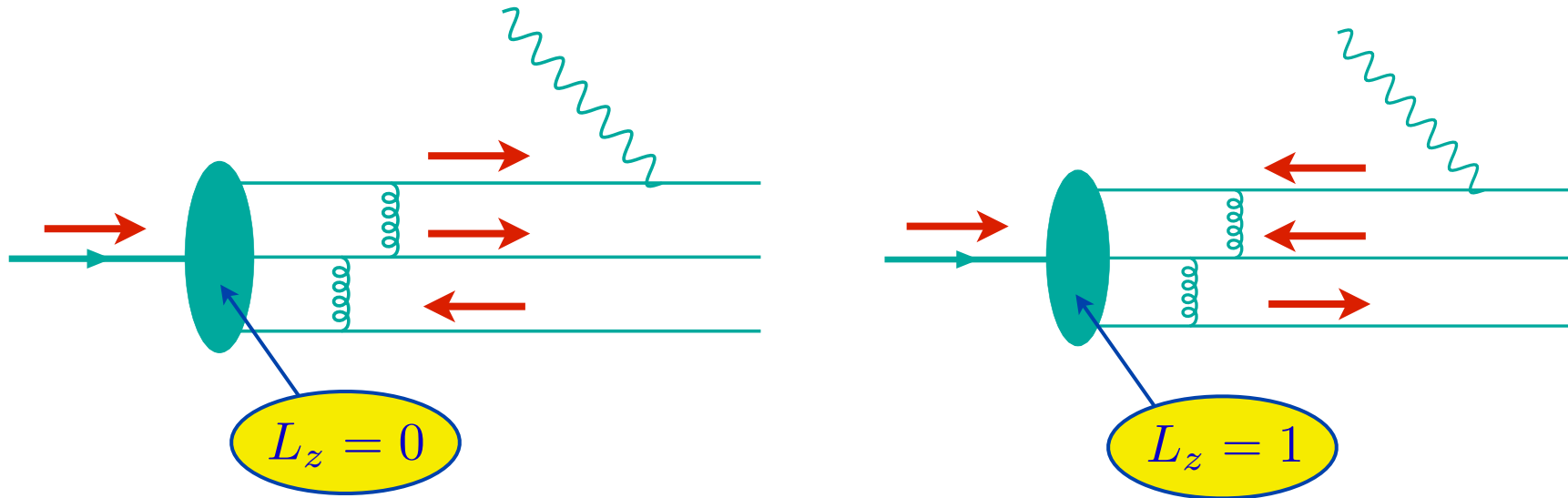
# PDFs at large $x$

- Current data cannot discriminate between different  $x \rightarrow 1$  behaviours
- Impose  $x \rightarrow 1$  pQCD constraint on PDFs “by hand”  
→ “JAM+” fit



# Orbital angular momentum

- Earlier analysis suggested need for additional nonzero OAM ( $L_z = 1$ ) component in nucleon wave function



→ leading  $(1-x)^3$  behaviour from  $L_z = 0$  component

→  $L_z = 1$  gives additional  $\log^2(1-x)$  enhancement of  $q^\downarrow$

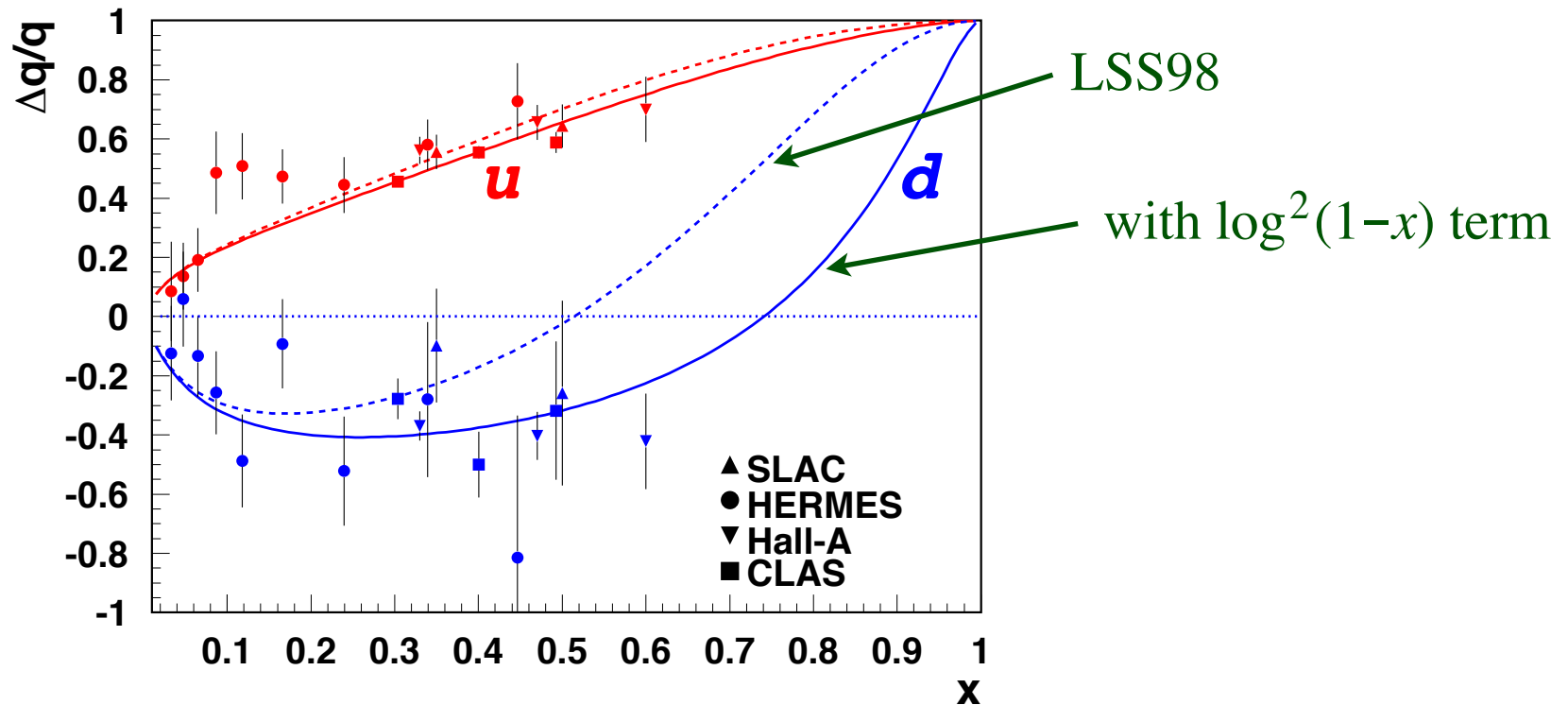
$$q^\downarrow \sim (1-x)^5 \log^2(1-x)$$

*Avakian, Brodsky, Deur, Yuan  
PRL 99, 082001 (2007)*



# Orbital angular momentum

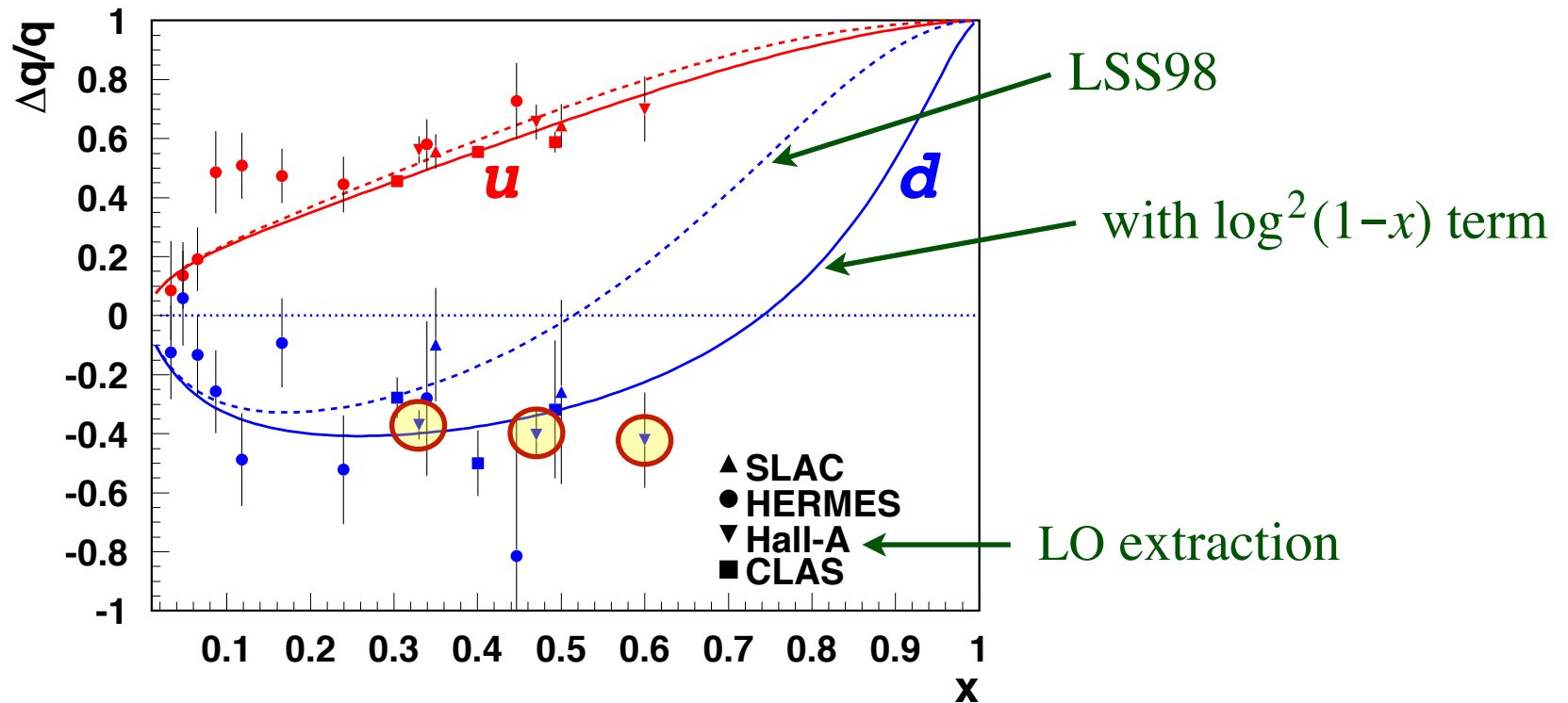
- Earlier analysis suggested need for additional nonzero OAM ( $L_z = 1$ ) component in nucleon wave function



*Avakian, Brodsky, Deur, Yuan  
PRL 99, 082001 (2007)*

# Orbital angular momentum

- Earlier analysis suggested need for additional nonzero OAM ( $L_z = 1$ ) component in nucleon wave function

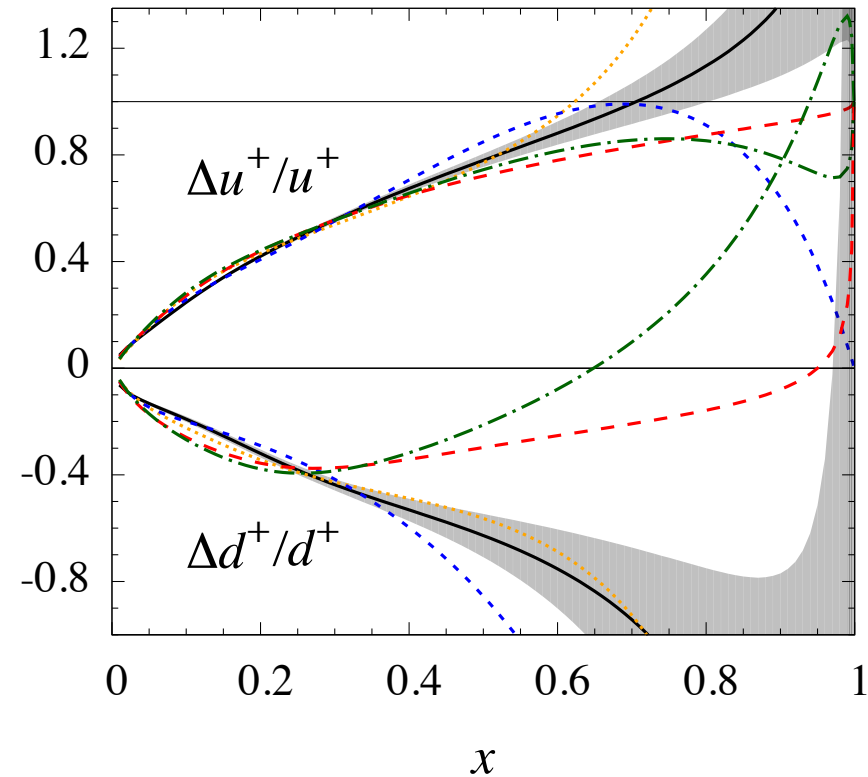
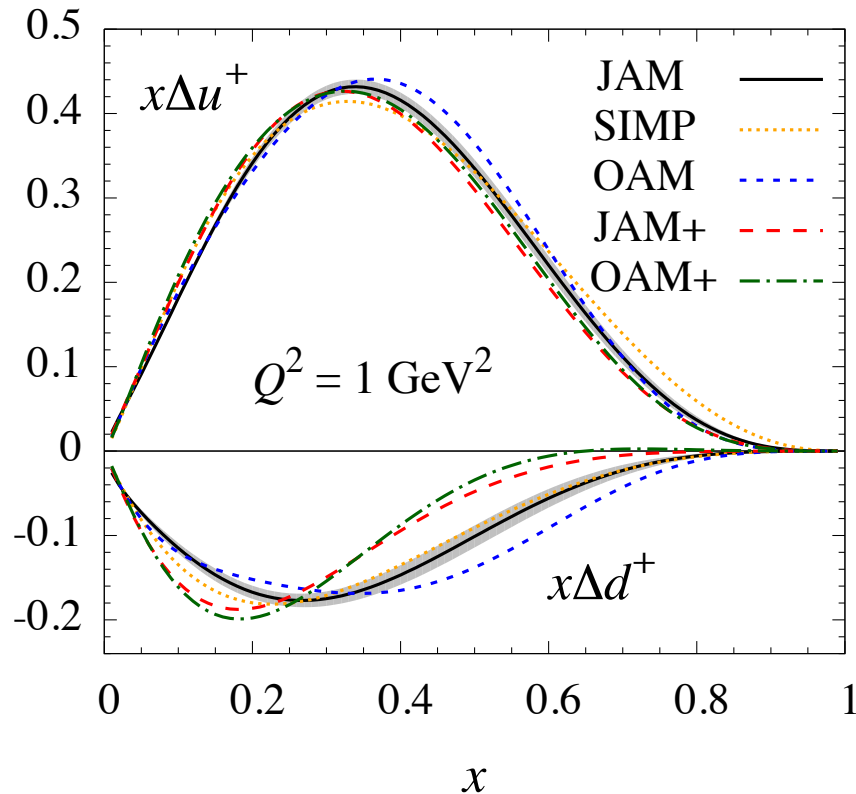


→  $L_z = 1$  term needed to delay  $\Delta d$  turnover until larger  $x$

*Avakian, Brodsky, Deur, Yuan  
PRL 99, 082001 (2007)*

# Orbital angular momentum

- Global JAM & JAM+ fits can accommodate data *without* need for additional  $L_z = 1$  terms



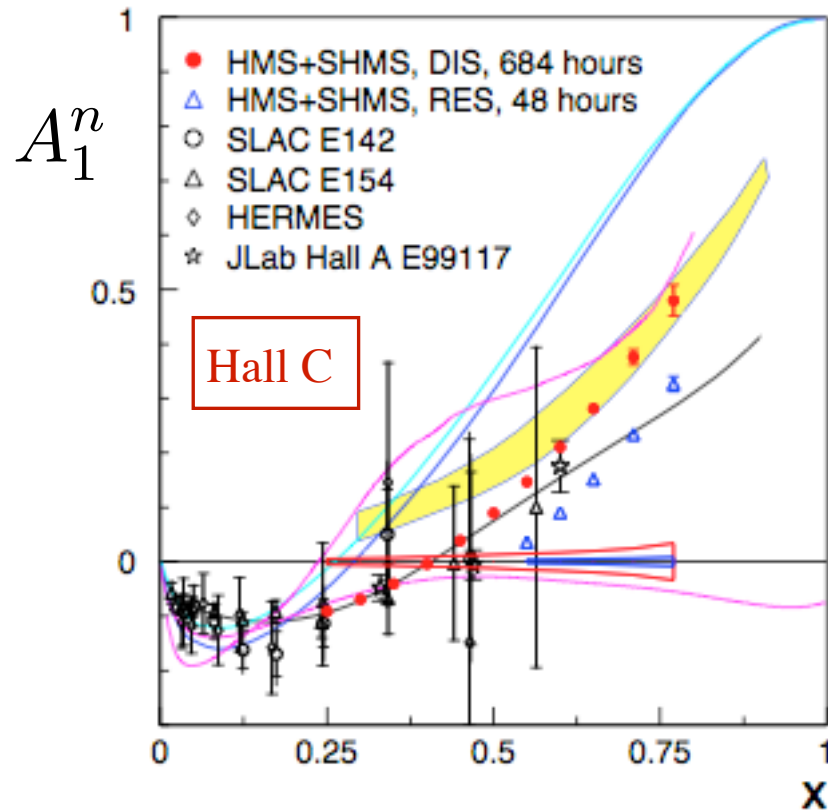
→ “OAM” and “OAM+” fits use

$$x\Delta f = Nx^\alpha(1-x)^\beta + N'x^\alpha(1-x)^5 \log^2(1-x)$$

→ can also accommodate data, with similar overall  $\chi^2$

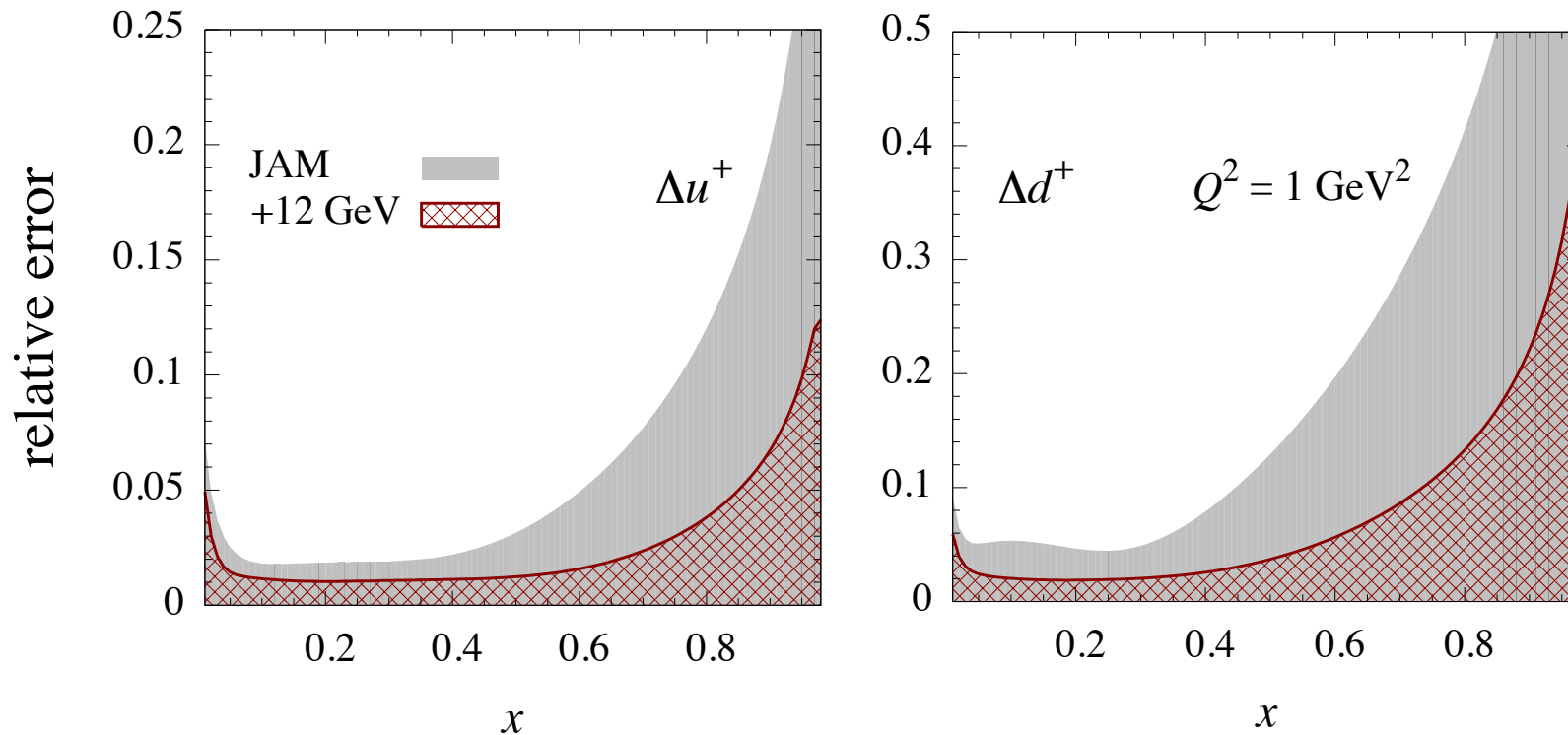
# JLab 12 GeV plans

- Several upcoming experiments at JLab will measure  $A_1(p, d, {}^3\text{He})$  up to  $x \sim 0.8$



# JLab 12 GeV plans

- Several upcoming experiments at JLab will measure  $A_1(p, d, {}^3\text{He})$  up to  $x \sim 0.8$



→ will significantly reduce PDF uncertainties at large  $x$

# Outlook

- Ongoing “CJ14” analysis includes new cross section data from JLab & collider experiments
  - allow for different HTs for  $F_2, F_L$  & isospin dependence
  - incorporate LHC ( $W, Z$ , jet production), PVDIS data
  - next release will include parametrisations of electroweak structure functions (down to low  $Q^2$ ) in addition to PDFs
- Next phase of JAM analysis will study polarisation of sea quarks and gluons
  - semi-inclusive DIS for flavour/antiflavour separation
  - polarised  $pp$  cross sections (inclusive jet & pion production) sensitive to  $\Delta g$

The End