

Uncertainties in determining the d  
quark PDF  
at large values of  $x$

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# Outline

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## Introduction

Cast of characters in the CTEQ-JLAB Collaboration - **Alberto Accardi**, Eric Christy, Cynthia Keppel, Simona Malace, Wally Melnitchouk, Peter Monaghan, Jorge Morfín, JFO, and Lingyan Zhu

Goals:

- Overall goal - Improve the precision of the  $d$  PDF
- Extend PDF fits to larger values of  $x$  and lower values of  $Q$
- Wealth of data from older SLAC experiments and newer JLAB experiments
- Study effects of different target mass correction methods
- Explore role of higher twist contributions
- Quantify the uncertainty due to nuclear corrections for deuteron targets
- Study the parametrization dependence of the results

## Motivation

- Traditional global fits focus on leading twist PDFs convoluted with hard scattering partonic cross sections
- Typically use DIS cuts similar to  $Q > 2 \text{ GeV}$  and  $W > 3.5 \text{ GeV}$
- Limits  $x$  coverage to  $x \lesssim 0.7$
- Goal is to relax the cuts in order to access higher values of  $x$
- Current results obtained with  $Q^2 > 1.69 \text{ GeV}^2$ ,  $W^2 > 3 \text{ GeV}^2$
- Current project results in arXiv:1102.3686

Previous analysis (Phys. Rev. **D81**:034016, 2010) showed the following

- Good fits could be obtained using the lower  $Q$  and  $W$  cuts on the DIS data
- Different target mass correction prescriptions gave equivalent fits as long as a simple parametrization of higher twist contributions was added
- Leading twist PDF was stable as the TMC prescription was varied

Residual questions:

- How do the results depend on the models used for the nuclear corrections for DIS data from deuterium targets (deuteron wavefunction, offshell corrections)?
- How do the results depend on the parametrization used for the  $d$  PDF?

# Information on the $d$ PDF

DIS

- $F_2^P(x, Q^2) \sim 4u + d$
- $F_2^d(x, Q^2) \sim 5(u + d)$ , but requires nuclear corrections

Lepton Pair Production

- $x_1 x_2 = \frac{M^2}{s}$  and  $x_F = x_1 - x_2$
- Can get to large  $x_1$  if high- $x_F$  data are available
- E-866 reaches to  $x \approx .8$
- $\sigma_{pp} \sim \bar{u}(x_2)[4u(x_1) + d(x_1)\bar{d}(x_2)/\bar{u}(x_2)]$
- $\sigma_{pn} \sim \bar{d}(x_2)[4u(x_1) + d(x_1)\bar{u}(x_2)/\bar{d}(x_2)]$
- At large  $x_F$ ,  $x_1 \gg x_2$
- To the extent that  $\bar{u}(x_2) \simeq \bar{d}(x_2)$ , which is roughly satisfied for small  $x_2$ , one is still sensitive to  $4u + d$

## $W$ asymmetry

- $x_{1,2} = \frac{M_W}{\sqrt{s}} e^{\pm y}$
- $W$  asymmetry directly sensitive to large  $x$   $d/u$  at large  $y$
- Effect is reduced if decay lepton asymmetry is used
- Newer data reach to  $x \approx .8$ , but the last bin is wide and the central value corresponds to  $x \approx .57$

## Vector boson production

- $W$  and  $Z$  production are sensitive to different linear combinations of PDFs than for Drell-Yan pairs
- Potential constraints from data at high values of rapidity

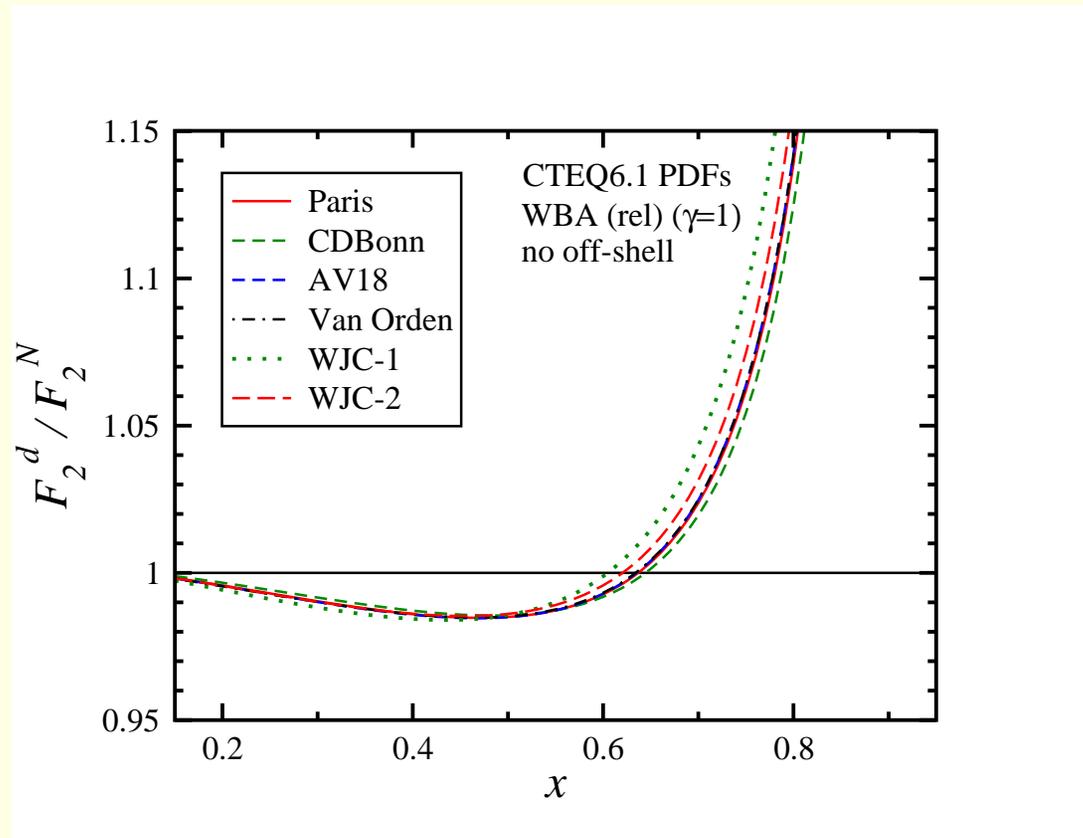
## Jet Data

- All parton pairs contribute, weighted by their respective subprocess cross sections
- Leads to an anticorrelation between the  $d$  PDF and the  $u$  and  $g$  PDFs

General idea is to study the effects of nuclear corrections and  $d$  PDF parametrization choices while watching the effects on various data sets

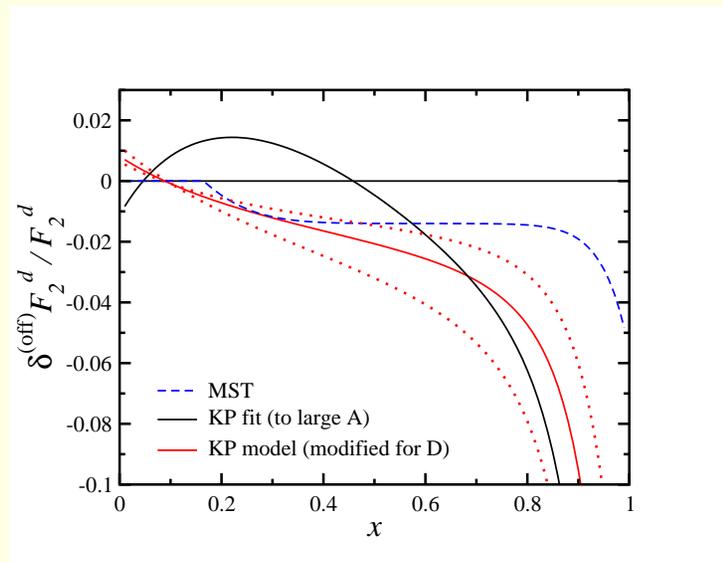
## Nuclear Corrections

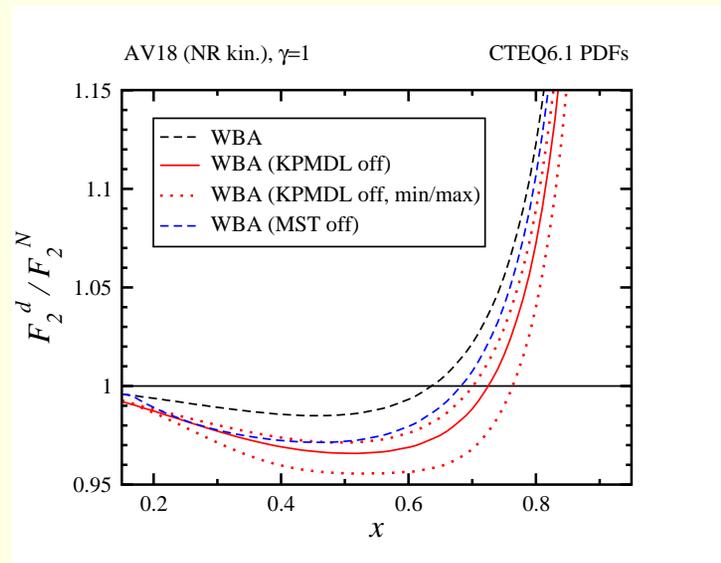
- Fermi motion smearing done using the Weak Binding Approximation (WBA) - see Sec. 2 of the current analysis for details
- Various choices of wavefunctions explored



## Offshell corrections

- Start with a parametrization due to Kulagin and Petti which is fitted to data for a range of heavy nuclei
- Parameters were adjusted (Wally Melnitchouk) to provide a range of corrections representative of the average offshellness of nucleons in a deuteron





- Easy way to think about the effects of the nuclear corrections on the PDFs
- The deuterium data are divided by this ratio, yielding effectively the sum of neutron and proton data
- When the ratio is less than one the data are enhanced and the  $d$  PDF will increase
- Conversely, the  $d$  PDF will be reduced when the ratio is greater than one

## Fitting Package

We are using my NLO DGLAP fitting package which I have continued to update and extend

- Can fit DIS, Drell-Yan,  $W$  lepton asymmetry, jets, and  $\gamma + \text{jet}$
- $W$  lepton asymmetry routine allows for a single  $p_T$  cut, but a generalization to allow for multiple  $p_T$  cuts has been developed
- Added PDF errors (Hessian method)
- Multiple TMC and HT terms added (Alberto Accardi)
- Some correlated errors added
- Options for nuclear corrections added (Wally Melnitchouk, Alberto Accardi)

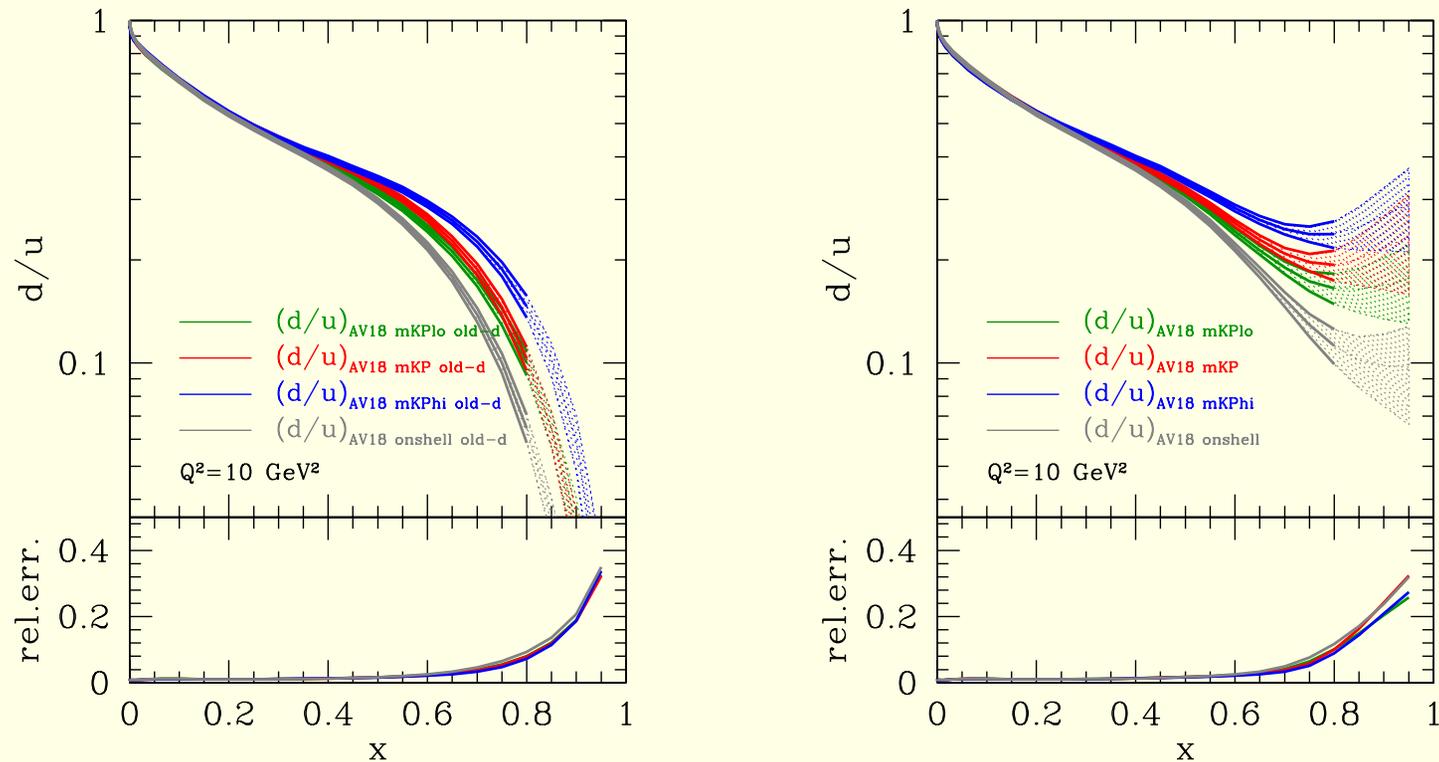
## Data Sets

- BCDMS, SLAC, NMC, H1, Zeus, and JLAB DIS data
- E-605 and E-866 lepton pair data
- CDF and D0 jet data
- $W$  asymmetry and  $W$ -lepton asymmetry data
- $D\bar{0}$   $\gamma + \text{jet}$  data
- Data sets similar to those used in CTEQ6.1 except CCFR removed, E-866 added,  $D\bar{0}$   $\gamma + \text{jet}$  added, and some new  $W$  asymmetry data added

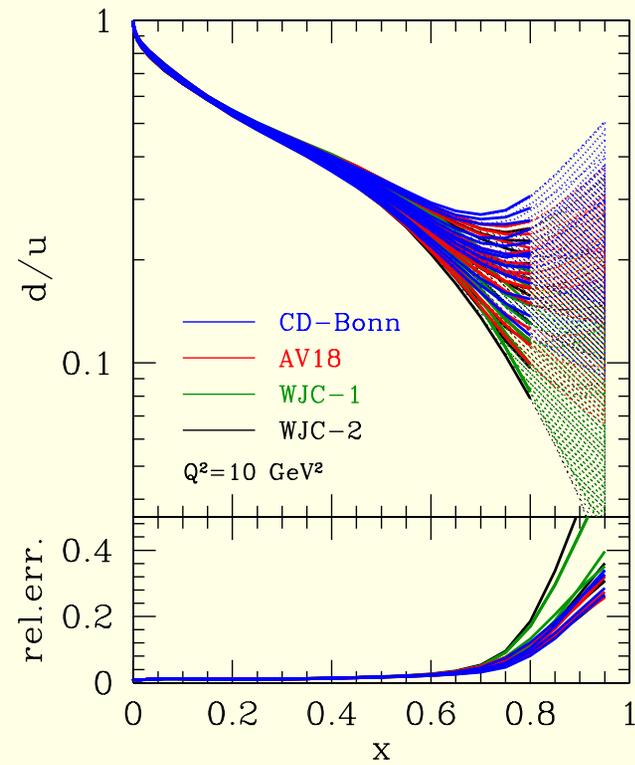
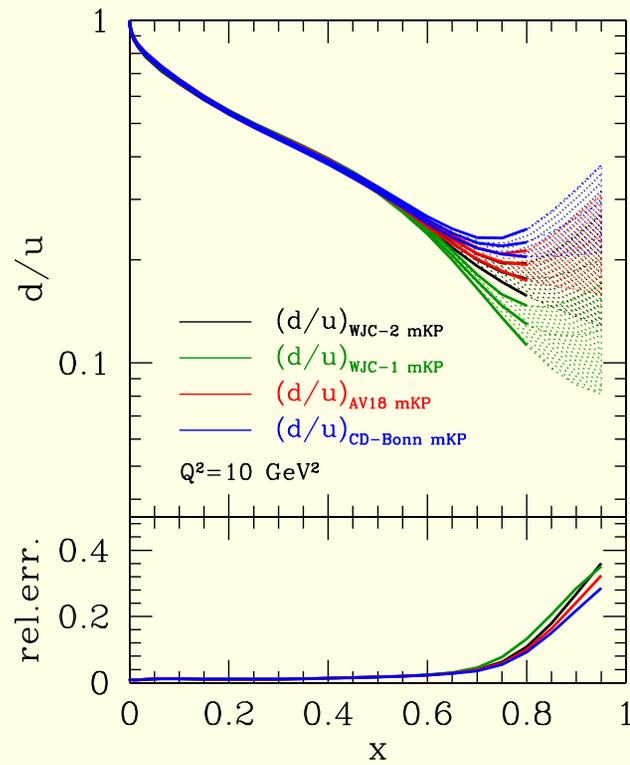
## Results

- Summarize results by showing  $d/u$  ratios
  - The  $u$  PDF is already well constrained
  - The different nuclear corrections have the largest effect on the  $d$  PDF
  - Basically, the  $d$  PDF shifts to accommodate whatever nuclear model is used and the other PDFs adjust to compensate for the shift
- Consider first a traditional parametrization where the  $d$  PDF vanishes as  $x \rightarrow 1$
- Then, compare to a parametrization where  $d \rightarrow d + c * u * x^b$  so that  $d/u \rightarrow c$  in the limit that  $x = 1$
- For clarity, the bands denote the PDF uncertainty resulting from the experimental errors with  $\Delta\chi = 1$

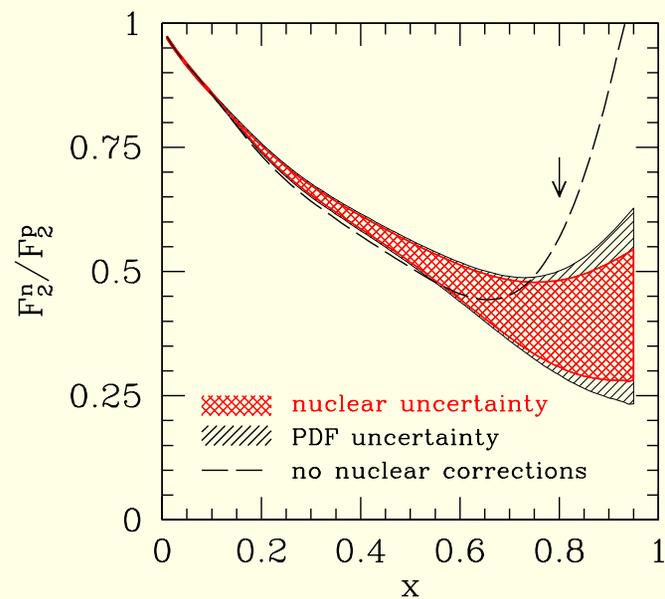
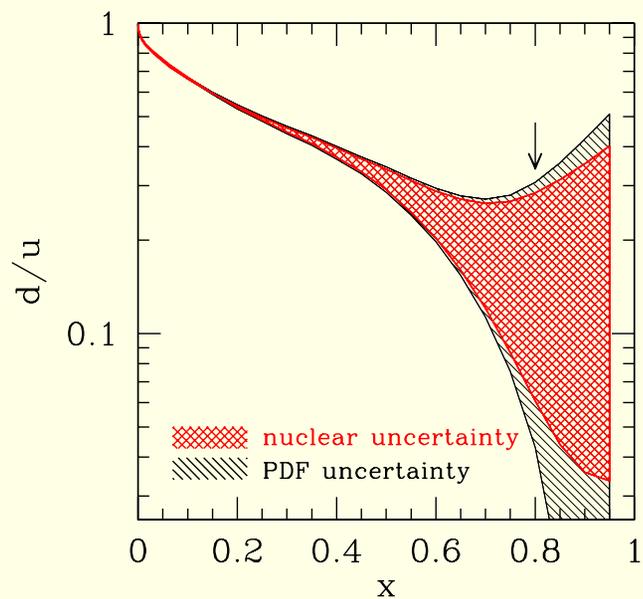
## Sample results obtained using the AV18 wavefunction



Either parametrization gives good fits, with a very slight chi square preference existing for the right-hand plots ( $d/u \rightarrow c$  at  $x = 1$ )

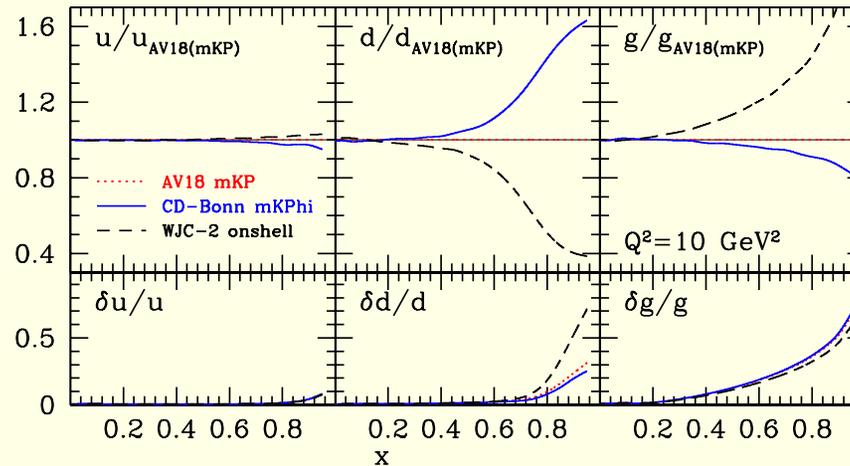


Left-hand plot shows the wavefunction dependence with a fixed offshell model while the right-hand plot shows the full effect of varying both the wavefunction and the offshell model



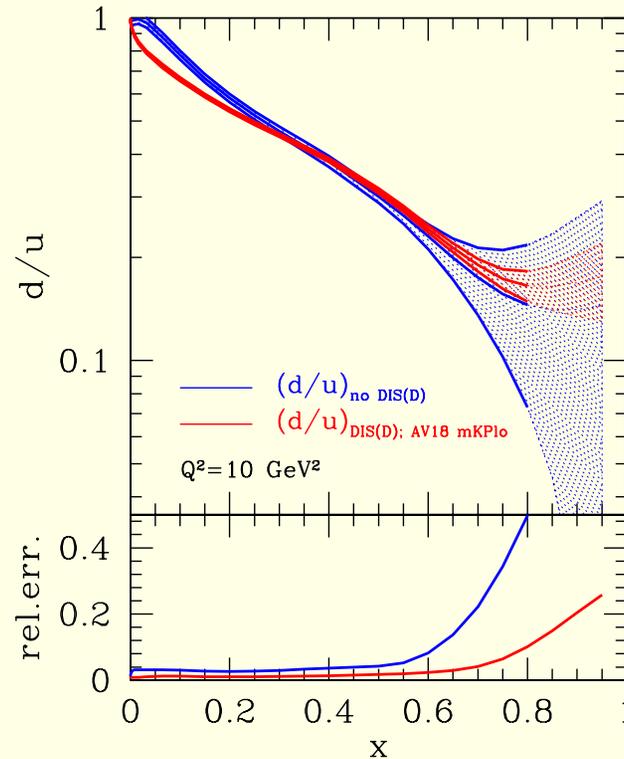
- These figures shows the resulting uncertainty bands for  $d/u$  and  $F_2^n/F_2^p$
- Neutron/proton  $F_2$  ratio is bounded below at  $1/4$
- Resulting uncertainty in the structure function ratio is reduced relative to that for the  $d/u$  ratio

Compare the PDFs resulting from the upper and lower extremes of the  $d/u$  ratios



- Center panels show the  $d$  PDFs for the upper and lower extremes
- A very small shift (few percent) in the  $u$  PDF compensates
- Primarily because the DIS and Drell Yan data are sensitive to  $4u + d = u(4 + d/u)$  in a region where  $d/u$  is already small
- Gluon PDF compensates the change in the  $d$  PDF for the jet data
- Uncertainty in the  $d$  PDF due to the variation of the nuclear corrections feeds into increased uncertainty in the large- $x$  gluon PDF

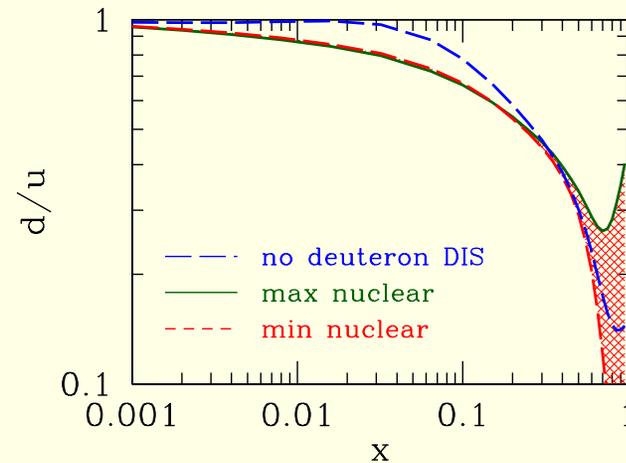
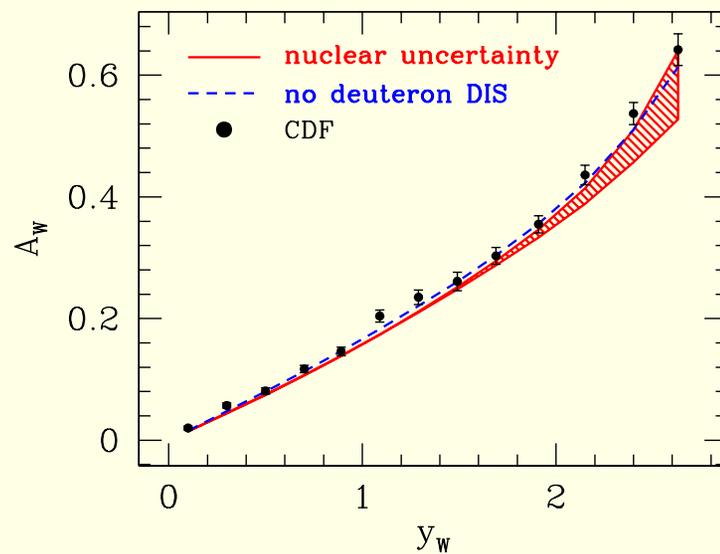
The figure below shows the result of removing the deuterium DIS data from the fit.



- For a fixed choice of the nuclear models the uncertainty on the  $d$  PDF is decreased when the deuterium data are included.
- Notice the relatively large shift in the  $d/u$  ratio at low values of  $x$
- Shift is unexpected based on standard error propagation

- Suggests that at least some of the deuterium DIS data (BCDMS, NMC, SLAC, and JLAB) is pulling against the other non-deuterium data sets
- Shadowing corrections are expected to be at the 1% level and can't account for the difference
- Suggests that the  $d$  PDFs may be underestimated at low values of  $x$
- Where else might this effect show up?

- CDF  $W$  asymmetry is not particularly sensitive to the nuclear corrections we have been studying - The weighted bin center for the highest rapidity bin corresponds to  $x = 0.57$
- On the other hand, the description of the data is improved significantly in the “No deuterium” fit.
- The  $W$  asymmetry data are providing about half of the chi square improvement and seem to be responsible for much of the shift shown previously when the deuterium DIS data are removed



## What can be done?

- How can one resolve the dilemma posed by the fact that the  $d$  PDF simply adjusts to whatever nuclear model is used while the other PDFs are anticorrelated and vary in order to maintain good fits to the non-deuterium data?
- Need new data which constrain the  $d$  PDF but which are not sensitive to nuclear corrections
- Examples include the BONUS, MARATHON, and PVDIS experiments at Jefferson Lab
- Could also consider experiments done with proton targets such as  $\nu$  and  $\bar{\nu}$  p DIS data, perhaps from the Minerva experiment. These will directly constrain the  $d/u$  ratio
- Another example - finer binning on  $W$  asymmetry data at high values of rapidity in order to get to large  $x$  values

## Current and Planned Developments

- Have extended the fitting package
  - Interfaced with FastNLO in order to handle NLO jet calculations for Tevatron Run I and Run II data sets
  - Added capability to fit HERA combined cross section data
  - Added NLO treatments of CDF and DØ  $Z$  rapidity distributions
- Currently updating the previous results
- Studying parametrization choices
- Plan to produce PDF sets using several representative sets of nuclear corrections

## Summary and Conclusions

- Nuclear corrections - Fermi smearing and offshell corrections - have significant effects on the behavior of  $d$  PDF when it is constrained by deuterium DIS data
- Good descriptions of the data are easily obtained and the  $d$  PDF varies significantly, depending on the nuclear model choice
- Other PDFs are anticorrelated with the  $d$  PDF (mostly the  $u$  and gluon PDFs) so that the fits to all other data sets are essentially independent of the nuclear corrections
- When the deuterium DIS data are removed from the fits there is a significant shift of the  $d/u$  ratio, especially at low values of  $x$ , suggesting that one or more of the remaining data sets is pulling against the deuterium DIS data
- One strong source of such a pull is the  $W$  asymmetry data from CDF - its description is much improved without the deuterium data in the fit
- To further constrain the  $d$  PDF we need data which are sensitive to the  $d$  PDF while not being sensitive to nuclear corrections. This includes experiments such as MARATHON, BONUS, and PVDIS. It also includes additional observables taken on proton targets.